

Nama : Eky Gustiyo Saputra
 Npm : 2313022061
 Kelas : 23 08 18
 Fisika modern

1. $x_1 = 0$ hingga $x_2' = l_0$

$$l = x_2 - x_1$$

$$x' = \gamma(x - ut)$$

$$t' = \gamma\left(t - \frac{ux}{c^2}\right)$$

$$\gamma = \frac{1}{\sqrt{1 - \frac{u^2}{c^2}}}$$

$$l_0 = \gamma(x_2 - x_1) \text{ atau}$$

$$l = \frac{l_0}{\gamma} \Rightarrow \gamma = \frac{l_0}{l} \Rightarrow \frac{1}{\sqrt{1 - \frac{u^2}{c^2}}} = \frac{l_0}{l}$$

• Waktu sama ($t_1 = t_2$)

$$x_1' = \gamma(x_1 - ut)$$

$$x_2' = \gamma(x_2 - ut)$$

$$l_0 = x_2' - x_1'$$

$$l_0 = \gamma(x_2 - ut) - \gamma(x_1 - ut)$$

$$l = l_0 \sqrt{1 - \frac{u^2}{c^2}}$$

2. Diketahui :

$$E = 25 \text{ GeV}$$

$$d = 3000 \text{ m}$$

$$m_0 = 0.511 \text{ MeV}/c^2$$

$$c = 3 \times 10^8 \text{ m/s}$$

Ditanya :

a. Kecepatan elektron yang energinya 25 GeV?

b. Waktu yang diperlukan untuk menempuh jarak 300 m?

c. Panjang akselerator dalam kerangka diam elektron?

d. Waktu tempuh elektron dalam kerangka diamnya sendiri?

Jawab :

$$a) E = \gamma m_0 c^2$$

$$\gamma = \frac{E}{m_0 c^2}$$

$$= \frac{25 \times 10^9 \text{ eV}}{0.511 \times 10^6 \text{ eV}}$$

$$= 4.89 \times 10^4$$

$$1 = \frac{v^2}{c^2} = \frac{1}{\gamma^2}$$

$$\frac{v^2}{c^2} = 1 - \frac{1}{(4.89 \times 10^4)^2}$$

$$v = c \sqrt{1 - \frac{1}{(4.89 \times 10^4)^2}}$$

$$v \approx c(1 - 1.05 \times 10^{-10})$$

$$v \approx 2.99999 \times 10^8 \text{ m/s}$$

Sangat dengan kecepatan cahaya

$$(-v \approx 0.031 \text{ m/s})$$

Jadi elektron hampir bergerak dengan kecepatan cahaya.

$$b) t = \frac{d}{v}$$

$$t = \frac{3000 \text{ m}}{2.99999 \times 10^8 \text{ m/s}}$$

$$t \approx 1.0000000001 \times 10^{-5} \text{ s}$$

$$\approx 10 \text{ ns}$$

$$c) l' = l \sqrt{1 - \frac{v^2}{c^2}}$$

Karena $\lambda \approx 4.89 \times 10^4$, maka

$$l' = \frac{3000}{4.89 \times 10^4}$$

$$l' \approx 0.0061 \text{ m} = 6.1 \text{ mm}$$

$$d) t' = \frac{t}{\gamma}$$

$$t' = \frac{10^{-5}}{4.89 \times 10^4}$$

$$t' \approx 2.04 \times 10^{-9} \text{ s} = 0.204 \text{ ns}$$

$$3. \text{ Diketahui : } \lambda_0 = 122 \text{ nm}$$

$$\lambda_1 = 366 \text{ nm}$$

$$c = 3 \times 10^8 \text{ m/s}$$

Ditanya = a) Kecepatan galaksi v jika spektrum bergeser dari λ_0 menjadi λ_1 ?

b) Panjang gelombang baru λ jika galaksi mendekati kita dengan kecepatan yang sama

$$a) \frac{\lambda}{\lambda_0} = \sqrt{\frac{1 + \frac{v}{c}}{1 - \frac{v}{c}}}$$

$$\frac{366 \text{ nm}}{122 \text{ nm}} = \sqrt{\frac{1 + \frac{v}{c}}{1 - \frac{v}{c}}}$$

$$3 \text{ nm} = \sqrt{\frac{1 + \frac{v}{c}}{1 - \frac{v}{c}}}$$

$$g = \frac{1 + \frac{v}{c}}{1 - \frac{v}{c}}$$

$$g = \left(1 - \frac{v}{c}\right) = 1 + \frac{v}{c}$$

$$g - g \frac{v}{c} = 1 + \frac{v}{c}$$

$$g = 10 \frac{v}{c}$$

$$v = \frac{g}{10} c = 0,8c$$

$$v = 0,8 (3 \times 10^8 \text{ m/s})$$

$$= 2,4 \times 10^8 \text{ m/s}$$

$$b. \frac{\lambda'}{\lambda_0} = \sqrt{\frac{1 - \frac{v}{c}}{1 + \frac{v}{c}}}$$

$$\lambda'' = \lambda_0 \times \sqrt{\frac{1 - 0,8}{1 + 0,8}}$$

$$= \lambda_0 \times \sqrt{\frac{0,2}{1,8}}$$

$$= 122 \times \sqrt{0,1111} \text{ m}$$

$$= 122 \times 0,3323$$

$$\lambda'' \approx 40,67 \text{ nm}$$

4. Diketahui :

$$E \text{ per atom} = 200 \text{ mev}$$

uranium :

$$A = 235$$

$$1 \text{ mev} = 1,602 \times 10^{-13} \text{ J}$$

$$c = 3 \times 10^8 \text{ m/s}$$

$$M \text{ atom} = 235g$$

$$6,022 \times 10^{23}$$

Ditanya : perubahan massa dan energi reaksi 1 kg uranium?

