

Nama : Neb Safitri

NPM : 2013022006

Prodi : Pendidikan Fisika (B)

Tugas Mekanika

4.1). a. $V = Cxyz + C$

$$\Rightarrow \text{jawab: } \vec{F} = -\vec{\nabla} V = -\hat{i} \frac{\partial V}{\partial x} - \hat{j} \frac{\partial V}{\partial y} - \hat{k} \frac{\partial V}{\partial z} = -C (\hat{i}yz + \hat{j}xz + \hat{k}xy)$$

b. $V = \alpha x^2 + \beta y^2 + \gamma z^2 + C$

$$\Rightarrow \text{jawab: } \vec{F} = -\vec{\nabla} V = -\hat{i} 2\alpha x - \hat{j} 2\beta y - \hat{k} 2\gamma z$$

c. $V = Ce^{-(\alpha x + \beta y + \gamma z)}$

$$\Rightarrow \text{jawab: } \vec{F} = -\vec{\nabla} V = Ce^{-(\alpha x + \beta y + \gamma z)} (\hat{i}\alpha + \hat{j}\beta + \hat{k}\gamma)$$

d. $V = Cr^n$ dalam koordinat bola

$$\Rightarrow \text{jawab: } \vec{F} = -\vec{\nabla} V = -\hat{e}_r \frac{\partial V}{\partial r} - \hat{e}_\theta \frac{1}{r} \frac{\partial V}{\partial \theta} - \hat{e}_\phi \frac{1}{r \sin \theta} \frac{\partial V}{\partial \phi}$$

4.2) a. $F = ix + jy + kz$

$$\Rightarrow \text{jawab: } \vec{\nabla} \times \vec{F} = \begin{vmatrix} \hat{i} & \hat{j} & \hat{k} \\ \frac{\partial}{\partial x} & \frac{\partial}{\partial y} & \frac{\partial}{\partial z} \\ x & y & z \end{vmatrix} = 0 \rightarrow \text{konservatif}$$

b. $F = ix - jy + kz^2$

$$\Rightarrow \text{jawab: } \vec{\nabla} \times \vec{F} = \begin{vmatrix} \hat{i} & \hat{j} & \hat{k} \\ \frac{\partial}{\partial x} & \frac{\partial}{\partial y} & \frac{\partial}{\partial z} \\ x & -y & z^2 \end{vmatrix} = \hat{k} (-1-1) \neq 0 \rightarrow \text{tidak konservatif}$$

c. $F = ix + jy + kz^3$

$$\Rightarrow \text{jawab: } \vec{\nabla} \times \vec{F} = \begin{vmatrix} \hat{i} & \hat{j} & \hat{k} \\ \frac{\partial}{\partial x} & \frac{\partial}{\partial y} & \frac{\partial}{\partial z} \\ x & y & z^3 \end{vmatrix} = \hat{k} (1-1) = 0 \rightarrow \text{konservatif}$$

d. $F = -kr^{-n} \hat{e}_r$ dalam koordinat bola

$$\Rightarrow \text{jawab: } \vec{\nabla} \times \vec{F} = \frac{1}{r^2 \sin \theta} \begin{vmatrix} \hat{e}_r & \hat{e}_\theta & \hat{e}_\phi \\ \frac{\partial}{\partial r} & \frac{1}{r} \frac{\partial}{\partial \theta} & \frac{1}{r \sin \theta} \frac{\partial}{\partial \phi} \\ -kr & 0 & 0 \end{vmatrix} = 0 \rightarrow \text{konservatif}$$

