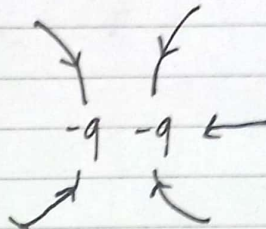
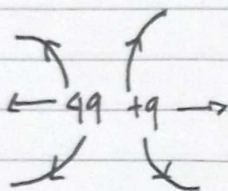
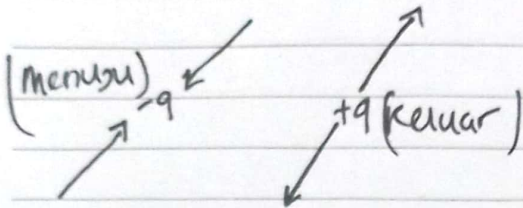


Kelistrikan

1. Statis = Gaya listrik, Medan listrik, Potensial
2. Dinamis = Energi, Usaha, Polarisasi, dielektrik

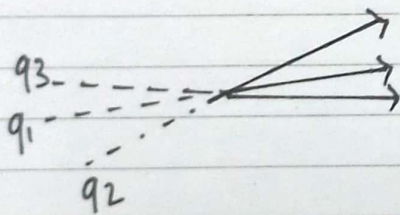
Kemagnetan : Medan magnet, elektromagnet

$$\text{atom} \rightarrow q = n \cdot e$$

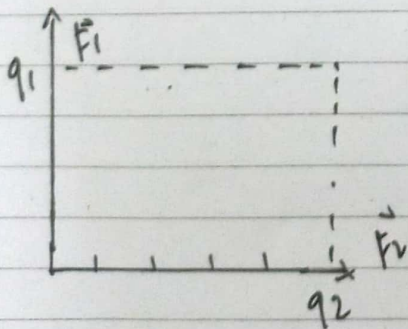


$$F = k$$

$$F = \frac{1}{4\pi\epsilon_0} \frac{q \cdot q}{r^2}$$

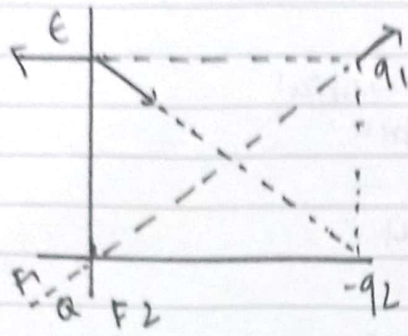


$$F_A = \vec{F}_1 + \vec{F}_2 + \vec{F}_3$$



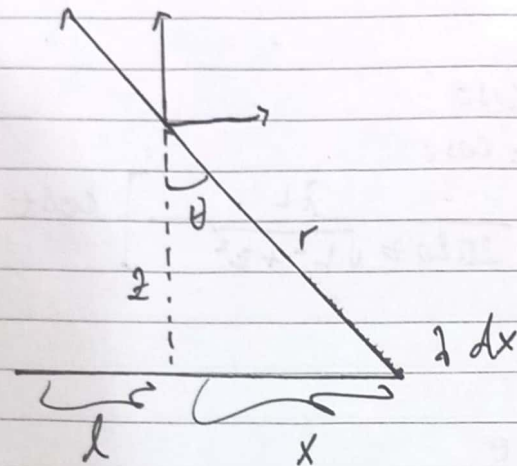
$$F_A = kq \left[\frac{q_1}{3^2} (\hat{j}) + \frac{q_2}{4^2} (\hat{i}) \right]$$

$$= -kq \left[\frac{q_1}{9} \hat{j} + \frac{q_2}{16} \hat{i} \right]$$



$$\hat{p} = \frac{\vec{p}}{r}$$

$$F = kQ \left[\frac{q_1}{5^2} \left(-\frac{4\hat{i}}{5} - \frac{3\hat{j}}{5} \right) + \frac{q_2}{4^2} \hat{j} \right]$$



$$d\vec{E} = d\vec{E}_x + d\vec{E}_y$$

$$= dE \cos \theta$$

$$= \frac{1}{4\pi\epsilon_0} \int_{-L}^L \frac{\lambda dx}{r^2} \cos \theta$$

$$= \frac{1}{4\pi\epsilon_0} \int_0^L \frac{2 \lambda dx}{r^2} \cos \theta$$

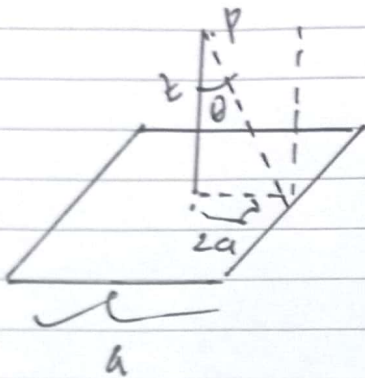
$$= \frac{1}{4\pi\epsilon_0} \int_0^L \frac{2 \lambda x dx}{(x^2 + z^2)^{3/2}}$$

