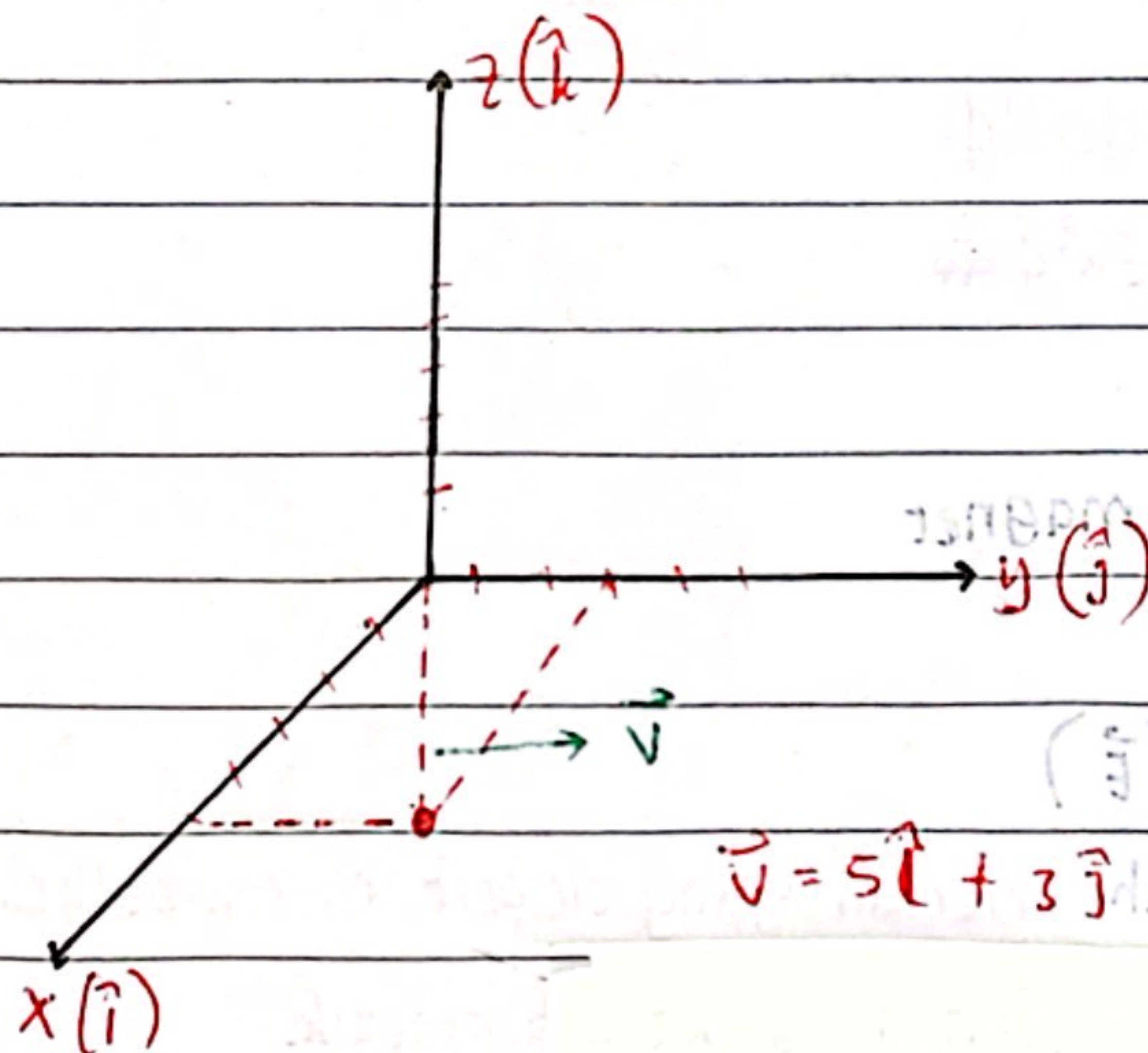
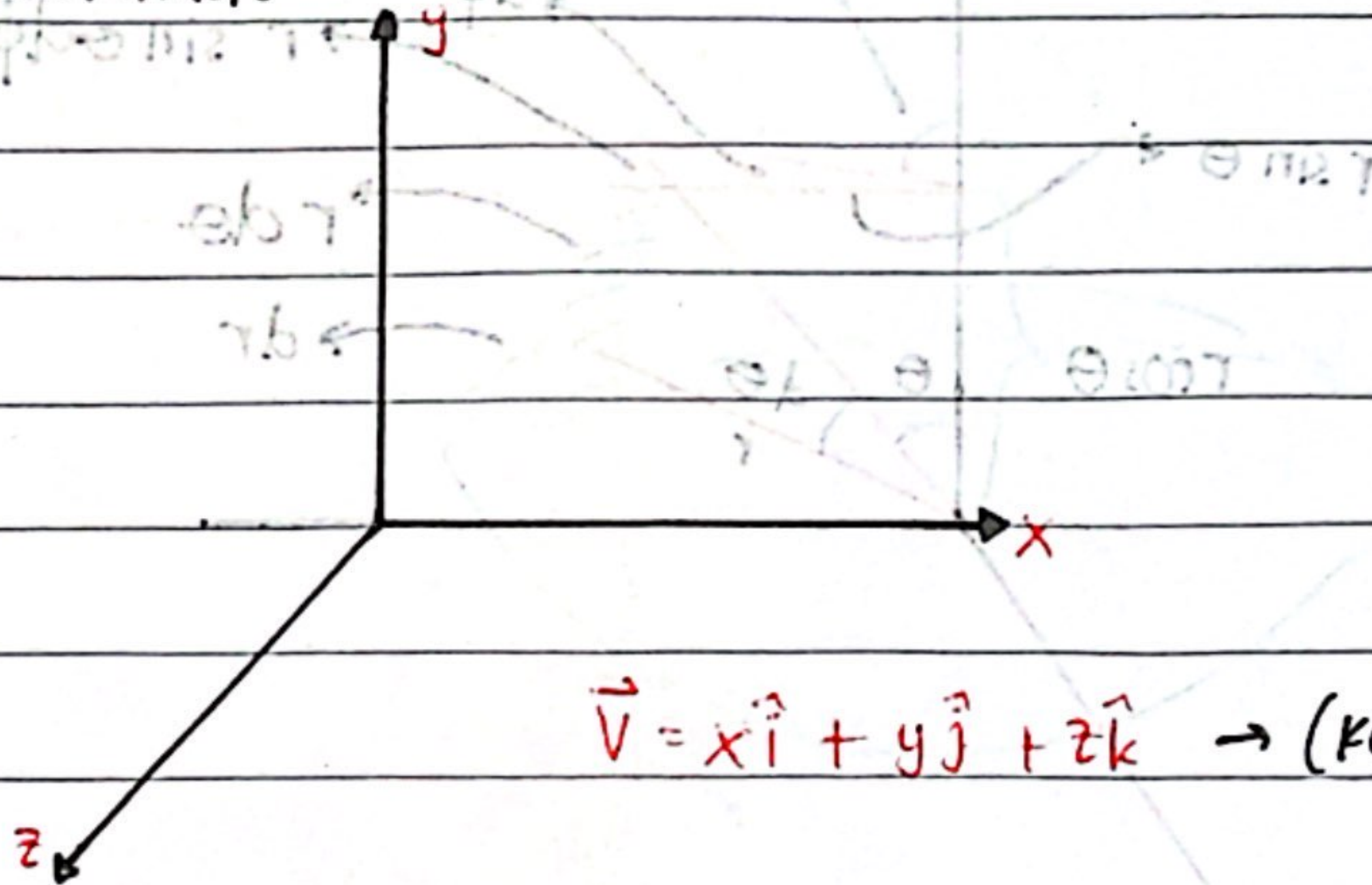