4.3) a. $F = i\alpha y + j\alpha x^2 + k\alpha z^3$

$$\Rightarrow \text{jawab: } \vec{\nabla} \times \vec{F} = \begin{vmatrix} \hat{i} & \hat{j} & \hat{k} \\ \frac{\partial}{\partial x} & \frac{\partial}{\partial y} & \frac{\partial}{\partial z} \\ \alpha y & \alpha x^2 & \alpha z^3 \end{vmatrix} = \alpha (2(x-x))$$

$$2(x-x) = 0 \rightarrow C = 1/2$$

$$b. F = i \left(\frac{z}{y} \right) + j \left(\frac{xz}{y^2} \right) + k \left(\frac{x}{y} \right)$$

$$\Rightarrow \text{Jawab: } \vec{\nabla} \times \vec{F} = \begin{vmatrix} \hat{i} & \hat{j} & \hat{k} \\ \frac{\partial}{\partial x} & \frac{\partial}{\partial y} & \frac{\partial}{\partial z} \\ xy & xz & z^2 \end{vmatrix} = k$$

$$c. F = i \left(\frac{z}{y} \right) + sj \left(\frac{xz}{y^2} \right) + k \left(\frac{x}{y} \right)$$

$$\Rightarrow \text{Jawab: } \vec{\nabla} \times \vec{F} = \begin{vmatrix} \hat{i} & \hat{j} & \hat{k} \\ \frac{\partial}{\partial x} & \frac{\partial}{\partial y} & \frac{\partial}{\partial z} \\ \frac{z}{y} & \frac{cxz}{y^2} & \frac{x}{y} \end{vmatrix} = \hat{i} \left(\frac{-x}{y} - \frac{cx}{y^2} \right) + \hat{j} \left(\frac{1}{y} - \frac{1}{y} \right) + \hat{k} \left(\frac{cz}{y^2} + \frac{z}{y^2} \right)$$

$$\frac{-x}{y} - \frac{cx}{y^2} = 0 \rightarrow c = -1 \quad \text{dan} \quad \frac{cz}{y^2} + \frac{z}{y^2} = 0 \rightarrow c = -1$$

4.4] a. $E = \text{konstan} = V(x, y, z) + \frac{1}{2} mv^2$

diambilnya $E = 0 + \frac{1}{2} mv^2$

Pada (1,1,1) $E = x + y + z + \frac{1}{2} mv^2 = \frac{1}{2} mv^2$

b. $V_0 = \frac{2}{m} (x + y + z) = 0$

$$V_0 = \left[\frac{2}{m} (x + y + z) \right]^{1/2}$$

c. $m\ddot{x} = F_x = -2V/x$

$$m\ddot{x} = -x$$

$$m\ddot{y} = \frac{-2V}{2y} = -2y$$

$$m\ddot{z} = \frac{-2V}{2z} = -3yz^2$$

4.5] . Pertimbangkan 2 fungsi gaya

(a). $F = \hat{i}x + \hat{j}y$

$$\Rightarrow \text{Jawab: } \vec{F} = \hat{i}x + \hat{j}y$$

$$\text{di } x = y, \quad d\vec{r} = \hat{i} dx + \hat{j} dy$$

$$\int_{(0,0)}^{(1,1)} \vec{F} \cdot d\vec{r} = \int_0^1 x dx + \int_0^1 y dy = \int_0^1 x dx + \int_0^1 y dy = -1$$

Pada lintasan sepanjang sumbu $x = \vec{dr} = \hat{i} dx$

dan pada garis $x = 1$

$$\int_{(0,0)}^{(1,1)} \vec{F} \cdot d\vec{r} = \int_0^1 F_x dx + \int_0^1 F_y dy = 1, \quad \vec{F} = \text{konseratif}$$

(b). $\vec{F} = \hat{i}y - \hat{j}x$

$$\text{di } x = y: \int_{(0,0)}^{(1,1)} \vec{F} \cdot d\vec{r} = \int_0^1 y dx + \int_0^1 (-x) dy = \int_0^1 y dx - \int_0^1 x dy$$

dan, dengan $x = y$ $\int_{(0,0)}^{(1,1)} \vec{F} \cdot d\vec{r} = \int_0^1 x dx - \int_0^1 y dy = 0$

pada sumbu $x = \int_{(0,0)}^{(1,1)} \vec{F} \cdot d\vec{r} = \int_0^1 x dx = \int_0^1 y dx = 0$

dan, dengan $y = 0$ pada sumbu x $\int_{(0,0)}^{(1,0)} \vec{F} \cdot d\vec{r} = 0$

pada garis $x = 1$ $\int_{(1,0)}^{(1,1)} \vec{F} \cdot d\vec{r} = \int_0^1 y dy = \int_0^1 x dy$

dan, dengan $x = 1$ $\int_{(1,0)}^{(1,1)} \vec{F} \cdot d\vec{r} = \int_0^1 dy = 1$

pada jalur ini $\int_{(0,0)}^{(1,1)} \vec{F} \cdot d\vec{r} = 0 + 1 = 1, \vec{F} = \text{tidak konservatif}$

