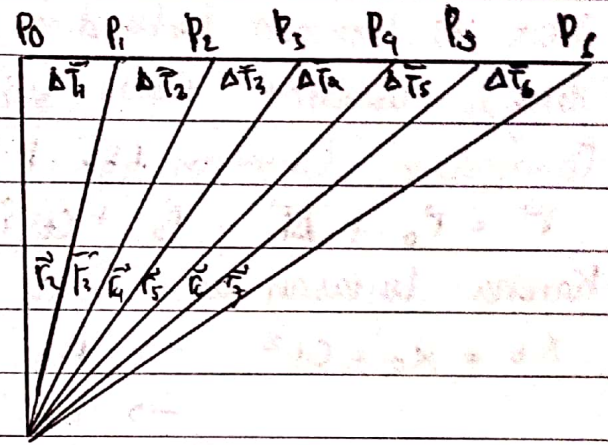
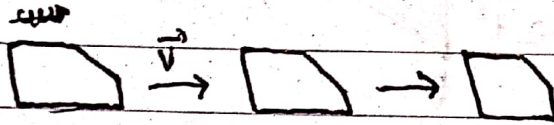


Nama : Insani Triana

NPM : 201302002

Kelas : B

1. Gerak Lurus Beraturan



$P_0, P_1, P_2, P_3, P_4, P_5$, dan P_6 merupakan posisi benda saat $t_0, t_1, t_2, t_3, t_4, t_5, t_6$ dg vektor posisi terhadap θ yaitu $\vec{r}_1, \vec{r}_2, \vec{r}_3, \dots$ dan perpindahan $\Delta r_1, \Delta r_2, \Delta r_3, \dots, \Delta r_6$

Δr_1 ditempuh dalam waktu $\Delta t_1 = t_1 - t_0$
 Δr_2 ditempuh dalam waktu $\Delta t_2 = t_2 - t_1$, dst

Karena benda bergerak lurus beraturan, maka :

$$\Delta r_1 = \Delta r_2 = \Delta r_3 = \dots = \Delta r \quad \text{konstan}$$

$$\Delta t_1 = \Delta t_2 = \Delta t_3 = \dots = \Delta t$$

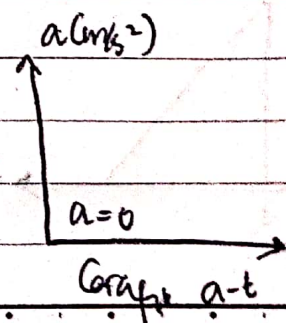
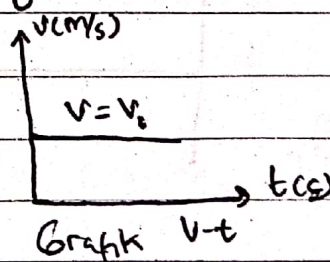
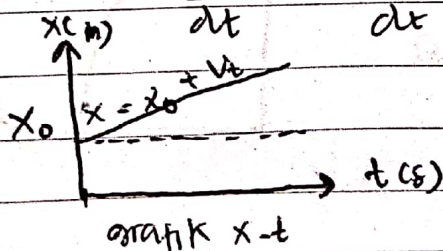
*) Persamaan lintasan di titik $P \rightarrow \vec{r} = \vec{r}_0 + \Delta \vec{r} = \vec{r}_0 + \Delta r \hat{e}_r$
 $\hat{e}_r$ = vektor satuan perpindahan $\Delta \vec{r}$
 Δr = tetap dalam selang waktu Δt yg sama

*) Kecepatan gerak dalam selang $\Delta t \rightarrow v = \frac{\Delta r}{\Delta t} = \text{konstan}, \Delta r = v \cdot \Delta t$
sehingga vektor posisi menjadi $\vec{r} = \vec{r}_0 + vt \hat{e}_r$

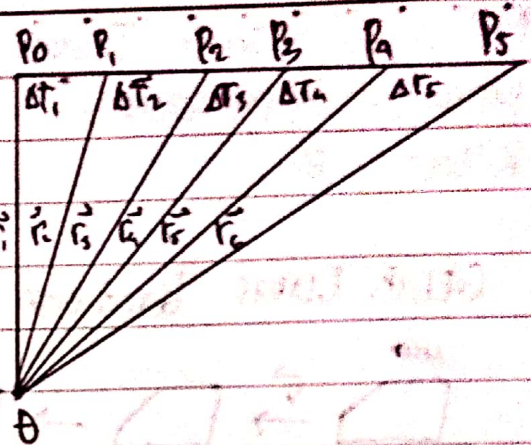
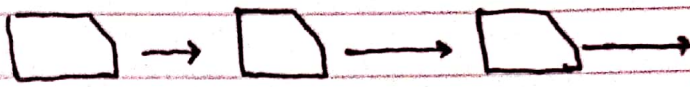
$$x(t) = v_x \cdot t \quad \text{atau} \quad y(t) = v_y \cdot t$$

