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$$\Rightarrow \begin{array}{c} \uparrow \\ \circ \\ \downarrow \\ \vec{w} \end{array} \quad \begin{array}{c} \downarrow \\ \circ \\ \downarrow \\ \vec{g} \end{array} \quad \begin{array}{c} \downarrow \\ \circ \\ \downarrow \\ \vec{f}_0 \end{array}$$

- Berdasarkan turuk Newton

$$\Sigma \vec{f} = m \vec{a}$$

$$\vec{w} + \vec{f} = -m \vec{a}$$

$$(mg + bv) \hat{y} = -m \vec{a} \hat{y}$$

$$(g + bv) = -a \left(\times \frac{1}{m} \right)$$

$$g + \frac{bv}{m} = -a$$

- Substitusi mulai a

$$g + \frac{b}{m} v = -\frac{dv}{dt}$$

$$g + \frac{b}{m} v = -\frac{dv}{dt}$$

$$\frac{-dv}{g + \frac{b}{m} v} = dt$$

$$\int_0^{v(x)} \frac{dv}{g + \frac{b}{m} v} = \int_0^t dt$$

$$\text{misal : } g + \frac{b}{m} \cdot v = u$$

$$= \frac{b}{m} dv = du$$

$$dv = \frac{m}{b} du$$

$$\text{maka } \int_0^{v(x)} \frac{1}{v} dv = \int_0^t dt$$

$$= \int_0^{v(x)} \frac{1}{v} \left(\frac{m}{b} du \right) = \int_0^t dt - \frac{m}{b} \ln |v| = t - \frac{m}{b} \ln \left| g + \frac{b}{m} v \right| \Big|_v^{v(t)} = t$$

$$= \frac{m}{b} \left(\ln \left| g + \frac{b}{m} (v(t)) \right| - \ln \left| g + \frac{b}{m} (v^2) \right| \right)$$

$$\text{Karena : } \ln a - \ln b = \ln \frac{a}{b}$$

Maka :

$$\ln \left| g + \frac{b}{m} (v(t)) \right| = -\frac{bt}{m}$$

$$\text{Contoh : } \left(\ln \left| g + \frac{b}{m} (v(t)) \right| \right) = e^{-\frac{bt}{m}}$$

$$g + \frac{b}{m} v(t) = e^{-\frac{bt}{m}}$$

$$g + \frac{b}{m} v_0$$

$$g + \frac{b}{m} v(t) = \left(g + \frac{b}{m} v_0 \right) e^{-\frac{bt}{m}}$$

$$\frac{b}{m} v(t) = \left(g + \frac{b}{m} v_0 \right) e^{-\frac{bt}{m}} - g \left(x - \frac{m}{b} \right)$$

$$v(t) = \frac{m}{b} \left(g + \frac{b}{m} v_0 \right) e^{-\frac{bt}{m}} - \frac{m}{b}$$

$$v(t)^2 = \left(\frac{mg}{b} + v_0 \right) e^{-\frac{bt}{m}} - \frac{mg}{b}$$

Karena, $f=w$

$$bv = mg$$

$$v = \frac{mg}{b}, \text{ maka}$$

$$v(t) = (v_r + v_0) e^{-\frac{bt}{m}} - v_r$$

Untuk $a(t)$

$$a(t) = \frac{dv(t)}{dt}$$

$$\begin{aligned}
 a(t) &= (vt + v_0) \left(-\frac{b}{m}\right) e^{-\frac{bt}{m}} \\
 &= -\frac{b}{m} (vt + v_0) e^{-\frac{bt}{m}} \\
 &= \left(-\frac{b}{m} \cdot \frac{mg}{b} - \frac{b}{m} v_0\right) e^{-\frac{bt}{m}} \\
 a(t) &= \left(-g - \frac{b}{m} v_0\right) e^{-\frac{bt}{m}}
 \end{aligned}$$

Untuk $y(t)$

$$dy(t) = v(t) \cdot dt$$

$$\int_0^{y(t)} dy(t) = \int_0^t v(t) dt$$

$$y(t) = \int_0^t (vt + v_0) e^{-\frac{bt}{m} - VT} dt$$

$$y(t) = \left((vt + v_0) \left(-\frac{m}{b}\right) e^{-\frac{bt}{m} - VT} \right)_0^t$$

$$y(t) = \left((vt + v_0) \left(-\frac{m}{b}\right) e^{-\frac{bt}{m} - VT} \right) - \left((vt + v_0) \left(-\frac{m}{b}\right) \right)$$

$$y(t) = -\frac{m}{b} (vt + v_0) (e^{-\frac{bt}{m}} - 1) - VT \cdot t$$

- Aproksimasi

$$e^{-\frac{bt}{m}} = 1 - \frac{bt}{m} + \frac{1}{2} \left(\frac{bt}{m}\right)^2 + \dots$$

$$y(t) = -VT \cdot \frac{m}{b} (vt + v_0) (1 - e^{-\frac{bt}{m}})$$

$$= -VT \cdot t + \frac{m}{b} (vt + v_0) (1 - e^{-\frac{bt}{m}})$$

$$= -VT \cdot t + \frac{m}{b} (vt + v_0) \left(1 + \frac{bt}{m} - \frac{1}{2} \left(\frac{bt}{m}\right)^2\right)$$

$$= v_0 t - \frac{1}{2} g t^2 - \frac{1}{2} \frac{b}{m} v_0 t^2$$

$$y(t) = v_0 t - \frac{1}{2} g t^2 - \frac{1}{2} \cdot \frac{b}{m} v_0 t^2$$

Untuk $b=0$ maka,

$$y(t) = v_0 t - \frac{1}{2} g t^2$$

$$v(t) = (vt + v_0) e^{-\frac{bt}{m}} - VT$$

$$= -VT + (vt + v_0) (1 - \frac{bt}{m})$$

$$= -VT + vt - \frac{b}{m} vt + \dots + v_0 - \frac{b}{m} v_0 t$$

$$= v_0 - \frac{b}{m} \left(\frac{mg}{b}\right) + \frac{b}{m} v_0 t$$

$$v(t) = v_0 - g t - \frac{b}{m} v_0 t$$

Untuk $b=0$ maka

$$v(t) = v_0 - g t$$

$$a(t) = \left(-g - \frac{b}{m} v_0\right) e^{-\frac{bt}{m}}$$

$$= \left(-g - \frac{b}{m} v_0\right) (1 - \frac{bt}{m})$$

$$= -g + g \frac{bt}{m} - \frac{b}{m} v_0 + \frac{b^2}{m^2} v_0 t$$

$$\begin{aligned}
 &\rightarrow a(t) = -g - \frac{b}{m} v_0 + \left(\frac{b^2}{m^2} v_0 + \frac{gb}{m}\right) t \\
 &\text{Maka } b=0 \\
 &\underline{a(t) = -g}
 \end{aligned}$$