Pert. 1

## MEDAN ELEKTROMAGNETIK

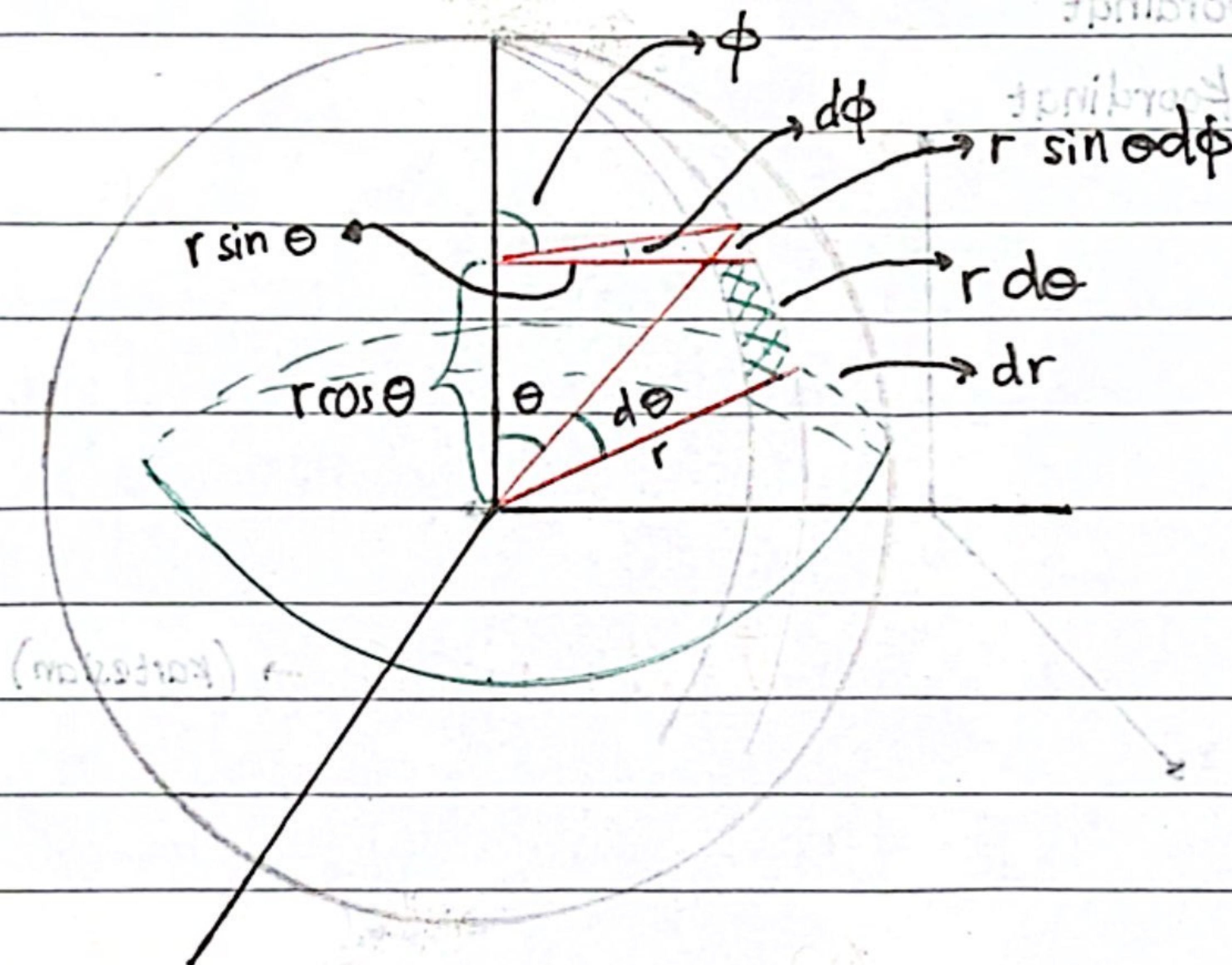
## 1. Sistem Koordinat

\* Sistem Koordinat





## \* Sistem Koordinat Bola



$$L = P \times \Delta = r^2 \sin \theta \, d\theta \, d\phi$$

$$V = P \times \Delta \times t = r^2 \sin \theta \, d\phi \, dr$$

## 2. Medan listrik dan magnet

### \* Medan listrik ( $\vec{E}$ )

Medan listrik adalah medan yang dapat menimbulkan gelombang listrik / elektromagnetik.

### \* Elektromagnetik

Elektromagnetik adalah gelombang yang ditimbulkan oleh arus listrik dan muatan.



\* Muatan  $\rightarrow$  Sifat dari sebuah benda.

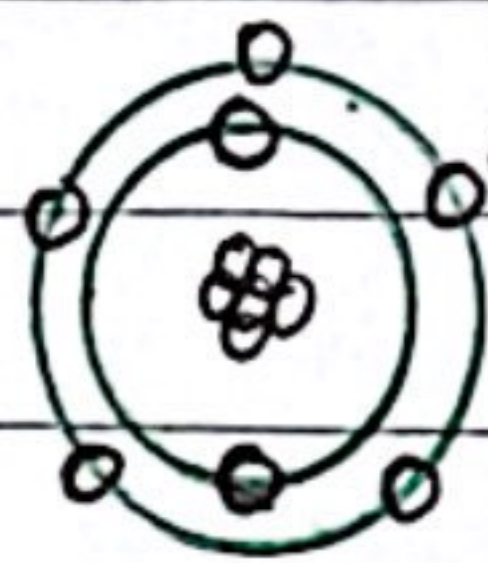
• Medan gravitasi:

$$\vec{g} = G \frac{M}{r^2} \hat{r}_0$$

• Elektromagnetik:

$$\vec{E} = k \frac{q}{r^2} \hat{r}_0$$

Muatan



Muatan  $\odot \rightarrow$  (bertambah) dinamakan muatan negatif.

$$q = 2C \rightarrow \text{Coulomb}$$

Note:

$$\vec{E} = k \frac{q}{r^2} \hat{r}_0$$

$$\vec{E} = k \left[ \frac{q_1}{r_1^2} \hat{r}_0 + \frac{q_2}{r_2^2} \hat{r}_0 + \dots \right]$$

• Medan Magnet

Ditimbulkan oleh arus listrik.



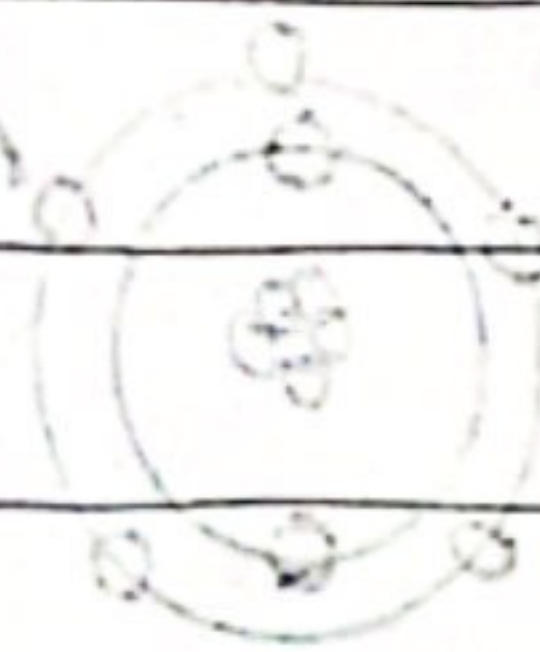
arus yang dilalui

$$\vec{B} = \frac{\mu_0 I}{2\pi r} \hat{\phi} \longrightarrow \vec{B} = \frac{q\vec{v} \times \hat{r}}{r^2}$$