$$v(t) = \frac{dx}{dt} = v_x = C = \text{konstan}$$

$$a(t) = \frac{dv}{dt} = \frac{d(C)}{dt} = 0$$



2. Gerak Lurus Berubah Beraturan



Jarak yg ditempuh berbanding lurus dengan kuadrat waktu, maka: $x = c \cdot t^2$

Persamaan lintasan titik P

$$\vec{r} = \vec{r}_0 + \Delta \vec{r} = \vec{r}_0 + ct^2 \hat{i}$$

Karena lintasan lurus, maka ditulis tanpa tanda vektor

$$x_t = x_0 + ct^2 \rightarrow \text{Pers. kecepatan benda } v_t = \frac{dx}{dt} = 2ct$$

$$\rightarrow \text{Pers. percepatan benda } a_t = \frac{dv_t}{dt} = 2c$$

Tetapi, jika benda bergerak dg kecepatan awal v_0 ,

persamaan menjadi :

$$x = x_0 + v_0 t + \frac{1}{2} a t^2$$

$$s = s_0 + v_0 t + \frac{1}{2} a t^2$$

$$v_x = v_0 + at$$

$$\text{Atau } v = v_0 + at$$

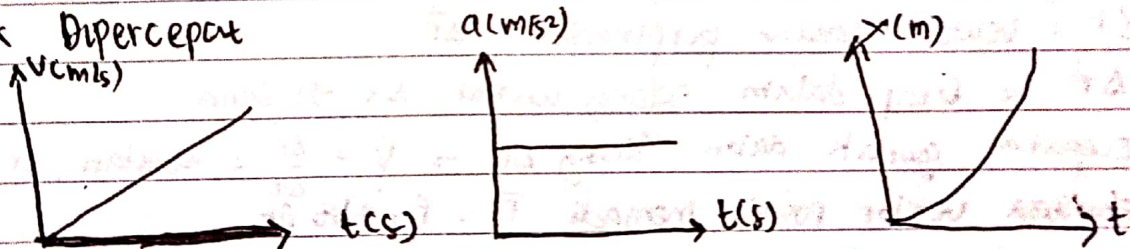
$$v_x^2 = v_0^2 + 2a(x - x_0)$$

$$v_t^2 = v_0^2 + 2a(s - s_0)$$

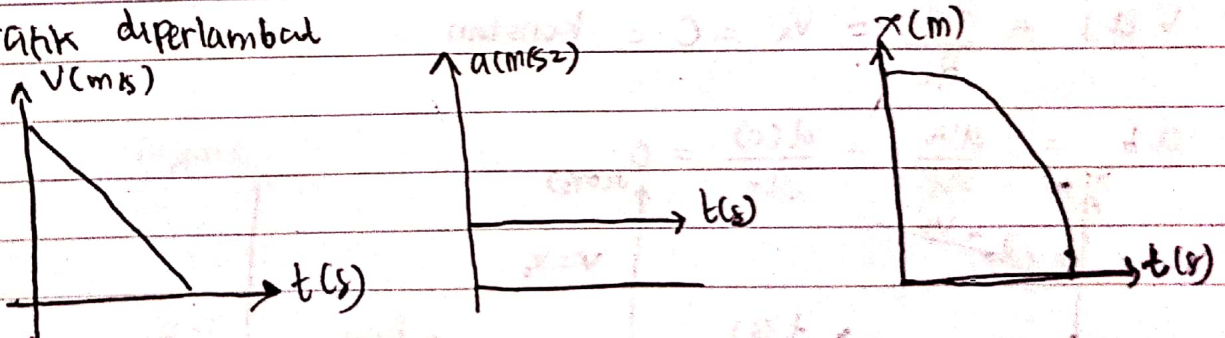
$$v_{\text{avg}} = \frac{v_0 + v_x}{2}$$