$$= \frac{2 \lambda x}{4\pi\epsilon_0} \int_0^L \frac{dx}{(x^2 + z^2)^{3/2}}$$

$$= \frac{2 \lambda x}{4\pi\epsilon_0} \left[\frac{x}{z^2 \sqrt{x^2 + z^2}} \right]_0^L$$

$$= \frac{\lambda}{2\pi\epsilon_0} = \left[\frac{L}{\sqrt{L^2 + z^2}} \right]$$

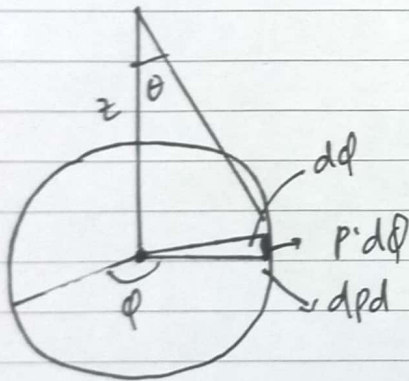
$$E = \frac{\lambda}{2\pi\epsilon_0 z \sqrt{L^2 + z^2}}$$



$$\begin{aligned} \vec{E}_z &= E_z' \cos \theta \\ &= 4 E_z' \cos \theta \\ &= 4 \left[\frac{\lambda L}{2\pi \epsilon_0 z \sqrt{L^2 + z^2}} \right] \cos \theta \end{aligned}$$

$$\cos \theta = \frac{z}{z'}$$

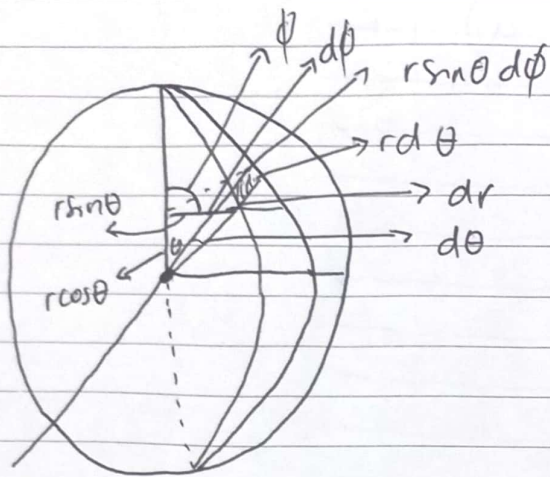
$$\begin{aligned} z &= z' \cos \theta \\ z' &= \sqrt{z^2 + \left(\frac{1}{2}a\right)^2} \end{aligned}$$



$$E = \frac{1}{4\pi\epsilon_0} \int_0^R \int_0^{2\pi} \frac{\sigma dA \cos \theta}{r^2}$$

$dr' r' d\phi$
 $r' dr' d\phi$

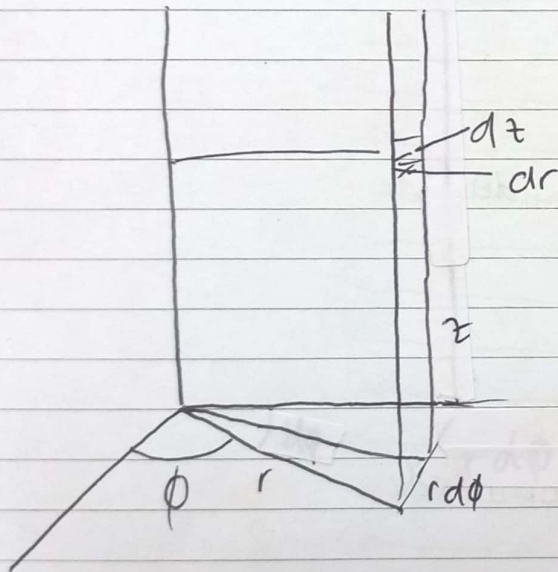
$$\begin{aligned} E &= \frac{\sigma}{4\pi\epsilon_0} 2\pi z \int_0^R \frac{r' dr'}{(z^2 + r'^2)^{3/2}} \\ &= \frac{2\pi z \sigma}{4\pi\epsilon_0} \frac{1}{2} \int_0^R \frac{d(r'^2 + z^2)}{(z^2 + r'^2)^{3/2}} \\ &= \frac{2\pi z \sigma}{4\pi\epsilon_0} \frac{1}{2} \end{aligned}$$



