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Kelas : B

Prodi : Pendidikan Fisika

Tugas Mekanika

2.1. a). $f_x = m \ddot{x} = f_0 + ct$

$$m dv = f_0 + ct$$

$$m dv = (f_0 + ct) dt$$

$$m \int_{v_0}^v dv = \int_0^t (f_0 + ct) dt$$

$$m(v - v_0) = f_0(t - t_0) + \frac{c}{2}(t^2 - t_0^2)$$

Karena $v_0 = 0$ dan $t = 0$, maka :

$$mv = f_0 t + \frac{ct^2}{2}$$

$$v(t) = \frac{1}{m} \left(f_0 t + \frac{ct^2}{2} \right) = \frac{dx}{dt}$$

$$\int_{x_0}^x dx = \int_{t_0}^t \frac{1}{m} \left(f_0 t + \frac{ct^2}{2} \right) dt$$

$$x - x_0 = \frac{1}{m} \left(\frac{f_0}{2} (t^2 - t_0^2) + \frac{c}{6} (t^3 - t_0^3) \right)$$

$$x = \frac{1}{m} \left(\frac{f_0 t^2}{2} + \frac{ct^3}{6} \right)$$

b). $f_x = m \frac{dv}{dt} = f_0 \sin ct$

$$\int_0^v dv = \frac{f_0}{m} \int_0^t \sin ct dt$$

$$vt = -\frac{f_0}{m} \cos ct$$

$$x(t) = \int_0^t v \, dt$$

$$x(t) = -\frac{f_0}{mc} \int_0^t \cos ct \, dt$$

$$x(t) = -\frac{f_0}{mc^2} \sin ct.$$

c). $f_x = f_0 e^{ct}.$

$$v(t) = \frac{f_0}{m} \int_0^t e^{ct} \, dt.$$

$$v(t) = \frac{f_0}{m} e^{ct}$$

$$x(t) = \frac{f_0}{c^2 m} e^{ct}$$

2.2). a). $f_x = f_0 + cx$

$$f(x) = mv \frac{dv}{dx} = f_0 + cx.$$

$$\int_0^v mv \, dv = \int_0^x (f_0 + cx) \, dx.$$

$$\frac{mv^2}{2} = f_0 x + \frac{c}{2} x^2$$

$$v = \sqrt{\frac{2}{m} \left(f_0 x + \frac{c}{2} x^2 \right)}$$

b). $f(x) = mv \frac{dv}{dx} = f_0 e^{-x}.$

$$= \frac{1}{2} mv^2 = -\frac{f_0}{c} e^{-cx}$$

$$v = \frac{2}{m} \left[-\frac{f_0}{c} e^{-cx} \right]^{1/2}$$

$$c). F(x) = mv \frac{dv}{dx} = F_0 \cos cx$$

$$= \frac{1}{2} mv^2 = \int_0^x F_0 \cos cx.$$

$$= \frac{F_0}{c} \sin cx.$$

$$v = \frac{2}{m} \left[\frac{F_0}{2} \sin cx \right]^{1/2}$$

$$23). a). Fx = -\frac{dv}{dx} = F_0 + cx.$$

$$u(x) = - \left[F_0 x + \frac{c}{2} x^2 \right] + c.$$

$$b). Fx = -\frac{dv}{dx} = F_0 e^{-cx}.$$

$$\int_{u(x_0)}^{u(x)} du = -F_0 \int_{x_0}^x e^{-cx} dx$$

$$c). Fx = -\frac{dv}{dx} = F_0 \cos cx.$$

$$\int_{u(x_0)}^{u(x)} dv = -F_0 \int_{x_0}^x \cos(x) dx.$$

$$u(x) - u(x_0) = -\frac{F_0}{c} [\sin x - \sin x_0]$$

$$2.4). V(x) = -\int F(x) \cdot dx.$$

$$a). V(x) = \int (-kx) dx.$$

$$V(x) = \frac{kx^2}{2}.$$

$$\text{Jadi energi potensialnya adalah } V(x) = \frac{kx^2}{2}$$

b). dan c).