4.6). Dari contoh 2.3.2, $V(r) = -mg \frac{re^2}{(re+z)}$

$$V(z) = -mgre (1 + z/re)^{-1}$$

$$V(z) = -mgre (1 - z/re + z^2/re^2 + \dots)$$

$$V(z) = -mgre + mgz - mgz^2/re^2 + \dots$$

dengan $-mgre$ sebuah konstan

$$V(z) = mgz (1 - z/re)$$

$$\vec{F} = -\vec{\nabla} V = -\hat{e}_z \frac{\partial}{\partial z} V(z)$$

$$= -\hat{e}_z mg [1 - z/re + z^2/re^2]$$

$$\vec{F} = -\hat{e}_z mg (1 - z^2/re)$$

$$m\ddot{x} = F_x = 0$$

$$m\ddot{z} = -mg (1 - z^2/re)$$

$$\int_{v_z}^0 \dot{z} dz = -g \int_0^h (1 - z^2/re) dz$$

$$\frac{1}{2} v_z^2 = -g (h - h^3/re)$$

$$h^3 - reh + rev^2 z / 2g = 0$$

$$h - reh + rev^2 z / 2g = 0$$

$$h = re \left[1 - \frac{1}{2} \sqrt{1 - \frac{rev^2 z}{gre}} \right] \quad (h, z < re)$$

$$h = \frac{re}{2} - \frac{re}{2} \sqrt{1 - \frac{rev^2 z}{gre}}$$

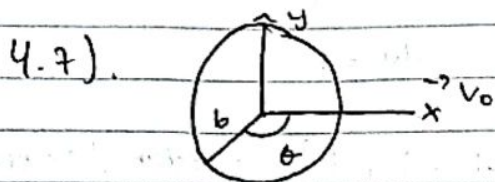
$$(1+x)^{1/2} = 1 + x/2 - x^2/8 + \dots$$

$$h = \frac{re}{2} - \frac{re}{2} + \frac{rev^2 z}{4g} + \frac{rev^4 z^2}{4gre} + \dots$$

$$h = \frac{v_{0y}^2}{2g} \left(1 + \frac{v_{0x}^2}{2gr} \right)$$

dan contoh 2.3.2 $h = \frac{v_0^2}{2g} \left(1 - \frac{v_0^2}{2gr} \right)^{-1}$

dan dengan $(1-x)^{-1} \approx 1+x$, $h \approx \frac{v_0^2}{2g} \left(1 + \frac{v_0^2}{2gr} \right)$



$$\vec{r}' = \hat{i} b \cos \theta - \hat{j} b \sin \theta$$

$$\theta = \omega t = \frac{v_0 t}{b} \Rightarrow \text{jadi } \vec{r}' = -\hat{i} v_0 \sin \theta - \hat{j} v_0 \cos \theta$$

Partikel keluar tepi = $y_0 = -b \sin \theta$ dan $v_{0y} = -v_0 \cos \theta$

Jadi, $v_y = v_{0y} - gt = -v_0 \cos \theta - gt$ dan $y = -b \sin \theta -$

$$v_0 t \cos \theta - \frac{1}{2} g t^2$$

tinggi maksimum $v_y = 0$

$$t = \frac{-v_0 \cos \theta}{g}$$

$$h = -b \sin \theta - v_0 \left(\frac{-v_0 \cos \theta}{g} \right) \cos \theta - \frac{1}{2} g \left(\frac{-v_0 \cos \theta}{g} \right)^2$$