$$F = BIl \sin \theta \Rightarrow \text{sudut } 90^\circ$$

$$F = q\vec{v} \times \vec{B}$$

$$F = BIl \sin \theta \quad \times 90^\circ$$





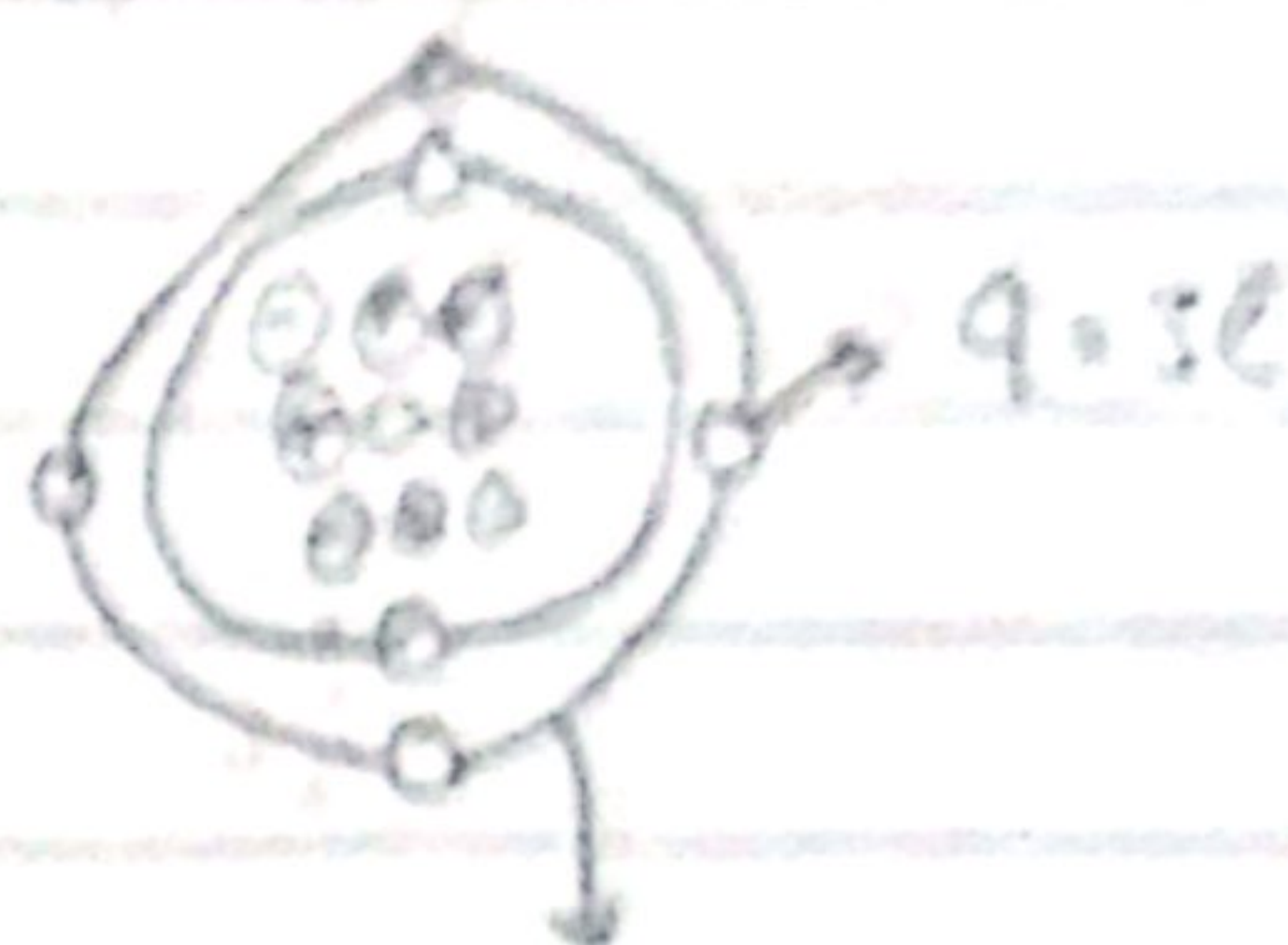
## MEDAN ELEKTROMAGNETIK

Medan oleh Muatan Diskrit

$$q \text{ (muatan)} = \pm Me$$

$$= 2e^-$$

Proton  $q$ , elektron  $q = \text{stabil}$



$$q = +2e^-$$

Note: Arah ke atas, maka simbolnya  $\uparrow$



$$\vec{E} = \frac{1}{4\pi\epsilon_0} = \frac{Lq}{r^2} \hat{r}$$

Muatan terperangkap di sistem koordinat

Note: Muatan adalah keta sifat dari atom

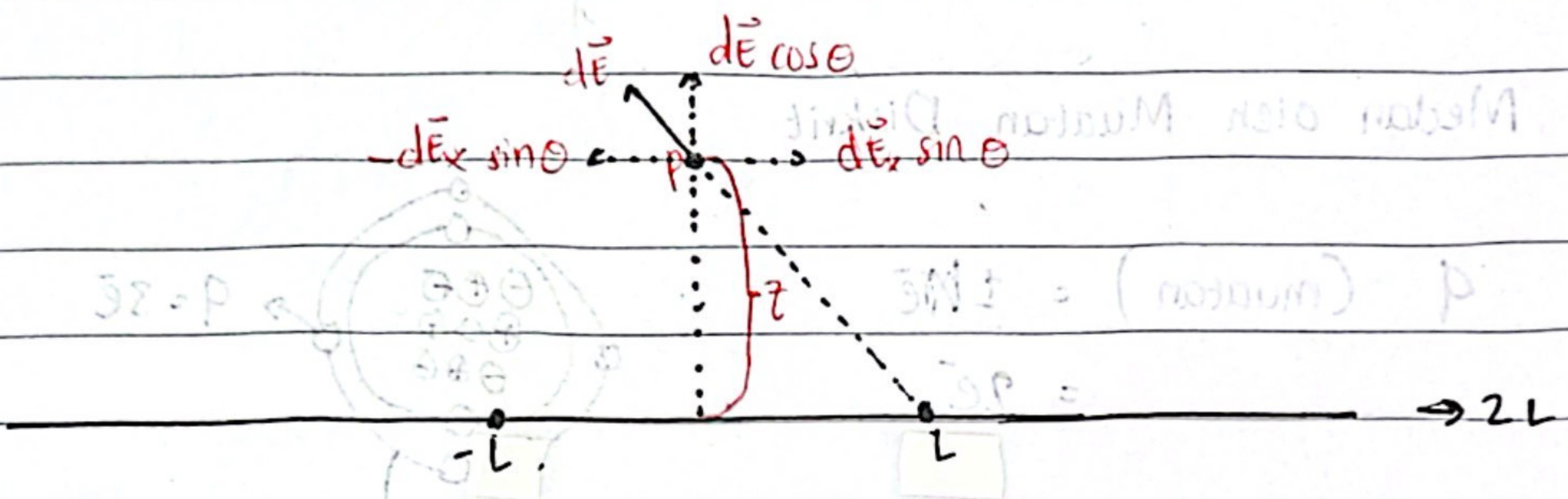
Medan ( $\vec{E}$ ) terdistribusi dalam bahan

$$\vec{E} = \frac{q}{4\pi\epsilon_0 r^2} \hat{r}_0 \rightarrow \text{diskrit}$$

$$\vec{E} = \frac{1}{4\pi\epsilon_0 r^2} \int \frac{q}{r^2} dl \rightarrow \text{terbentuk garis}$$



Contoh:



Penyelesaian:

$$d\vec{E} = dE_y + dE_x = 0$$

$$= dE_y$$

$$d\vec{E} = dE \cos \theta$$

$$\vec{E} = \frac{1}{4\pi\epsilon_0} \int_{-L}^L \frac{d\vec{q}}{r^2}$$

$$= \frac{1}{4\pi\epsilon_0} \int_{-L}^L \frac{\lambda dl}{r^2} \cos \theta$$

$$= \frac{1}{4\pi\epsilon_0} \int_0^{2L} \frac{\lambda dl}{r^2} \cos \theta = \frac{1}{4\pi\epsilon_0} \int_0^{2L} \frac{\lambda z}{r^3} dl$$

$$= \frac{1}{4\pi\epsilon_0} \int_0^{2L} \frac{\lambda z}{(z^2 + l^2)^{3/2}} dl$$

$$= \frac{1}{4\pi\epsilon_0} \int_0^{2L} \frac{\lambda z dl}{(z^2 + l^2)^{3/2}}$$

$$= \frac{z\lambda}{4\pi\epsilon_0} \int_0^{2L} \frac{dl}{(z^2 + l^2)^{3/2}}$$



$$= \frac{z\lambda}{4\pi\epsilon_0} \left[ \frac{l}{z^2(z^2+l^2)^{1/2}} \right]_0^{2l}$$