$$F = T_0 = \frac{1}{2} k A^2.$$

$$E = T_x + V(x).$$

$$T(x) = E - V(x).$$

$$T(x) = \frac{1}{2} k A^2 - \frac{1}{2} k x^2.$$

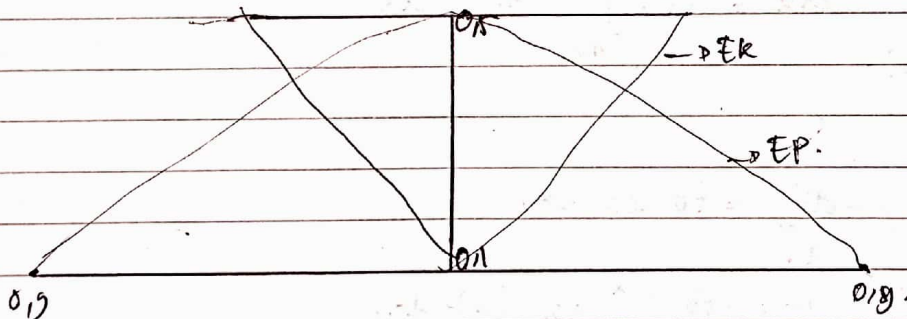
$$T(x) = \frac{k}{2} (A^2 - x^2).$$

d). $E = V(x).$

$$\frac{1}{2} k A^2 = \frac{1}{2} k x^2.$$

$$x = \pm A.$$

e).



Hasilnya: a). $V(x) = \frac{kx^2}{2}.$

b). $T(x) = \frac{k}{2} (A - x^2).$

c). $E = T_0 = \frac{1}{2} k A^2.$

$$2.8). \quad v = \frac{b}{x^3}.$$

$$F = m \frac{dv}{dt} = m \frac{dv}{dx} \frac{dx}{dt}$$

$$= mv \frac{dv}{dx}$$

$$\frac{dv}{dx} = -\frac{3b}{x^4}$$

$$F = m \left(\frac{b}{x^3} \right) \left(-\frac{3b}{x^4} \right) = -\frac{3mb^2}{x^7}.$$

$$2.11. \quad F(v) = -cv^{3/2}$$

$$= m \frac{dv}{dt} = m \cdot \frac{dv}{dx} \cdot \frac{dx}{dt}$$

$$= m \frac{dv}{dt}$$

$$-cv^{3/2} = m \frac{dv}{dx}$$

$$\int_0^x dx = \int_{v_0}^v \frac{-mv}{cv^{3/2}} dv$$

$$x = -\frac{m}{c} \int_{v_0}^v \frac{dv}{\sqrt{v}} = -\frac{m}{c} \int_{v_0}^v v^{-1/2} dv$$

$$= -\frac{m}{c} \frac{v^{1/2}}{1/2} \Big|_{v_0}^v$$

$$= \frac{2m}{c} (\sqrt{v_0} - \sqrt{v}).$$

Partikel berhenti, maka $v=0$, jadi $x_{\max} = \frac{2m\sqrt{v_0}}{c}$

$$2.12. \quad m \cdot a_x = \sum f_x.$$

$$m \cdot a_x = -m \cdot g - c_2 v^2$$

$$a_x = \frac{dv}{dt} = \frac{dv \cdot dx}{dx \cdot dt} = \frac{dv}{dx} \cdot v$$