$$h = -b \sin \theta = \frac{v_0^2 \cos^2 \theta}{2g}$$

h maksimum terjadi untuk $\frac{dh}{d\theta} = 0 = -b \cos \theta - \frac{2 v_0^2 \cos \theta \sin \theta}{2g}$

$$\sin \theta = \frac{-gb}{v_0^2}$$

$$\cos^2 \theta = 1 - \sin^2 \theta = \frac{v_0^4 - g^2 b^2}{v_0^4}$$

$$h_{\max} = \frac{gb^2}{v_0^2} + \frac{v_0^4 g^2 b^2}{2g v_0^4} = \frac{gb^2}{2v_0^2} + \frac{v_0^2}{2g}$$

(umpir meninggalkan roda di $\theta = \sin^{-1} \left(-\frac{gb}{v_0^2} \right)$)

4.8). $x = R \cos \phi$ dan $x = v_0 x t = (v_0 \cos \alpha) t$

Jadi, $t = \frac{R \cos \phi}{v_0 \cos \alpha}$

$y = R \sin \phi$ dan $y = v_0 y t = -\frac{1}{2} g t^2 = (v_0 \sin \alpha) t - g t^2$

$$R \sin \phi = (v_0 \sin \alpha) \frac{R \cos \phi}{v_0 \cos \alpha} - \frac{1}{2} g \left(\frac{R \cos \phi}{v_0 \cos \alpha} \right)^2$$

$$\sin \phi = \tan \phi \cos \phi = \frac{gR \cos^2 \phi}{2V_0^2 \cos^2 \phi}$$

$$R = \frac{2V_0^2 \cos^2 \phi}{g \cos \phi} (\tan \phi \cos \phi - \sin \phi) = \frac{2V_0^2 \cos \phi}{g \cos^2 \phi} (\sin \phi \cos \phi - \sin \phi)$$

$$\sin(\phi + \phi) = \sin \phi \cos \phi + \cos \phi \sin \phi$$

$$R = \frac{2V_0^2 \cos^2 \phi}{g \cos^2 \phi} \sin(2\phi)$$

$$R \text{ maks. untuk } \frac{dR}{d\phi} = 0 = \frac{2V_0^2}{g \cos^2 \phi} [-\sin 2\phi \sin(2\phi) + \cos 2\phi \cos(2\phi)]$$

$$\cos(\phi + \phi) = \cos \phi \cos \phi - \sin \phi \sin \phi \text{ jadi } \cos(2\phi) = 0$$

$$2\phi = \pi/2 \quad \phi = \pi/4$$

$$R_{\max} = \frac{2V_0^2}{g \cos^2 \phi} \cos\left(\frac{\pi}{4} + \frac{\phi}{2}\right) \sin\left(\frac{\pi}{4} - \frac{\phi}{2}\right)$$

$$\sin\left(\frac{\pi}{4} - \frac{\phi}{2}\right) = \cos\left[\frac{\pi}{2} - \left(\frac{\pi}{4} - \frac{\phi}{2}\right)\right] = \cos\left(\frac{\pi}{4} + \frac{\phi}{2}\right)$$

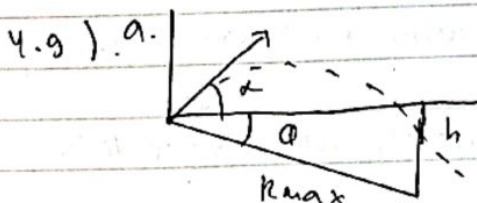
$$R_{\max} = \frac{2V_0^2}{g \cos^2 \phi} \cos^2\left(\frac{\pi}{4} + \frac{\phi}{2}\right)$$

$$R_{\max} = \frac{2V_0^2}{g \cos^2 \phi} \left[\frac{1}{2} \cos\left(\frac{\pi}{2} + \phi\right) + \frac{1}{2} \right] = \frac{V_0^2}{g \cos^2 \phi} [\cos(\frac{\pi}{2} + \phi) + 1]$$