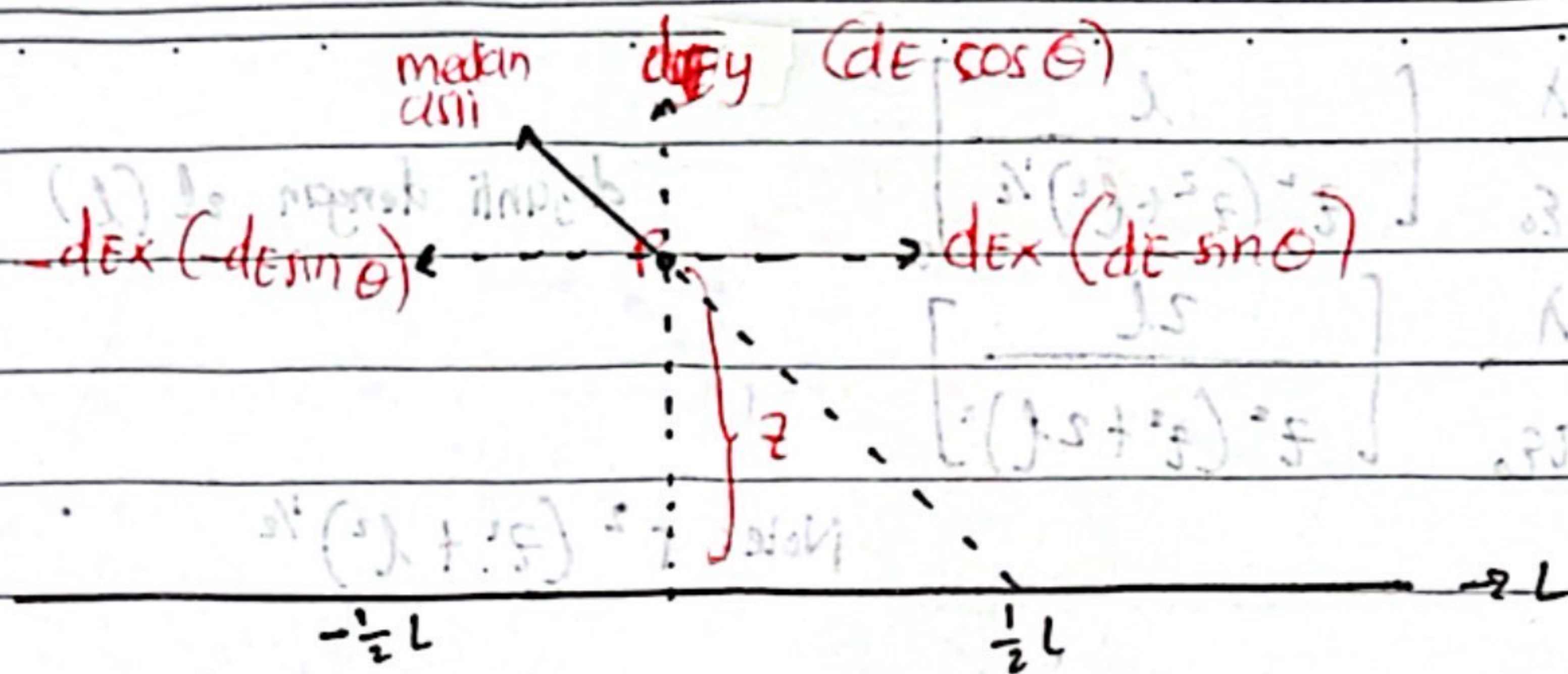
diganti dengan  $z l (L)$

$$\vec{E} = \frac{z\lambda}{4\pi\epsilon_0} \left[ \frac{2l}{z^2(z^2+2l)^2} \right]$$

Note:  $r^2(z^2+l^2)^{1/2}$



Soal



Jawab:

$$d\vec{E} = d\vec{E}_y + d\vec{E}_x$$

$$= d\vec{E}_y$$

$$d\vec{E} = dE \cos \theta$$

$$\text{Note: } r = (z^2 + l^2)^{1/2}$$

$$\vec{E} = \frac{1}{4\pi\epsilon_0} \int_{-L/2}^{L/2} \frac{dq}{r^2} \cos \theta$$

$$= \frac{1}{4\pi\epsilon_0} \int_{-L/2}^{L/2} \frac{\lambda dl}{r^2} \cos \theta$$

$$= \frac{1}{4\pi\epsilon_0} \int_0^L \frac{\lambda dl}{r^2} \cos \theta = \frac{1}{4\pi\epsilon_0} \int_0^L \frac{\lambda dl}{r^2} \cos \theta$$

$$= \frac{1}{4\pi\epsilon_0} \int_0^L \frac{dz}{r^3} dl$$

$$\vec{E} = \frac{1}{4\pi\epsilon_0} \int_0^L \frac{\lambda z dl}{(z^2 + l^2)^{3/2}}$$

$$= \frac{z\lambda}{4\pi\epsilon_0} \int_0^L \frac{dl}{(z^2 + l^2)^{3/2}}$$

$$= \frac{z\lambda}{4\pi\epsilon_0} \left[ \frac{\lambda}{z^2 (z^2 + l^2)^{1/2}} \right]_0^L$$



$$E = \frac{z\lambda}{4\pi\epsilon_0} \left[ \frac{L}{z^2(z^2 + (L)^2)} \right]$$

$$E = \frac{1}{4\pi\epsilon_0} \left[ \frac{\lambda L}{z^2(z^2 + (L)^2)} \right]$$





# MEDAN ELEKTROMAGNETIK

## A. Medan Listrik ( $\vec{E}$ )

### 1. $\vec{E}$ (medan diskrit)

$$\vec{E} = \frac{1}{4\pi\epsilon_0} \frac{q_1 q_2}{r^2} \hat{r}_0 \quad \text{medan terpisah-pisah}$$

### 2. $\vec{E}$ (medan kontinu)

$$\vec{E} = \frac{1}{4\pi\epsilon_0} \frac{\lambda dr}{r^2} \rightarrow \text{gans}$$

$$\vec{E} = \frac{1}{4\pi\epsilon_0} \frac{\sigma dA}{r^2} \rightarrow \text{luas} \rightarrow \text{Hukum Coulomb}$$

$$\vec{E} = \frac{1}{4\pi\epsilon_0} \frac{\rho d\tau}{r^2} \rightarrow \text{volume} \rightarrow \text{Hukum Gauss}$$