$$V = \rho \times \Delta x \times \Delta y \times \Delta z$$

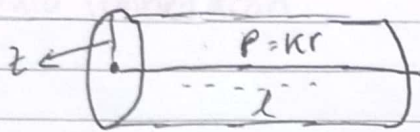
$$= r d\theta \cdot r \sin \theta d\phi \cdot dr$$

$$V = r^2 \sin \theta d\theta d\phi dr$$



$$V = \rho \times \Delta x \times \Delta y \times \Delta z$$

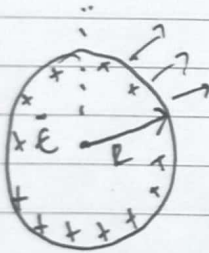
$$V = \rho d\phi dr dz$$



$$\oint \vec{E} \cdot d\vec{a} = \frac{Q_{in}}{\epsilon_0}$$

$$\begin{aligned} (2\pi r l) &= \frac{1}{\epsilon_0} \iiint \rho db \\ &= \frac{1}{\epsilon_0} \int_0^l \int_0^{2\pi} \int_0^r (kr) r dr d\phi dz \\ &= \frac{2\pi l k}{\epsilon_0} \int_0^r r^2 dr \end{aligned}$$

Potensial



$$\vec{E} = \nabla v$$

$$\vec{E} \cdot d\vec{\phi} = -\Delta v d\phi$$

$$\int \vec{E} d\phi = -\int \Delta v d\phi$$

$$= -dv$$

$$dv = -\int \vec{E} d\phi$$

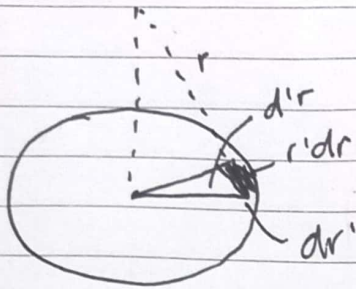
$$\int_a^b dv = -\int \frac{Q}{4\pi\epsilon_0 r^2} dr$$

$$v_b - v_a = \frac{Q}{4\pi\epsilon_0 r^2}$$

$$v_b = v_a = \frac{Q}{4\pi\epsilon_0 r}$$

$$\begin{aligned} v &= -\int \frac{Q}{4\pi\epsilon_0 r} = \frac{Q}{4\pi\epsilon_0 r} \Big|_0^r \\ &= \frac{Q}{4\pi\epsilon_0 r} \end{aligned}$$

$$= -\int \vec{E} d\phi + \int_r^R \vec{E} d\phi = \frac{Q}{4\pi\epsilon_0 R}$$



$$V = \frac{1}{4\pi\epsilon_0} \iint \frac{\sigma da}{r}$$

$$da = r' dr$$

$$V = \frac{1}{4\pi\epsilon_0} \int_0^R \int_0^{2\pi} \frac{r' dr' d\theta}{(r'^2 + z^2)^{1/2}}$$

$$= \frac{2\pi}{4\pi\epsilon_0} \sigma \int_0^R \frac{r' dr'}{(r'^2 + z^2)^{1/2}}$$

$$= \frac{2\pi}{4\pi\epsilon_0} \sigma \int_0^R \frac{(r'^2 + z^2)^{-1/2} dr'^2}{2}$$

$$= \frac{2\pi}{4\pi\epsilon_0} \sigma \int_0^R (r'^2 + z^2)^{-1/2} dr'^2$$

$$\int x^n dx$$

$$= \frac{1}{2} \sigma \frac{2\pi}{4\pi\epsilon_0} \left[\frac{(r'^2 + z^2)^{-1/2 + 1}}{-1/2 + 1} \right]$$

$$= \frac{1}{2} \sigma \left[\frac{r'^2 + z^2}{1/2} \right]^{1/2}$$

$$= \frac{\sigma 2\pi}{4\pi\epsilon_0} \left[(r'^2 + z^2)^{1/2} \right]_0^R$$

$$= \frac{\sigma 2\pi}{4\pi\epsilon_0} (R^2 + z^2)^{1/2} + (r^2 + z^2)^{1/2}$$

$$= \frac{\sigma 2\pi}{4\pi\epsilon_0} (R^2 + z^2)^{1/2} + z$$