$$\text{menggunakan } \cos\left(\frac{\pi}{2} + \phi\right) = -\sin \phi$$

$$R_{\max} = \frac{V_0^2}{g(1 - \sin \phi)}$$

$$= \frac{V_0^2}{g(1 + \sin \phi)}$$



$$R = \frac{2V_0^2}{g} \frac{\cos \phi \sin \phi}{\cos^2 \phi} (\cos \phi + \sin \phi)$$

$$-b = \dots R_{\max} = V_0^2(1 + \sin \phi) \text{ dan}$$

$$2\phi = \pi/2 = d$$

$$R_{\max} = \frac{h}{\sin \phi} = \frac{V_0^2}{g} \frac{(1 + \sin d)}{\cos^2 \phi} = \frac{V_0^2}{g(1 - \sin \phi)}$$

$$\sin \phi = \frac{gh}{V_0^2} \left/ \left(1 + \frac{gh}{V_0^2}\right)\right.$$

$$\sin \phi = \sin\left(\frac{\pi}{2} - 2\phi\right) = \cos 2\phi = 1 - 2\sin^2 \phi$$

$$1 - 2\sin^2 \phi = \frac{gh}{V_0^2} \left/ \left(1 + \frac{gh}{V_0^2}\right)\right.$$

$$2\sin^2 \phi = \frac{2}{1 + \frac{gh}{V_0^2}} = \frac{1}{1 + \frac{gh}{V_0^2}}$$

$$\text{akhirnya } = \sin^2 \phi = \frac{1}{2\left(1 + \frac{gh}{V_0^2}\right)}$$

$$b). R_{\max} = \frac{h}{\sin 4} = \frac{h}{1 - 2\sin^2 x} = \frac{h}{1 - 2/\cos^2 x}$$

$$R_{\max} = \frac{v_0^2}{g} \left(1 + \frac{2h}{v_0^2} \right)$$

4.12) a. x dan z adalah posisi bola

$$x = v_0 t \cos \frac{1}{2} \theta_0, \quad z = v_0 t \cos \frac{1}{2} \theta_0 \sin \theta_0 - \frac{1}{2} g t^2$$

$$\text{sejak } v_x = v_0 \cos \frac{1}{2} \theta_0,$$

$$R = \frac{v_0^2}{g} \cos^2 \frac{1}{2} \theta_0 \sin 2\theta_0$$

$$\text{maks } \frac{dR}{d\theta} = 0$$

$$\frac{dR}{d\theta} = \frac{v_0^2}{g} (2 \cos^2 \frac{1}{2} \theta_0 \cos 2\theta_0 - \cos \frac{1}{2} \theta_0 \sin 2\theta_0)$$

$$\sin \frac{1}{2} \theta_0 \sin 2\theta_0 = 0$$

$$2 \cos^2 \frac{1}{2} \theta_0 \cos 2\theta_0 = \cos \frac{1}{2} \theta_0 \sin \frac{1}{2} \theta_0 \sin 2\theta_0$$

$$2 \cos^2 \theta_0 = 1 + \cos 2\theta_0 \text{ dan } \sin 2\theta_0 = 2 \sin \theta_0 \cos \theta_0$$

$$\text{didapat } = (1 + \cos \theta_0) (2 \cos^2 \theta_0 - 1) = \sin \theta_0 \sin \theta_0$$

$$\cos \theta_0 = (1 - \cos^2 \theta_0) \cos \theta_0$$

$$\text{atau } (1 + \cos \theta_0) (3 \cos^2 \theta_0 - \cos \theta_0 - 1) = 0$$

hanya akar Pokrif yang berlaku adalah $\theta_0, 0 \leq \theta_0 \leq \pi/2$

$$\cos \theta_0 = \frac{1}{6} (1 + \sqrt{13}) = 0,7676 \quad \theta_0 = 39^\circ 51'$$

$$b. \text{ Untuk } v_0 = 25 \text{ m/s}, \quad R_{\max} = 55,4 \text{ m} \quad \theta_0 = 39^\circ 51'$$

$$\text{maks } \frac{dz}{dt} = 0$$

$$v_0 \cos \frac{1}{2} \theta_0 \sin \theta_0 = gT \text{ atau } T = \frac{v_0 \cos \frac{1}{2} \theta_0 \sin \theta_0}{g}$$