Dimensi tinggi

## B. Medan Magnet ( $\vec{B}$ )



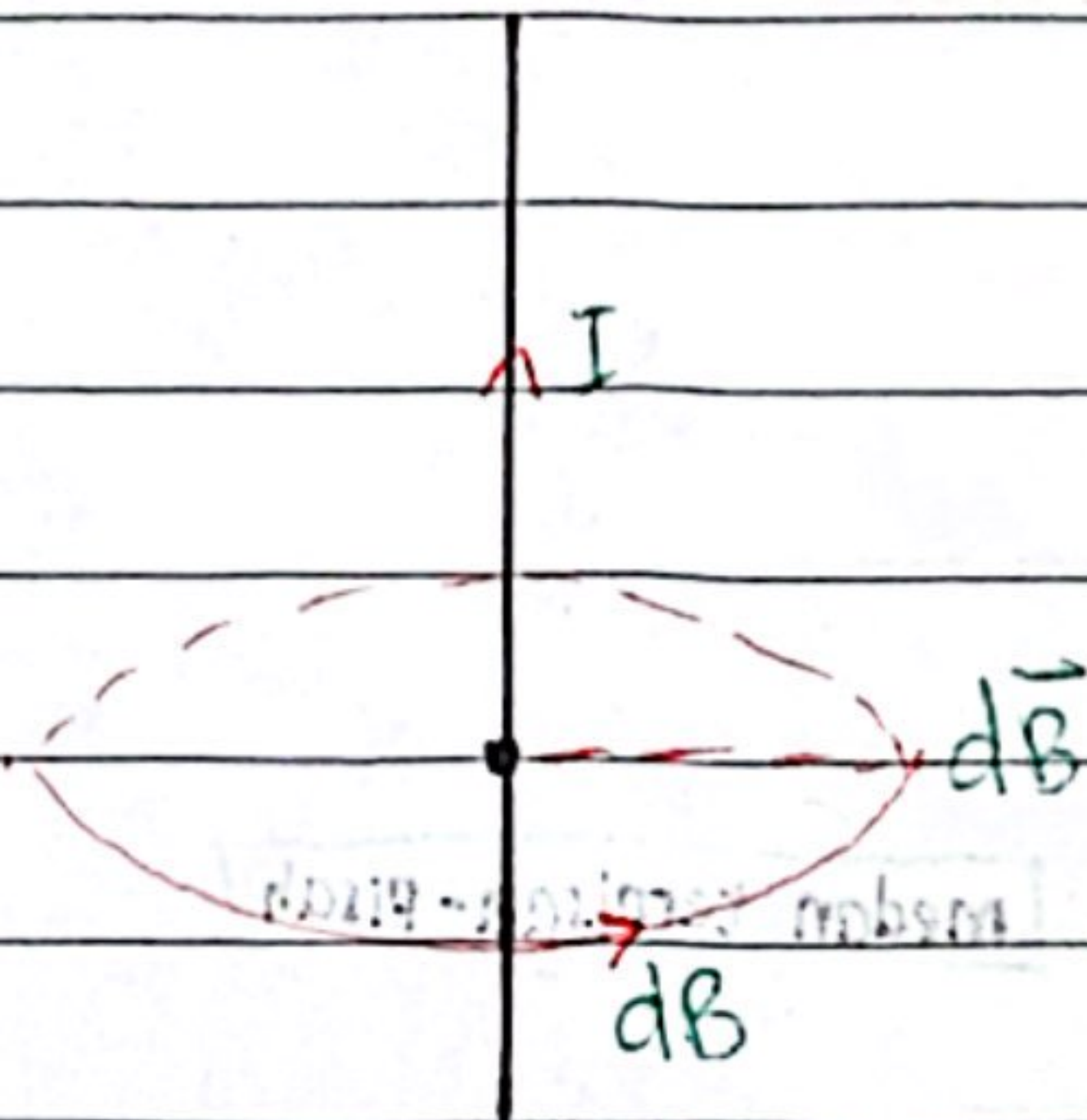
$$\vec{F} = q \vec{v} \times \vec{B}$$

$$\vec{B} = \frac{\mu_0}{4\pi} \frac{q \vec{v} \times \hat{r}}{r^2}$$

$$\vec{B} = \frac{\mu_0}{4\pi} \frac{q \vec{v} \times \hat{r}}{r^2}$$

$$\vec{B} = \frac{\mu_0}{4\pi} \frac{q \vec{v} \times \hat{r}}{r^2}$$



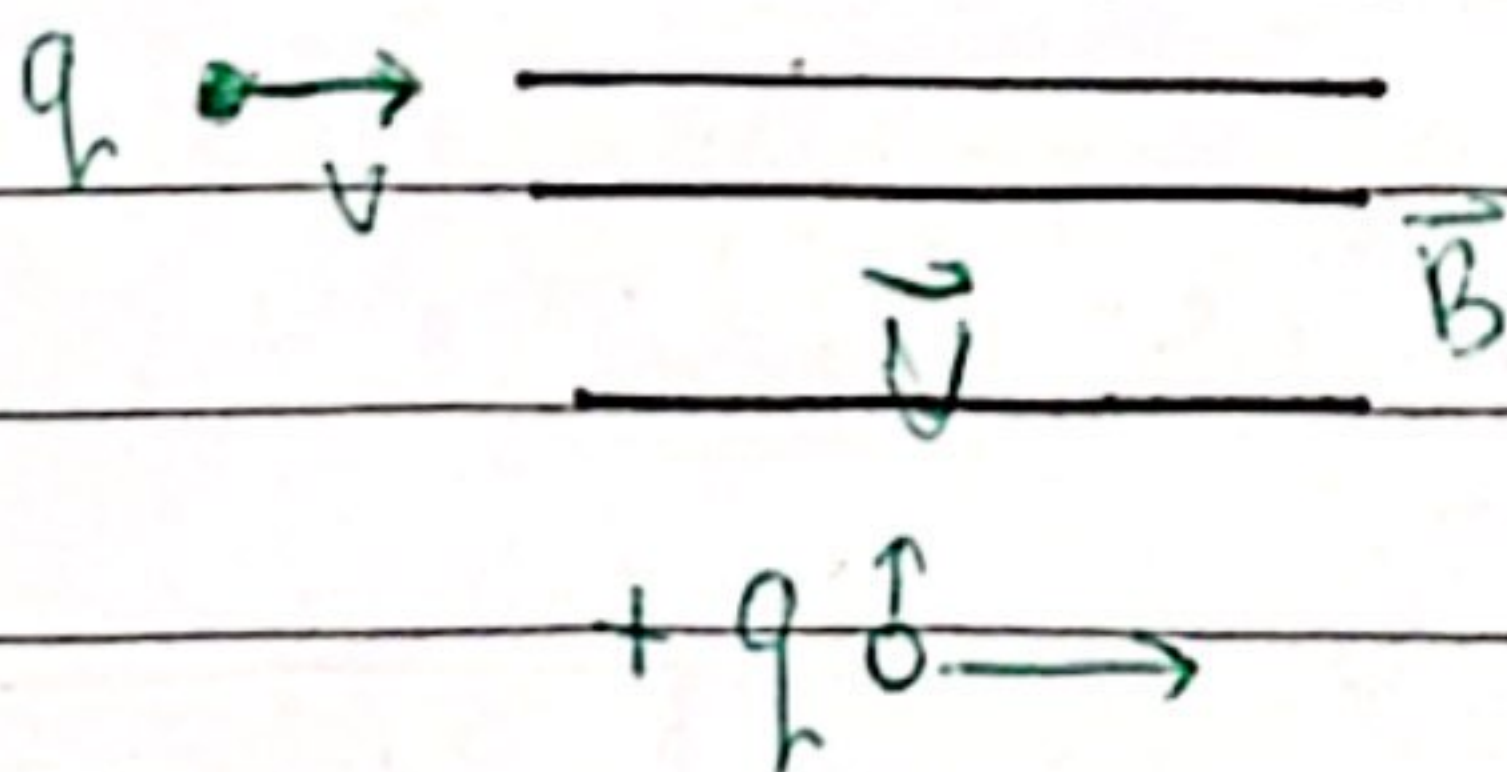


$$d\vec{B} = \frac{\mu_0}{4\pi} \frac{I d\vec{r} \times \hat{r}_0}{r^2} \quad \text{muatan}$$

$$\vec{B} = \frac{\mu_0}{4\pi} \int \frac{I d\vec{r} \times \hat{r}_0}{r^2} \quad \text{arus}$$

$$B = \frac{\mu_0}{4\pi} \iint \frac{I d\vec{a} \times \hat{r}_0}{r^2} \quad \text{luas}$$