Jawab :

$$E = 200 \text{ mev} \times 1,602 \times 10^{-13} \text{ J/mev}$$

$$= 3,204 \times 10^{-11} \text{ J}$$

Jumlah atom dalam uranium 1kg :

$$N = \frac{1000 \text{ g}}{M \text{ atom}}$$

$$= \frac{1000 \text{ g}}{235} \cdot 2,56 \times 10^{24} \text{ atom}$$

$$6,022 \times 10^{23}$$

$$E \text{ total} : (3,204 \times 10^{-11} \text{ J (atom)}) (2,56 \times 10^{24})$$

$$= 8,20 \times 10^{13} \text{ J}$$

$$E = mc^2 \rightarrow m = E / c^2$$

$$m = (1,20 \times 10^{16} \text{ J}) / (3 \times 10^8 \text{ m/s})^2$$

$$= 9,91 \times 10^{-4} \text{ kg}$$

5. Diketahui :

$$m_p = 1,017276 \text{ u}$$

$$m_n = 1,008665 \text{ u}$$

$$m_{\text{helium}} = 4,001506 \text{ u}$$

$$1 \text{ u} = 1,66054 \times 10^{-27} \text{ kg}$$

$$1 \text{ u} = 931,5 \text{ MeV}$$

Ditanya :

a) energi kuat-mukha helium E_b

b) benda massa muh helium dengan foto massa fotokul

Jawab :

$$a) \text{ massa total} = 2 m_p + 2 m_n$$

$$= 2 (1,017276) + 2 (1,008665)$$

$$= 4,031822$$

$$\Delta m = m_{\text{total}} - m_{\text{helium}}$$

$$= 4,031822 - 4,001506$$

$$= 0,030316 \text{ u}$$

$$E = \Delta m c^2$$

$$= (3,044 \times 10^{-29} \text{ kg}) (2,9979 \times 10^8 \text{ m/s})^2$$

$$= 2,73 \times 10^{-12} \text{ J} = 17,1 \text{ MeV}$$

$$b) \Delta m \text{ kg} = 0,030316 \text{ u} \times (1,66054 \times 10^{-27} \text{ kg})$$

$$= 5,04 \times 10^{-29} \text{ kg}$$

6. Diketahui :

$$v_A = 0,8 \text{ c}$$

$$v_B = 0,6 \text{ c}$$

Ditanya : kecepatan perawat di bulan (v') ?

Jawab :

$$v' = \frac{v_A + v_B}{1 + \frac{v_A v_B}{c^2}} = \frac{0,8 + 0,6 \text{ c}}{1 + (0,8)(0,6)} = \frac{1,4 \text{ c}}{1 + 0,48} = \frac{1,4}{1,48} = 0,946 \text{ c}$$

7. Diketahui :

$$P = 20 \text{ W}$$

$$\lambda = 589 \text{ nm} = 589 \times 10^{-9} \text{ m}$$

$$h = 6.626 \times 10^{-34} \text{ Js}$$

$$c = 3 \times 10^8 \text{ m/s}$$

Ditanya : Jumlah foto m yang dipancarkan ?

Jawab :

$$E = \frac{hc}{\lambda} = \frac{(6.626 \times 10^{-34}) (3 \times 10^8)}{589 \times 10^{-9}}$$
$$= \frac{1.9878 \times 10^{-25}}{589 \times 10^{-9}} \approx 3.37 \times 10^{-19} \text{ J}$$

$$N = \frac{20}{3.37 \times 10^{-19}} = 5.99 \times 10^{19} \text{ foton / detik.}$$

8. Diketahui :

$$W = 2.2 \text{ eV}$$

$$\lambda = 3500 \text{ Å} = 3500 \times 10^{-10} \text{ m} = 3.5 \times 10^{-7} \text{ m}$$

$$c = 3 \times 10^8 \text{ m/s}$$

$$1 \text{ eV} = 1.6 \times 10^{-19} \text{ J}$$

Ditanya : Energi kinetik maksimum foto elektron (h) dalam eV ?

Jawab :

$$E = \frac{hc}{\lambda} = \frac{(6.626 \times 10^{-34}) (3 \times 10^8)}{3.5 \times 10^{-7}} = \frac{1.9878 \times 10^{-25}}{3.5 \times 10^{-7}}$$
$$\approx 5.68 \times 10^{-19} \text{ J.}$$

$$E = \frac{5.68 \times 10^{-19}}{1.6 \times 10^{-19}} = 3.53 \text{ eV}$$

$$K = E - W$$

$$= 3.53 - 2.2 = 1.33 \text{ eV}$$