$$\text{atau } H = \frac{v_0^2}{2g} \cos^2 \frac{1}{2} \theta_0 \sin^2 \theta_0, \text{ maks. tetap di } \theta_0$$

maks. pada ketinggian tetap terjadi $dH = 0$

$$\frac{dH}{d\theta} = \frac{v_0^2}{2g} (2 \cos^2 \frac{1}{2} \theta_0 \sin \theta_0 \cos \theta_0 - \cos \frac{1}{2} \theta_0 \sin^2 \theta_0) = 0$$

$$(1 + \cos \theta_0) \sin \theta_0 \cos \theta_0 = \frac{1}{2} \sin \theta_0 \sin^2 \theta_0 =$$

$$\frac{1}{2} \sin \theta_0 (1 - \cos^2 \theta_0) / \sin \theta_0 (1 + \cos \theta_0) (3 \cos \theta_0 - 1) = 0$$

$$\sin \theta_0 = 0 \quad \cos \theta_0 = -1$$

$$\text{Jadi } H_{\max} = 18,9 \text{ m} \quad \theta_0 = \cos^{-1} \frac{1}{3} = 70,32^\circ$$

4.13). r menggantikan x

$$z = \frac{\dot{r}_0}{r_0} r - \frac{g}{2\dot{r}_0^2} r^2 \text{ dimana } \dot{r}_0 = V_0 \cos \theta_0 \quad \dot{z}_0 = V_0 \sin \theta_0$$

$$z = r \tan \theta_0 - \frac{gr}{2V_0^2} \sec^2 \theta \text{ jika } \sec^2 \theta_0 = 1 + \tan^2 \theta$$

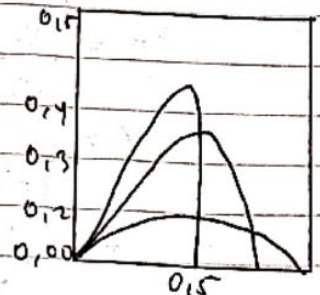
$$\frac{gr}{2V_0^2} \tan^2 \theta_0 - r \tan \theta_0 + z + \frac{gr}{2V_0^2} = 0$$

(r, z) titik koordinat

$$\tan \theta_0 = \frac{1}{gr} \left[V_0^2 \pm (V_0^4 - g^2 V_0^2 - g^2 r^2)^{1/2} \right]$$

$$V_0^4 - 2g^2 V_0^2 - g^2 r^2 \geq 0$$

Permukaan kritis oleh karena itu $V_0^4 - 2g^2 V_0^2 - g^2 r^2 = 0$



4.17). $m\ddot{x} = f_x = -\frac{\partial V}{\partial x} = -kx = -\pi^2 mx$

$$x = A \cos \left(\sqrt{\frac{k}{m}} t + \angle \right) = A \cos (\pi t + \angle)$$

$$m\ddot{y} = -\frac{\partial V}{\partial y} = 4\pi^2 m y$$

$$y = B \cos (2\pi t + \beta)$$

$$m\ddot{z} = -\frac{\partial V}{\partial z} = -g\pi^2 m z$$

$$z = C \cos (3\pi t + \gamma)$$

Sejak $x = y = z = 0$ Pada $t = 0$ $\alpha = \beta = \gamma = -\pi/2$

$$x = A \cos (\pi t - \pi/2) = A \sin \pi t$$

$$\dot{x}_0 = A\pi \cos \pi t$$

$$V_0^2 = \dot{x}_0^2 + \dot{y}_0^2 + \dot{z}_0^2 \text{ dan } \ddot{x}_0 = \ddot{y}_0 = \ddot{z}_0$$

