

5.6

$$a.) \vec{r} = \hat{i}(x_0 + R \cos \omega t) + \hat{j} R \sin \omega t$$

$$\dot{\vec{r}} = -\hat{i} \omega R \sin \omega t + \hat{j} \omega R \cos \omega t$$

$$\dot{\vec{r}} \cdot \dot{\vec{r}} = v^2 = \omega^2 R^2$$

$$v = \omega R$$

$$b.) \dot{\vec{r}} = \vec{v} = -\vec{\omega} \times \vec{r} \text{ ketika } \vec{r} = \hat{i}x' + \hat{j}y'$$

$$= -\hat{i} \omega R \sin \omega t + \hat{j} \omega R \cos \omega t - \omega \hat{k} \times (\hat{i}x' + \hat{j}y')$$

$$= -\hat{i} \omega R \sin \omega t + \hat{j} \omega R \cos \omega t - \hat{j} \omega x' + \hat{i} \omega y'$$

$$\dot{x}' = \omega y' - \omega R \sin \omega t$$

$$\dot{y}' = -\omega x' + \omega R \cos \omega t$$

$$c.) u' = x' + iy' = i \sqrt{-1}!$$

$$\dot{u}' = \dot{x}' + i\dot{y}' = \omega y' - \omega R \sin \omega t - i\omega x' + i\omega R \cos \omega t$$

$$i\omega u' = -\omega y' + i\omega x'$$

$$\Rightarrow \dot{u}' + i\omega u' = -\omega R \sin \omega t + i\omega R \cos \omega t = i\omega R e^{i\omega t}$$

$$u' = A e^{-i\omega t} + B e^{i\omega t}$$

$$\dot{u}' = -i\omega A e^{-i\omega t} + i\omega B e^{i\omega t}$$

$$i\omega u' = i\omega A e^{-i\omega t} + i\omega B e^{i\omega t}$$

$$\Rightarrow \dot{u}' + i\omega u' = i(\omega + \omega) B e^{i\omega t}, \text{ maka } B = \frac{\omega R}{\omega + \omega}$$

$$u' = A + B = x'(0) + iy(0) = x_0 + iR$$

$$\Rightarrow A = x_0 + R - B$$

$$= x_0 + R - \frac{\omega R}{\omega + \omega}, \text{ maka } A = x_0 + \frac{\omega R}{\omega + \omega}$$

$$u' = \left[x_0 + \frac{\omega R}{\omega + \omega} \right] e^{-i\omega t} + \frac{\omega R}{\omega + \omega} e^{i\omega t}$$

5.7

$$a.) \begin{matrix} s \\ n(t) \end{matrix} = \begin{matrix} R a \cos \omega t \\ R a \sin \omega t \end{matrix}$$

$$\begin{matrix} s \\ e(t) \end{matrix} = \begin{matrix} R e \cos \omega t \\ R e \sin \omega t \end{matrix}$$

$$\frac{e}{a} = \frac{s}{a} \cdot \frac{s}{e}$$

$$\frac{e}{a}(t) = \begin{matrix} R a \cos \omega t - R e \cos \omega t \\ R a \sin \omega t - R e \sin \omega t \end{matrix}$$

$$r^e = r^i_a - r^i_e$$

$$r^e(t) = \begin{bmatrix} R_a \cos \omega_a t - R_e \cos \omega_e t \\ R_a \sin \omega_a t - R_e \sin \omega_e t \end{bmatrix}$$

$$b.) \quad v^e_a(t) = \frac{d}{dt} r^e_a(t)$$

$$\begin{bmatrix} -\omega_a R_a \sin \omega_a t + \omega_e R_e \sin \omega_e t \\ \omega_a R_a \cos \omega_a t - \omega_e R_e \cos \omega_e t \end{bmatrix}$$

$$t = 0$$

$$v^e_a(t) = 0 \begin{bmatrix} 0 \\ \omega_a R_a - \omega_e R_e \end{bmatrix}$$

$$c.) \quad a^e_a(t) = \frac{d}{dt} v^e_a(t)$$

$$= \begin{bmatrix} -\omega_a^2 R_a \cos \omega_a t + \omega_e^2 R_e \sin \omega_e t \\ -\omega_a^2 R_a \sin \omega_a t + \omega_e^2 R_e \cos \omega_e t \end{bmatrix}$$