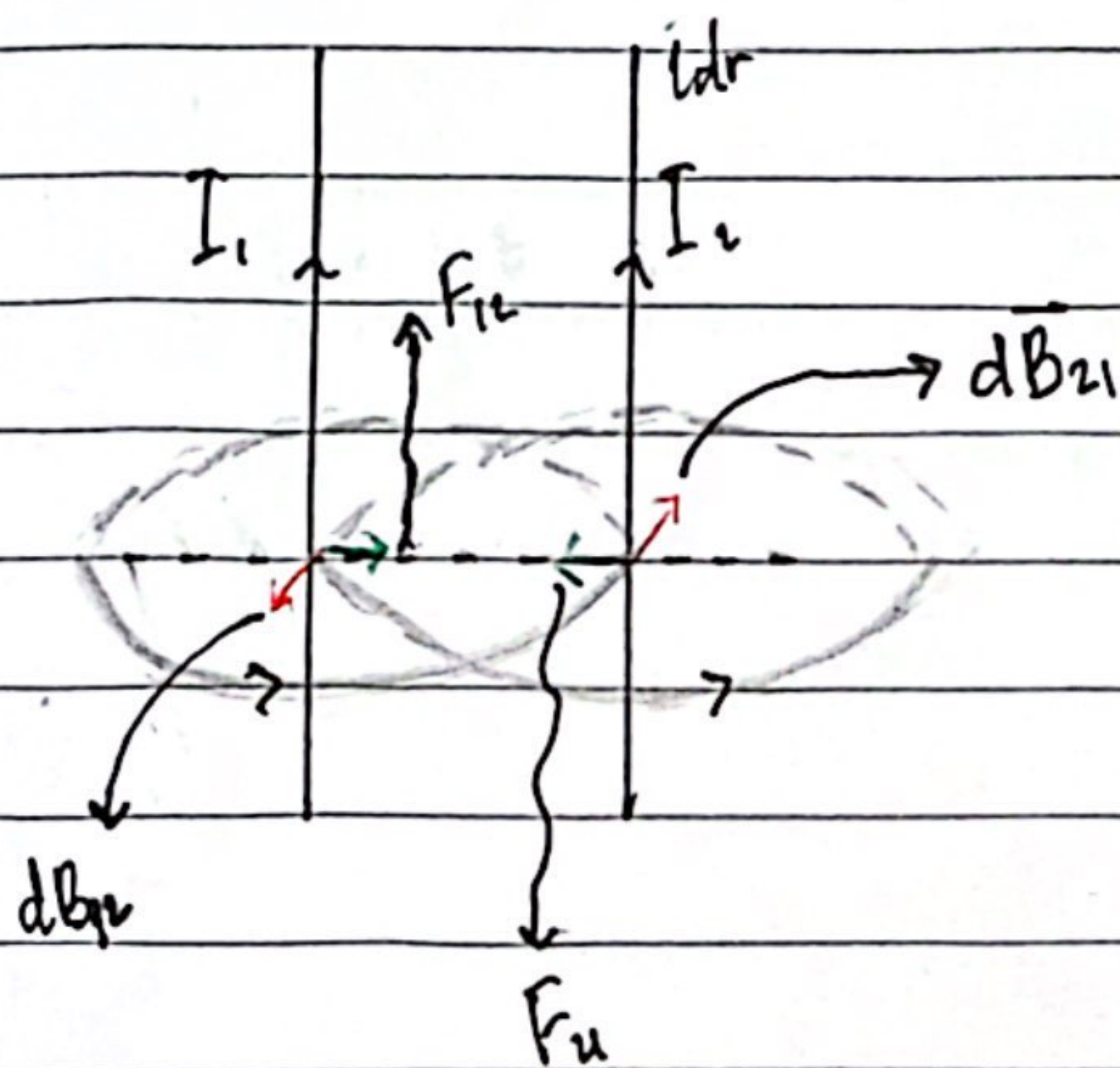
$$B = \frac{\mu_0}{4\pi} \iiint \frac{I d\vec{\tau} \times \hat{r}_0}{r^2} \quad \text{volume}$$



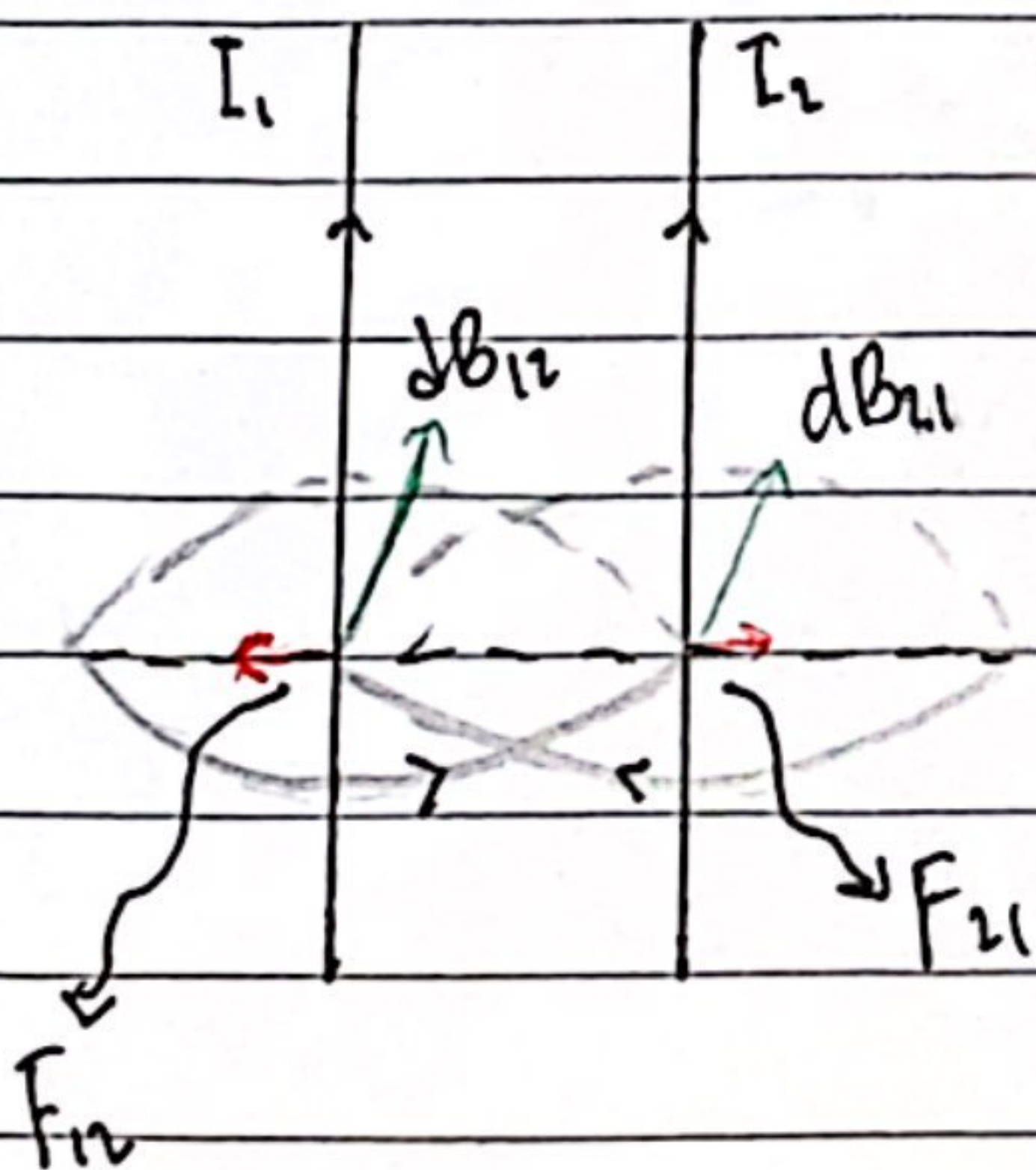
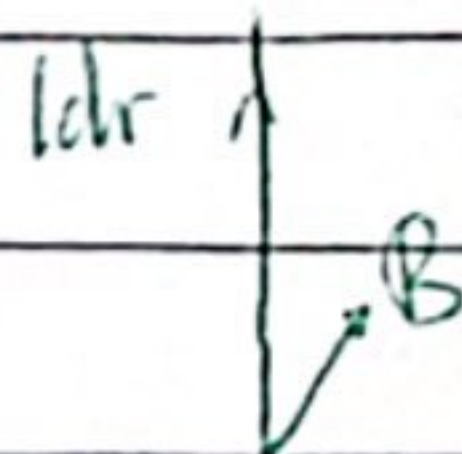
$$\vec{F} = q\vec{v} \times \vec{B}$$