$$\dot{x}_0 = \frac{V_0}{\sqrt{3}} = A\pi$$

$$A = \frac{V_0}{\pi\sqrt{3}}$$

$$x = \frac{V_0}{\pi\sqrt{3}} \sin \pi t$$

$$y = B \sin 2\pi t, \quad y = 2B\pi \cos 2\pi t$$

$$\dot{y}_0 = \frac{V_0}{2} = 2\pi B$$

$$B = \frac{\sqrt{3}}{2\pi\sqrt{3}}$$

$$y = \frac{V_0}{2\pi\sqrt{3}} \sin 2\pi t$$

$$z = C \sin 3\pi t$$

$$\dot{z}_0 = \frac{V_0}{\sqrt{3}} = 3\pi t$$

$$\dot{z} = 3C\pi \cos 3\pi t$$

$$\dot{z}_0 = \frac{V_0}{\sqrt{3}} = 3C\pi$$

$$C = \frac{V_0}{3\pi\sqrt{3}}$$

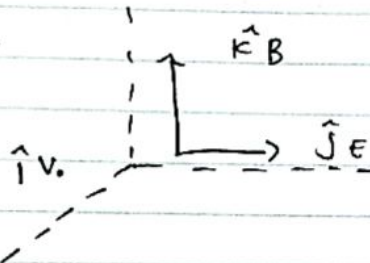
$$z = \frac{V_0}{3\pi\sqrt{3}} \sin 3\pi t$$

sejak $\omega_x = \pi$, $\omega_y = 2\pi$ dan $\omega_z = 3\pi$, maka

$$I_{\min} = \frac{2\pi n}{\omega_x} = \frac{2\pi n_2}{\omega_y} = \frac{2\pi n_3}{\omega_z}$$

waktu Maks pada $n_1=1, n_2=2, n_3=3$ $t_{\min} = \frac{2\pi}{\pi} = 2$

4.20).



$$\vec{F} = q(\vec{E} + \vec{v} \times \vec{B})$$

$$\vec{v} \times \vec{B} = (\hat{i}\dot{x} + \hat{j}\dot{y} + \hat{k}\dot{z}) \times B\hat{k} = \hat{i}\dot{y}B - \hat{j}\dot{x}B$$

$$\vec{F} = \hat{i}q\dot{y}B + \hat{j}q(\dot{x} - \dot{z}B)$$

$$m\ddot{x} = F_x = q\dot{y}B$$

$$\dot{x} - \dot{x}_0 = \frac{qB}{m} y$$

$$m\ddot{y} = F_y = q\dot{x}B - q\dot{z}B = qB(\dot{x} - \dot{z})$$

$$\ddot{y} = \frac{qB}{m}(\dot{x} - \dot{z}) = \frac{qB}{m}(\dot{x}_0 - \dot{z}_0 + \frac{qB}{m}y) = \frac{qB}{m}\dot{x}_0 - \frac{qB}{m}\dot{z}_0 + \left(\frac{qB}{m}\right)^2 y$$

$$\ddot{y} + \omega^2 y = -\frac{qB}{m}\dot{x}_0 + \frac{qB}{m}\dot{z}_0$$

$$y = \frac{1}{\omega^2} \left(-\frac{qB}{m}\dot{x}_0 + \frac{qB}{m}\dot{z}_0 \right) + A \cos(\omega t + \theta_0)$$

$$\dot{y} = -A\omega \sin(\omega t + \theta_0)$$

$$\dot{y}_0 = 0, \text{ Jadi } \theta_0 = 0, A = -\frac{1}{\omega^2} \left(-\frac{qB}{m}\dot{x}_0 + \frac{qB}{m}\dot{z}_0 \right)$$

$$y = \frac{1}{\omega^2} (1 - \cos \omega t), a = \frac{1}{\omega^2} (-\frac{qB}{m}\dot{x}_0 + \frac{qB}{m}\dot{z}_0)$$

$$\dot{x} = \dot{x}_0 = \frac{qB}{m} y = \dot{x}_0 - \omega a (1 - \cos \omega t)$$

$$x = (\dot{x}_0 - \omega a) t + a \sin \omega t$$

$$x = a \sin \omega t + b t, \quad b = \dot{x}_0 - \omega a$$

$$m\ddot{z} = F_z = 0$$

$$\dot{z} = \dot{z}_0 t + \dot{z}_0 = 0$$