$$m \cdot \frac{dv}{dx} \cdot v = -m \cdot g - c_2 v^2$$

$$v \frac{dv}{dx} = -g - \frac{c_2}{m} v^2.$$

$$k = \frac{c_2}{m}.$$

$$\int_{v_0}^v \frac{v \, dv}{-g - kv^2} = \int_0^x dx.$$

$$y = -g - kv^2$$

$$dy = -2kv \, dv.$$

$$v \, dv = -\frac{1}{2k} dy.$$

$$\int_{v_0}^v \frac{-1 \, dy}{2ky} = \int_0^x dx$$

$$\frac{-1}{2k} \ln(y) \Big|_{v_0}^v = x \Big|_0^x$$

$$\frac{-1}{2k} \ln(-g - kv^2) \Big|_{v_0}^v = x$$

$$\frac{-1}{2k} \ln \left(\frac{-g - kv^2}{-g - kv_0^2} \right) = x.$$

$$\frac{-g - kv^2}{-g - kv_0^2} = e^{-2kx}.$$

$$-g - kv^2 = (-g - kv_0^2) e^{-2kx}.$$

$$kv^2 = (g + kv_0^2) e^{-2kx} - \frac{g}{k}.$$

$$A = \frac{g}{k} + v_0^2$$

$$v^2 = A e^{-2kx} - \frac{g}{k}.$$

$$m \cdot a_x = \Sigma F_x.$$

$$m \cdot a_x = -mg + c^2 v^2$$

$$a_x = \frac{dv}{dt} = \frac{dv}{dx} \frac{dx}{dt} = \frac{dv}{dx} \cdot v.$$

$$mv \cdot \frac{dv}{dx} = -mg + c^2 v^2.$$

$$c \cdot \frac{dv}{dx} = -g + \frac{c^2}{m} v^2.$$

$$k = \frac{c^2}{m}.$$

$$v \cdot \frac{dv}{dx} = -g + kv^2.$$

$$\int_{v_0}^v \frac{v \cdot dv}{-g + kv^2} = \int_{x_0}^x dx.$$

$$y = -g + kv^2$$

$$dy = 2kv \, dv.$$

$$v \, dv = \frac{1}{2k} dy$$

$$\int_{v_0}^v \frac{1}{2k} \frac{dy}{y} = \int_{x_0}^x dx.$$

$$\frac{1}{2k} \ln y \Big|_{v_0}^v = x \Big|_{x_0}^x.$$

$$\frac{1}{2k} \ln(-g + kv^2) \Big|_{v_0}^v = x - x_0.$$

$$\frac{1}{2k} \ln \left(\frac{-g + kv^2}{-g} \right) = x - x_0$$

$$\frac{-g + kv^2}{-g} = e^{2k(x-x_0)}.$$

$$-g + kv^2 = -g e^{2k(x-x_0)}.$$

$$kv^2 = -g e^{2k(x-x_0)} + g.$$

$$v^2 = \frac{-g}{k} e^{2k(x-x_0)} + \frac{g}{k}.$$

$$B = \frac{g}{k} e^{2kx_0}.$$

$$V^2 = \frac{g}{k} - B e^{2kx} \quad \text{dengan} \quad B = \frac{g}{k} e^{2kx_0}$$

$$2.13. \quad V^2 = \left(\frac{g}{k} + V_0^2 \right) e^{-2kx} - \frac{g}{k} \quad \text{keatas.}$$

$$V^2 = -\frac{g}{k} e^{-2kx_0} e^{2kx} + \frac{g}{k} \quad \text{ke bawah.}$$

dengan $V_0 = 0$ Pada Gerak ke atas.

$$0 = \left(\frac{g}{k} + V_0^2 \right) e^{-2kx} - \frac{g}{k}$$

$$e^{-2kh} = \frac{\frac{g}{k}}{\frac{g}{k} + V_0^2}$$

h adalah posisi awal untuk gerakan ke bawah dan $(t) \quad a=0$.

$$V^2 = -\frac{g}{k} e^{-2kh} e^{2kx} + \frac{g}{k} \quad \text{Substitusikan nilai } x=0.$$

$$V^2 = -\frac{g}{k} \cdot \frac{\frac{g}{k}}{\frac{g}{k} + V_0^2} + \frac{g}{k}$$

$$Vt^2 = \frac{g}{k}$$

$$V^2 = -Vt^2 \frac{Vt^2 + V_0^2}{Vt^2 + V_0^2} + Vt^2$$

$$V^2 = Vt^2 \left(\frac{1 - Vt^2}{Vt^2 + V_0^2} \right)$$

$$V^2 = Vt^2 \left(\frac{Vt^2 + V_0^2 - Vt^2}{Vt^2 + V_0^2} \right)$$

$$V^2 = \frac{Vt^2 + V_0^2}{Vt^2 + V_0^2}$$

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$$2.14. \quad m \cdot dx = \Sigma Fx.$$

$$m \cdot dx = -kx^{-2}$$

$$dx = \frac{dv}{dt} = -kx^{-2}$$

$$v \cdot \frac{dv}{dx} = -\frac{k}{m} x^{-2}$$

$$\int_0^v v \cdot dv = -\frac{k}{m} \int_0^x x^{-2} dx$$

$$\frac{v \cdot v}{2} \Big|_0^v = \frac{k}{m} (-1) x^{-1} \Big|_0^x$$

$$\frac{v^2}{2} = \frac{k}{m} (x^{-1} - b^{-1})$$

$$v^2 = \frac{2k}{m} \left(\frac{b-x}{bx} \right)$$

$$v = \frac{dx}{dt}$$

$$\sqrt{\frac{2k(b-x)}{m}} = \frac{dx}{dt}$$

$$\int_b^0 \frac{dx}{\sqrt{\frac{2k}{m} \left(\frac{b-x}{bx} \right)}} = \int_0^t dt$$