$$\vec{B} = \frac{\mu_0}{4\pi} \frac{q\vec{v} \times \vec{B}}{r^2}$$



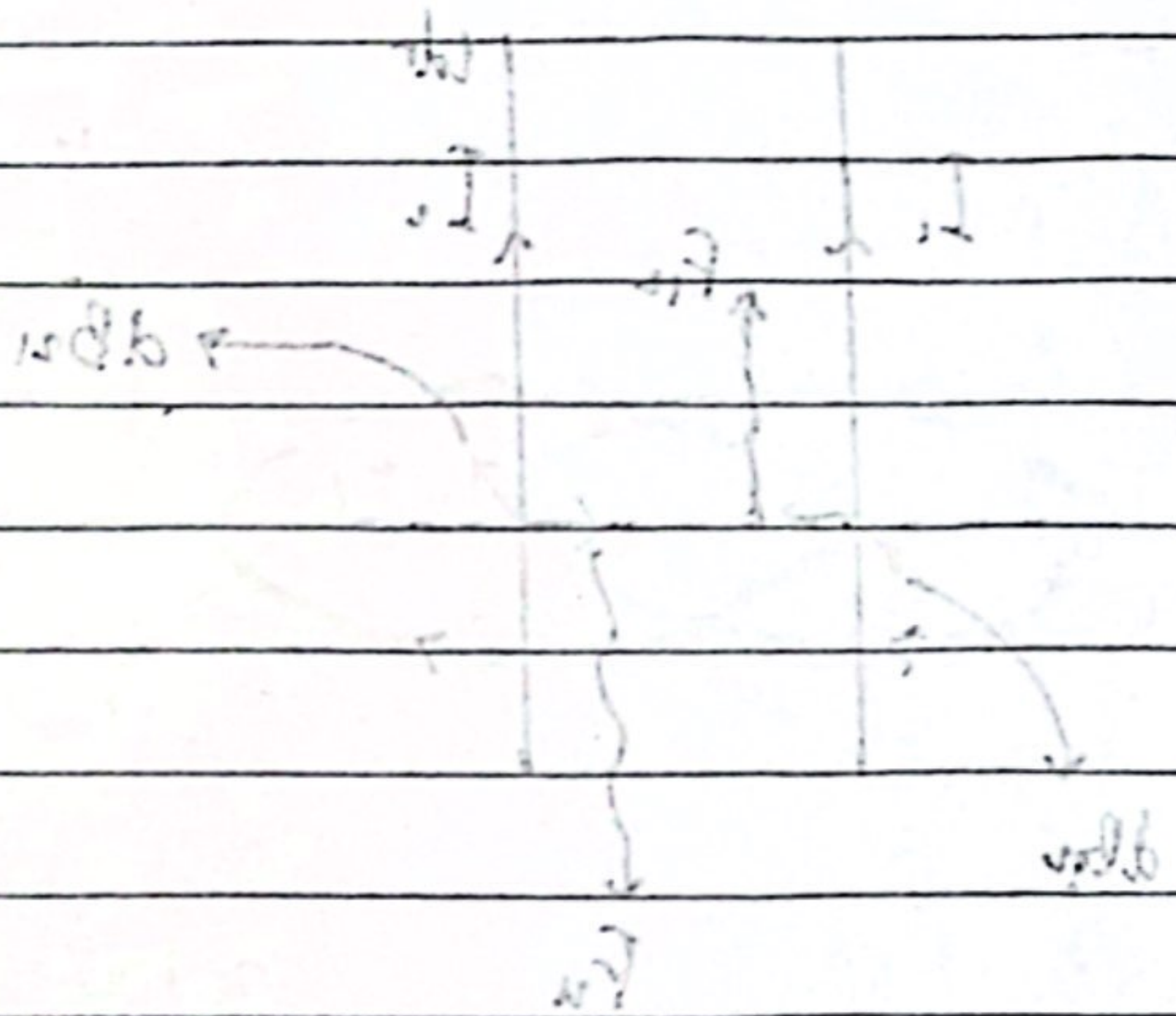
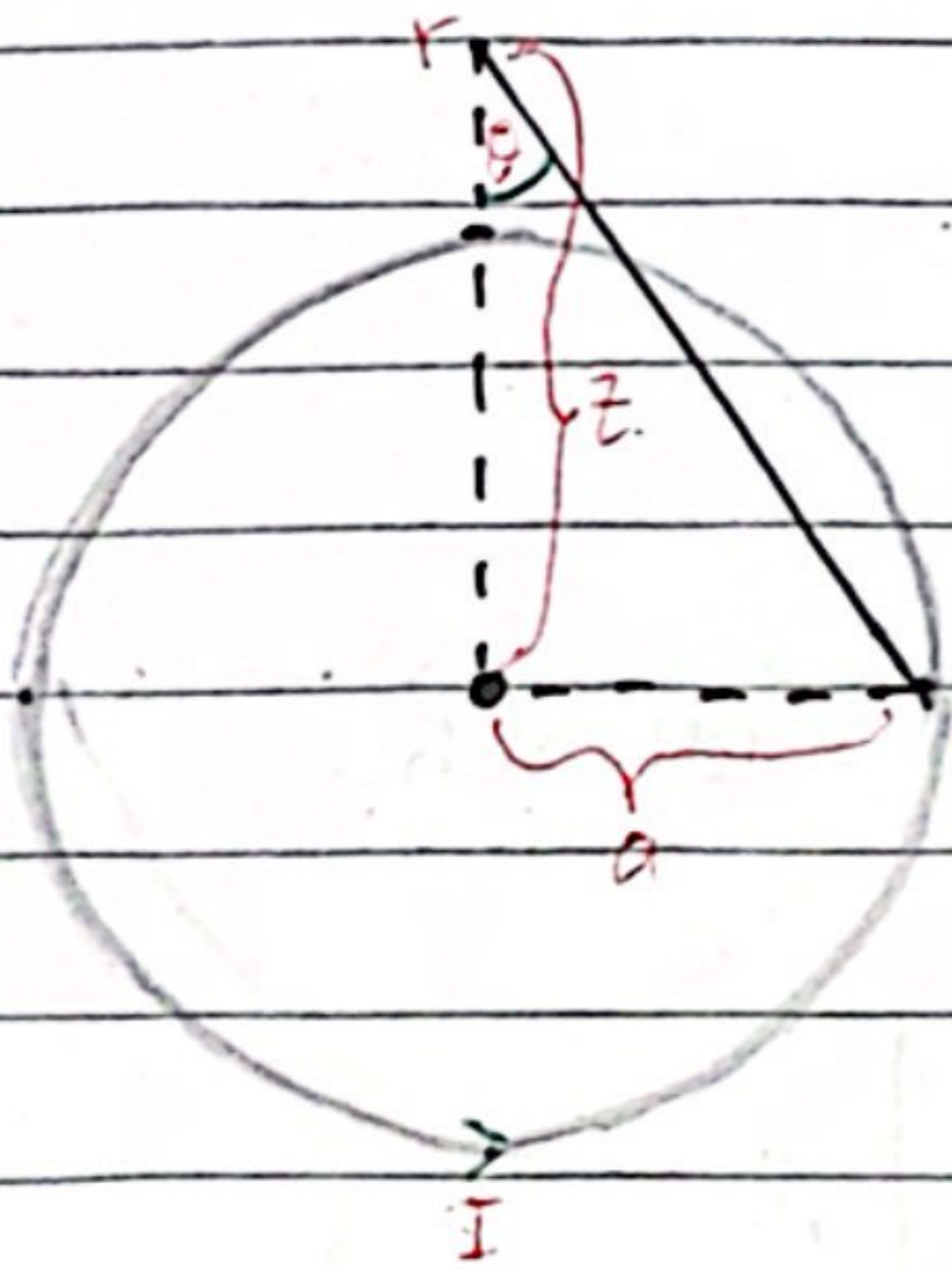


