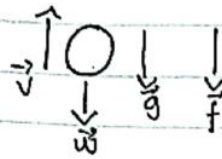


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Berdasarkan Hk II Newton

$$\sum \vec{F} = m\vec{a}$$

$$\vec{w} + \vec{F} = -m\vec{a}$$

$$(mg + bv)\hat{y} = -m\hat{a}y$$

$$(mg + bv) = -m\hat{a} \quad \left(\times \frac{1}{m}\right)$$

$$g + \frac{b}{m}v = -a$$

Substitusikan nilai a

$$g + \frac{b}{m}v = -\frac{d^2 y(t)}{dt^2}$$

$$g + \frac{b}{m}v = \frac{-dv}{dt}$$

$$\frac{-dv}{g + \frac{b}{m}v} = dt$$

$$= \int_{v_0}^{v(t)} \frac{dv}{g + \frac{b}{m}v} = \int_0^t dt$$

$$\text{misal } g + \frac{b}{m}v = u$$

$$= \frac{b}{m} dv = du$$

$$du = \frac{m}{b} du$$

maka

$$\int_{v_0}^{v(t)} \frac{1}{u} dv = \int_0^t dt$$

$$= \int_{v_0}^{v(t)} \frac{1}{u} \left(\frac{m}{b} du \right) = \int_0^t dt$$

$$-\frac{m}{b} \ln |u| = t$$

$$-\frac{m}{b} \ln \left| g + \frac{b}{m}v \right|_{v_0}^{v(t)} = t$$

$$-\frac{m}{b} \left(\ln \left| g + \frac{b}{m}v(t) \right| - \ln \left| g + \frac{b}{m}v_0 \right| \right)$$

karena : $\ln a - \ln b = \ln \frac{a}{b}$, maka

$$\ln \left| \frac{g + \frac{b}{m}v(t)}{g + \frac{b}{m}v_0} \right| = -\frac{bt}{m}$$

$$\exp \left(\ln \left| \frac{g + \frac{b}{m}v(t)}{g + \frac{b}{m}v_0} \right| \right) = e^{-\frac{bt}{m}}$$

$$g + \frac{b}{m}v(t) = e^{-\frac{bt}{m}} \left(g + \frac{b}{m}v_0 \right)$$

$$g + \frac{b}{m}v(t) = \left(g + \frac{b}{m}v_0 \right) e^{-\frac{bt}{m}}$$

$$\frac{b}{m}v(t) = \left(g + \frac{b}{m}v_0 \right) e^{-\frac{bt}{m}} - g \left(\times \frac{m}{b} \right)$$

$$v(t) = \frac{m}{b} \left(g + \frac{b}{m}v_0 \right) e^{-\frac{bt}{m}} - \frac{mg}{b}$$

$$v(t) = \left(\frac{mg}{b} + v_0 \right) e^{-\frac{bt}{m}} - \frac{mg}{b}$$

karena : $f = w$

$$bv = mg$$

$$v_T = \frac{mg}{b} \quad \text{maka :}$$

$$v(t) = (v_T + v_0) e^{-\frac{bt}{m}} - v_T$$

untuk $a(t)$

$$a(t) = \frac{dv(t)}{dt}$$

$$\begin{aligned} a(t) &= (v_T + v_0) \left(-\frac{b}{m}\right) e^{-\frac{bt}{m}} \\ &= -\frac{b}{m} (v_T + v_0) e^{-\frac{bt}{m}} \\ &= \left(-\frac{b}{m} \cdot \frac{mg}{b} - \frac{b}{m} v_0\right) e^{-\frac{bt}{m}} \end{aligned}$$

$$a(t) = \left(-g - \frac{b}{m} v_0\right) e^{-\frac{bt}{m}}$$

untuk $y(t)$

$$v(t) = \frac{dy(t)}{dt}$$

$$dy(t) = v(t) dt$$

$$\int_0^{y(t)} dy(t) = \int_0^t v(t) dt$$

$$y(t) = \int_0^t (v_T + v_0) e^{-\frac{bt}{m}} - v_T dt$$

$$y(t) = \left[(v_T + v_0) \left(-\frac{m}{b}\right) e^{-\frac{bt}{m}} - v_T t \right]_0^t$$

$$y(t) = \left[(v_T + v_0) \left(-\frac{m}{b}\right) e^{-\frac{bt}{m}} - v_T t \right] - \left[(v_T + v_0) \left(-\frac{m}{b}\right) \right]$$

$$y(t) = -\frac{m}{b} (v_T + v_0) (e^{-\frac{bt}{m}} - 1) - v_T t$$

$$y(t) = -\frac{m}{b} (v_T + v_0) (1 - e^{-\frac{bt}{m}}) - v_T t$$

Aprokham:

$$e^x = 1 + \frac{x}{1!} + \frac{x^2}{2!} + \frac{x^3}{3!} + \dots$$

$$e^{-\frac{bt}{m}} = 1 - \frac{bt}{m} + \frac{1}{2} \left(\frac{bt}{m}\right)^2 + \dots$$

$$y(t) = -v_T t + \frac{m}{b} (v_T + v_0) (1 - e^{-\frac{bt}{m}})$$

$$= -v_T t + \frac{m}{b} (v_T + v_0) \left(1 - 1 + \frac{bt}{m} - \frac{1}{2} \left(\frac{bt}{m}\right)^2\right)$$

$$= v_0 t = \frac{1}{2} g t^2 - \frac{1}{2} \frac{b}{m} v_0 t^2$$

$$y(t) = v_0 t - \frac{1}{2} g t^2 - \frac{1}{2} \frac{b}{m} v_0 t^2$$

untuk $b=0$ maka,
 $y(t) = v_0 t - \frac{1}{2} g t^2$

$V(t)$
 $v(t) = (v_T + v_0) e^{-bt/m} - v_T$
 $= -v_T + (v_T + v_0) (1 - bt/m)$
 $= -\cancel{v_T} + \cancel{v_T} - \frac{b}{m} v_T t + v_0 - \frac{b}{m} v_0 t$
 $= v_0 - \frac{b}{m} \left(\frac{mg}{b} \right) t - \frac{b}{m} v_0 t$

$V(t) = v_0 - g t - \frac{b}{m} v_0 t$

untuk $b=0$ maka,

$V(t) = v_0 - g t$

$a(t) = (-g - b/m v_0) e^{-bt/m}$
 $= (-g - b/m v_0) (1 - bt/m)$
 $= -g + g \frac{bt}{m} - \frac{b}{m} v_0 + \frac{b^2}{m^2} v_0 t$

$a(t) = -g - \frac{b}{m} v_0 + \left(\frac{b^2}{m^2} v_0 + \frac{gb}{m} \right) t$

maka $b=0$

$a(t) = -g$