$$\int_b^0 \frac{dx}{\sqrt{\frac{2k}{m} \left(\frac{b-x}{bx} \right)}} = \sqrt{\frac{mb}{2k}} \int_b^0 \sqrt{\frac{x}{b-x}} dx$$

$$u = \frac{\sqrt{b-x}}{\sqrt{x}}$$

$$du = \frac{1}{2\sqrt{b-x}} \cdot (-1) \cdot \sqrt{x} \cdot dx \cdot \frac{1}{2\sqrt{x}}$$

$$dx = \frac{du}{\frac{1}{2\sqrt{x}\sqrt{b-x}} - \frac{v\sqrt{x}}{2x^{3/2}}}$$

$$= \frac{du}{\frac{1}{2} - \frac{v}{2}}$$

$$= -\frac{du}{1+u^2} \cdot \frac{1}{2xv}$$

$$= -\frac{2xv \cdot dv}{v^2+1}$$

$$dx = -\frac{2bv \cdot dv}{(v^2+1)^2}$$

$$\sqrt{\frac{mb}{2k}} \int_b^0 \frac{1}{\sqrt{b-x}} dx = \sqrt{\frac{mb}{2k}} \int_b^0 \frac{1}{v} \cdot \frac{(-1)^2 \cdot 2bv \cdot dv}{(v^2+1)^2}$$

$$= \sqrt{\frac{mb}{2k}} \int_b^0 \frac{2b \cdot dv}{(v^2+1)^2}$$

$$\int \frac{du}{(u^2+1)^2} = \frac{u}{2(u^2+1)} \Big|_b^0 + \frac{1}{2} \int_b^0 \frac{dv}{v^2+1}$$

$$\int_b^0 \frac{du}{(v^2+1)^2} = \frac{u}{2(v^2+1)} \Big|_b^0 + \frac{1}{2} \arctan v \Big|_b^0$$

$$-\sqrt{\frac{mb}{2k}} \int_b^0 \frac{2b \cdot dv}{(v^2+1)^2} = -2b \sqrt{\frac{mb}{2k}} \left(\frac{v}{2(v^2+1)} \Big|_b^0 + \frac{1}{2} \arctan v \Big|_b^0 \right)$$

$$= -2b \sqrt{\frac{mb}{2k}} \left(\frac{v}{2(v^2+1)} \Big|_0^{-\infty} + \frac{1}{2} \arctan v \Big|_0^{-\infty} \right)$$

$$= -2b \sqrt{\frac{mb}{2k}} \left(0 - 0 + \frac{1}{2} \left(\frac{\pi}{2} - 0 \right) \right)$$

$$= -\pi \sqrt{\frac{mb^3}{8k}}$$

$$\pi \sqrt{\frac{mb^3}{8k}} = \int_0^t dt$$

$$t \propto \sqrt{\frac{mb^3}{8k}}$$

$$2.15. \quad m \cdot a_x = \Sigma F_x.$$

$$m \cdot a = mg - C_1 V - C_2 V^2$$

$$m \cdot a = 0.$$

$$mg - C_1 V - C_2 V^2 = 0.$$

$$C_2 V^2 + C_1 V - mg = 0.$$

$$V_{1/2} = \frac{-C_1 \pm \sqrt{C_1^2 + 4C_2 mg}}{2C_2}.$$

Kita (+).

$$V_1 = \frac{-C_1 + \sqrt{C_1^2 + 4C_2 mg}}{2C_2}.$$

$$V_1 = V_t = \frac{-C_1}{2C_2} + \sqrt{\left(\frac{C_1}{2C_2}\right)^2 + \frac{mg}{C_2}}.$$

$$V_t = \frac{-C_1}{2C_2} + \sqrt{\left(\frac{C_1}{2C_2}\right)^2 + \frac{mg}{C_2}}.$$