$$\vec{F} = i d\vec{r} \times \vec{B}$$



$$\begin{aligned} \frac{d\vec{B}_{12}}{dB} &= \frac{\mu_0 I_1}{2\pi r} \hat{r} \\ \frac{d\vec{B}_{21}}{dB} &= \frac{\mu_0 I_2}{2\pi r} \hat{r} \\ \frac{d\vec{B}_{12}}{dB} &= \frac{\mu_0 I_1}{2\pi r} \hat{r} \\ \frac{d\vec{B}_{21}}{dB} &= \frac{\mu_0 I_2}{2\pi r} \hat{r} \\ \frac{d\vec{B}_{12}}{dB} &= \frac{\mu_0 I_1}{2\pi r} \hat{r} \\ \frac{d\vec{B}_{21}}{dB} &= \frac{\mu_0 I_2}{2\pi r} \hat{r} \\ \frac{d\vec{B}_{12}}{dB} &= \frac{\mu_0 I_1}{2\pi r} \hat{r} \\ \frac{d\vec{B}_{21}}{dB} &= \frac{\mu_0 I_2}{2\pi r} \hat{r} \end{aligned}$$





$$\vec{B} = \frac{\mu_0}{4\pi} \int \frac{I d\vec{r} \times \hat{r}_0}{r^2}$$

$$= \frac{\mu_0}{4\pi} \int_0^{2\pi a} \frac{i \sin\theta dr}{r^2}$$

$$= \frac{\mu_0}{4\pi} \int_0^{2\pi a} \frac{ia}{r^3} dr$$

$$= \frac{\mu_0}{4\pi} \int_0^{2\pi a} \frac{ia}{(a^2+z^2)^{3/2}} dr$$

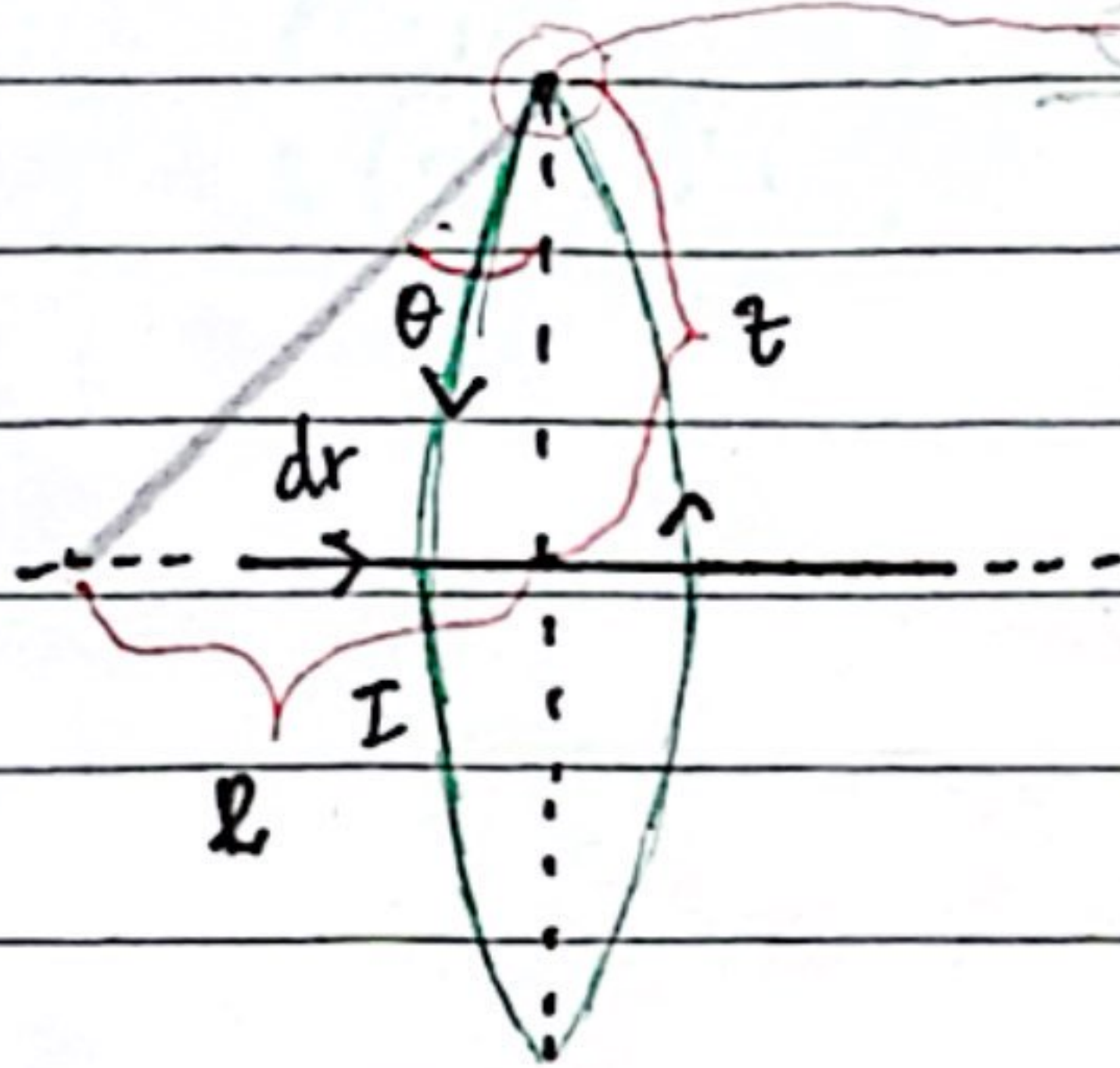
$$= \frac{\mu_0}{4\pi} \cdot \frac{ia}{(a^2+z^2)^{3/2}} \int_0^{2\pi a} dr$$

$$= \frac{\mu_0}{4\pi} \cdot \frac{ia}{(a^2+z^2)^{3/2}} (2\pi a)$$

$$= \frac{\mu_0 \cdot a^2}{2(a^2+z^2)^{3/2}}$$

$$B = \frac{\mu_0 I a^2}{2(a^2+z^2)^{3/2}}$$





$$d\vec{B} = \frac{\mu_0}{4\pi} \int \frac{I d\vec{r} \times \vec{r}}{r^3}$$

$$= \frac{\mu_0 I}{4\pi} \int \frac{\sin \theta dr}{r^2}$$

$$\tan \theta = \frac{R}{z} \rightarrow R = z \tan \theta$$

$$dr = z \sec^2 \theta d\theta$$

$$\tan \theta = \frac{\sin \theta}{\cos \theta}$$

$$= \frac{\sin^2 \theta + \cos^2 \theta}{\cos^2 \theta}$$

$$= \frac{1}{\cos^2 \theta}$$

$$= \sec^2 \theta$$

$$\cos \theta = \frac{z}{r}$$

$$r = \frac{z}{\cos \theta}$$

$$= z \sec \theta$$



$$\vec{B} = \frac{M_0}{4\pi} \int_{-2\pi}^{2\pi} \frac{\sin \theta \, z \, \sec^2 \theta \, d\theta}{z^2 \sec^2 \theta}$$

$$= \frac{M_0 i}{4\pi} \int_{-2\pi}^{2\pi} \frac{\sin \theta \, d\theta}{z}$$

$$= \frac{M_0 i}{4\pi z} \int_{-2\pi}^{2\pi} \sin \theta \, d\theta$$

$$= \frac{M_0 i}{2\pi z}$$

$$- \cos 2\pi = -(-1)$$

$$= 1 - (\cos 2\pi)$$

$$1 + 1 = 2$$

$$\vec{B} = \frac{M_0}{4\pi} \int \frac{i d\vec{r} \times \hat{r}_0}{r^2} \theta^{200} + \theta^{100}$$

$$= \frac{M_0}{4\pi} \int_0^{2\pi a} \frac{i \sin \theta \, dr}{r^2}$$

$$= \frac{M_0}{4\pi} \int_0^{2\pi a} \frac{ia}{r^3} \, dr$$

$$= \frac{M_0}{4\pi} \int_0^{2\pi a} \frac{ia}{(a^2 + z^2)^{3/2}} \, dr$$

$$= \frac{M_0}{4\pi} \frac{ia}{(a^2 + z^2)^{3/2}} \int_0^{2\pi a} dr$$

$$= \frac{M_0}{4\pi} \frac{ia}{(a^2 + z^2)^{3/2}} (2\pi a)$$



No. 7

Date :

$$= \frac{\mu_0 i a^2}{2 (a^2 + z^2)^{3/2}}$$