$$v_{\text{avg}} = \frac{v_0 + v}{2}$$

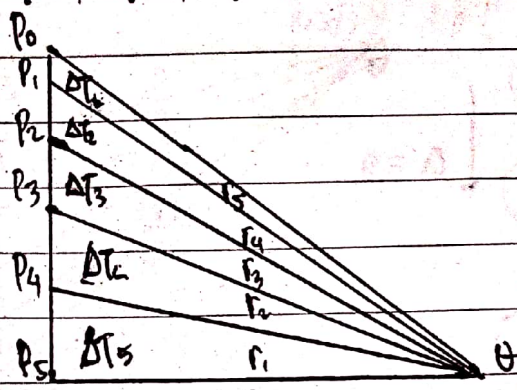
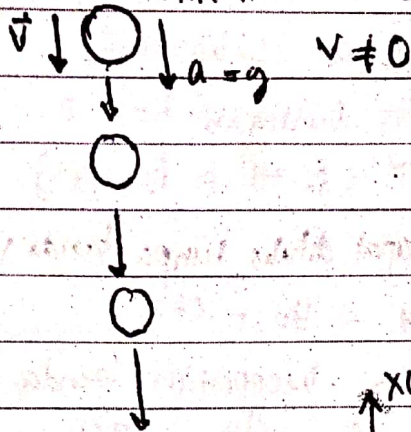
Gratik Dipercepat



Gratik diperlambat



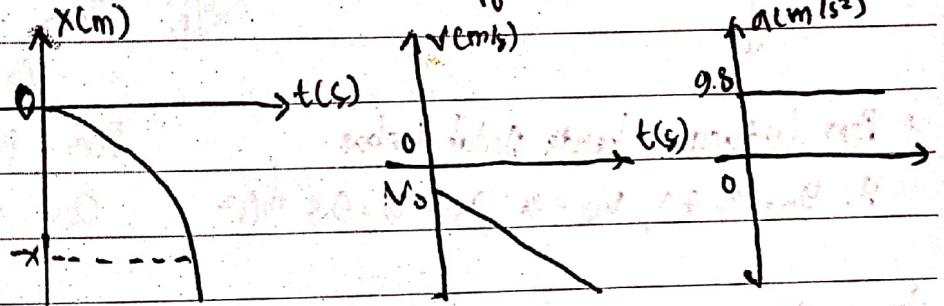
3. Gerak Vertikal ke Bawah



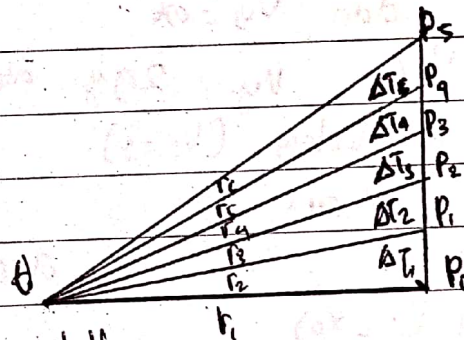
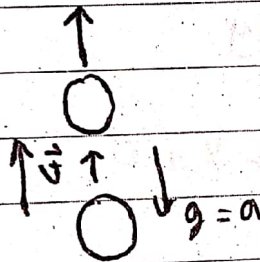
$$v_t = v_0 + gt$$

$$v_t^2 = v_0^2 + 2gh$$

$$h = v_0 t + \frac{1}{2} g t^2$$



4) Gerak Vertikal ke Atas



Ketika bergerak dg kecepatan awal v_0 ,

Pers. lintasannya : $x = x_0 + v_0 t + \frac{1}{2} a t^2$

$$v_x = v_0 + a$$

$$v_x^2 = v_0^2 + 2a(x - x_0)$$

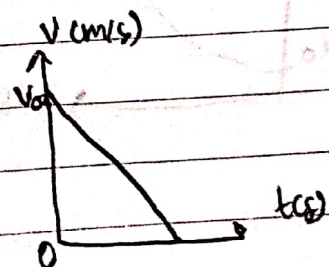
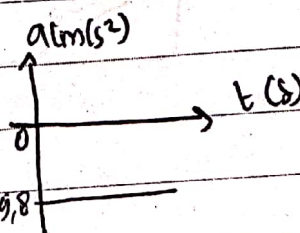
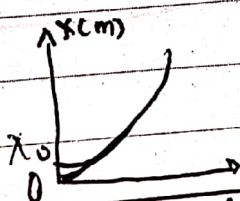
$$v_r = \frac{v_0 + v_x}{2}$$

Ketika benda bergerak tanpa kecepatan awal $v_0 = 0$, persamaannya :

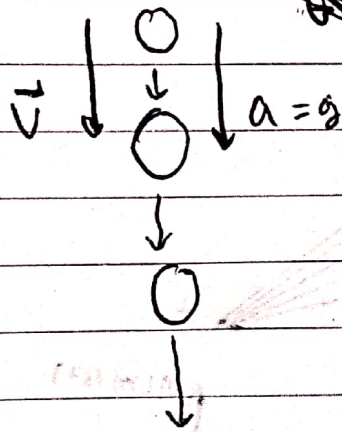
$$x = x_0 + \frac{1}{2} a t^2$$

$$v_x = at$$

$$v_x^2 = 2a(x - x_0)$$



5. Gerak Jatuh Bebas



P_0 Jarak berpindah lurus dg t^2

$$y = at^2 (c = \text{konstan})$$

P_1 Pers. lintasan titik P

$$\vec{r} = \vec{r}_0 + t\vec{v} = \vec{r}_0 + at^2\hat{j}$$

P_2 dapat ditulis tanpa tanda vektor

$$y = y_0 + ct^2$$

P_3 Pers. kecepatan benda

$$V_y = \frac{dy}{dt} = 2ct$$

P_4 Pers. Percepatan benda

$$a_y = \frac{dV_y}{dt} = 2c = g \rightarrow c = \frac{1}{2}g$$

→ Pers. lintasan benda jatuh bebas:

$$y = y_0 + \frac{1}{2}gt^2, V_y = gt, a_y = g = 9,8 \text{ m/s}^2$$

Jika ditinjau pada titik lintasan yg berhimpit dg P_0

$$y = \frac{1}{2}gt^2 \text{ dan } V_y = gt$$

$$\text{Jadi, } t = V_y/g, V_y = 2gy \text{ atau } V_y = \sqrt{2gy}$$

→ Benda jatuh bebas ($V_0 = 0$)

$$x = x_0 + \frac{1}{2}at^2$$

$$V_x = at$$

$$V_x^2 = 2a(x - x_0)$$

atau $V = at$

$$V^2 = 2a(s - s_0)$$

→ Benda jatuh bebas (V_0)

$$x = x_0 + V_0t + \frac{1}{2}at^2$$

$$V_x = V_0 + at$$

$$V_x^2 = V_0^2 + 2a(x - x_0)$$

$$V_r = \frac{V_0 + V_x}{2}$$

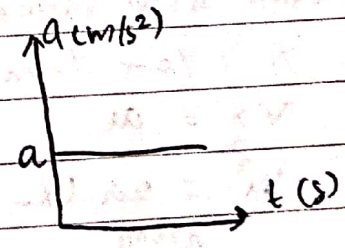
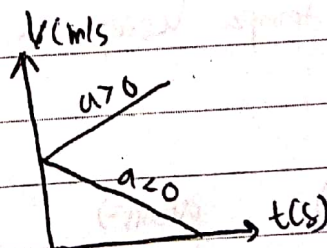
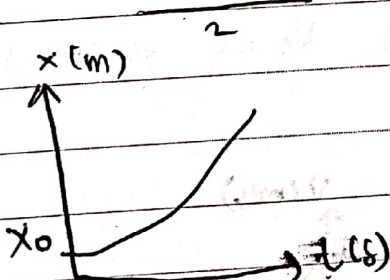
atau

$$s = s_0 + V_0t + \frac{1}{2}at^2$$

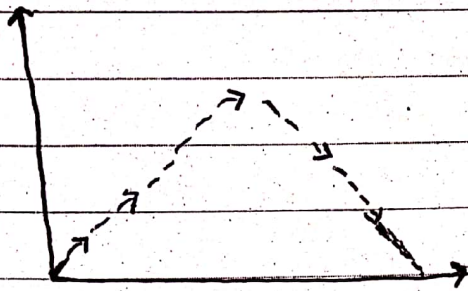
$$V = V_0 + at$$

$$V^2 = V_0^2 + 2a(s - s_0)$$

$$V_r = \frac{V_0 + V}{2}$$



6. Gerak Parabola



Keterangan :

V_0 = kecepatan awal (m/s)

V_x = kecepatan arah sumbu x (m/s)

V_y = kecepatan arah sumbu y (m/s)

x = posisi di sumbu x (m)

y = posisi di sumbu y (m)

θ = sudut elevasi

g = percepatan gravitasi (m/s^2)

•) Kecepatan di Sembarang Titik

$V = \sqrt{(V_x)^2 + (V_y)^2}$	Kecepatan (V_x, V_y)	
	sumbu x	sumbu y
Kondisi awal	$V_0 \cos \theta$	$V_0 \sin \theta$
saat t sekon	$V_0 \cos \theta$	$V_0 \sin \theta - gt$

•) Kecepatan saat t sekon

	Redudukan (x, y)		Waktu
	sumbu x	sumbu y	
Redudukan awal	0	0	0
saat t sekon	$x = V_0 \cos \theta \cdot t$	$y = V_0 \sin \theta \cdot t - \frac{1}{2}gt^2$	t
pd titik tertinggi	$X = \frac{V_0^2 \sin 2\theta}{g}$	$y_{\max} = \frac{V_0^2 \sin^2 \theta}{2g}$	$t = \frac{V_0 \sin \theta}{g}$
pd titik terjauh	$X_{\max} = \frac{V_0^2 \sin 2\theta}{g}$	0	$t = 2 \cdot \frac{V_0 \sin \theta}{g}$