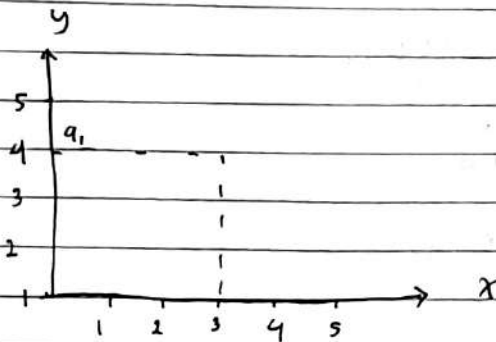


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1. Gaya, medan, potensial, usaha dan energi oleh muatan listrik empat buah muatan berada pada posisi $q_1 (0, 4) \text{ m}$, $-q_2 (0, 0)$, $q_3 (3, 4) \text{ m}$ dan $q_4 (3, 0) \text{ m}$
- Hitung gaya listrik yg dialami oleh muatan q_2 !
 - Hitung medan listrik pada muatan q_2 !
 - Hitung potensial pada muatan q_4
 - Berapa besarnya usaha untuk memindahkan ke empat muatan dari jarak tak hingga

Jawab

a.



gaya q_1 ke q_2 $r = 4 \text{ m}$

$$\begin{aligned} \vec{F}_{21} &= k \frac{q_1 q_2}{r^2} \\ &= k \frac{q_1 q_2}{4^2} \\ &= k \frac{q_1 q_2}{16} \end{aligned}$$

gaya q_3 ke q_2 $r = 5 \text{ m}$

$$\begin{aligned} \vec{F}_{32} &= k \frac{q_1 q_2}{r^2} \\ &= k \frac{q_1 q_2}{5^2} \\ &= k \frac{q_1 q_2}{25} \end{aligned}$$

gaya q_4 ke q_2 $r = 3 \text{ m}$

$$\begin{aligned} F_{q_2} &= k \frac{q_1 q_2}{r^2} \\ &= k \frac{q_1 q_2}{3^2} \\ &= k \frac{q_1 q_2}{9} \end{aligned}$$

$$F_{\text{tot}} = F_{21} + F_{32} + F_{q_2}$$

$$= k \frac{q_1 q_2}{16} \hat{j} + k \frac{q_1 q_2}{25} + k \frac{q_1 q_2}{9} \hat{i}$$

b. Medan listrik q_1
 Medan q_{21} $r = 4$

$$E_{q_{21}} = k \frac{q_1}{r_{21}^2} \hat{r}_{21}$$

$$= k \frac{q_1}{4^2} \hat{i}$$

$$= k \frac{q_1}{16} \hat{i}$$

Medan q_{23} $r = 5$ atau $\sqrt{3^2 + 4^2}$

$$E_{q_{23}} = k \frac{q_3}{r_{23}^2} \hat{r}_{23}$$

$$= k \frac{q_3}{(\sqrt{3^2 + 4^2})^2} \left(\frac{3\hat{i} + 4\hat{j}}{5} \right)$$

$$= k \frac{q_3}{\sqrt{3^2 + 4^2}} \left(\frac{3\hat{i} + 4\hat{j}}{5} \right)$$

$$= k \frac{q_3}{25} \left(\frac{3\hat{i} + 4\hat{j}}{5} \right)$$

Medan q_{24} $r = 3$

$$E_{q_{24}} = k \frac{q_4}{r_{24}^2} \hat{r}_{24}$$

$$= k \frac{q_4}{3^2} \hat{i}$$

$$= k \frac{q_4}{9} \hat{i}$$

$$E_{\text{tot}} = E_{q_{21}} + E_{q_{23}} + E_{q_{24}}$$

$$= k \frac{q_1}{16} \hat{i} + k \frac{q_3}{25} \left(\frac{3\hat{i} + 4\hat{j}}{5} \right) + \frac{q_4}{9} \hat{i}$$

$$= k \left[\left(\frac{3q_3}{125} + \frac{q_4}{9} \right) \hat{i} + \left(\frac{q_1}{16} + \frac{4q_3}{125} \right) \hat{j} \right]$$

c. Potensial q_4

$$V_{q_1} = k \frac{q_1}{r_{q_1}}$$

$$= k \frac{q_1}{\sqrt{3^2 + 4^2}} (3\hat{i} + 4\hat{j})$$

$$= k \frac{q_1}{5} \left(\frac{3\hat{i} + 4\hat{j}}{5} \right)$$

$$V_{q_2} = k \frac{q_2}{r_{q_2}} \hat{r}_{q_2}$$

$$= k \frac{q_2}{3} \hat{i}$$

$$V_{q_3} = k \frac{q_3}{r_{q_3}} \hat{r}_{q_3}$$

$$= k \frac{q_3}{4} \hat{j}$$

d. Besarnya untuk usaha memindahkan muatan

$$U = k \frac{q_1 q_2}{r}$$

$$U_{12} = k \frac{q_1 q_2}{r_{12}} \hat{r}_{12} = k \frac{q_1 q_2}{4} (\hat{j})$$

$$U_{13} = k \frac{q_1 q_3}{r_{13}} \hat{r}_{13}$$

$$= k \frac{q_1 q_3}{5} \left(\frac{3\hat{i} + 4\hat{j}}{5} \right)$$

$$U_{14} = k \frac{q_1 q_4}{r_{14}} \hat{r}_{14}$$

$$= k \frac{q_1 q_4}{\sqrt{3^2 + 4^2}} \left(\frac{3\hat{i} + 4\hat{j}}{5} \right)$$

$$U_{23} = k \frac{q_2 q_3}{r_{23}} \hat{r}_{23}$$

$$= k \frac{q_2 q_3}{\sqrt{3^2 + 4^2}} (3\hat{i} + 4\hat{j})$$

$$U_{24} = k \frac{q_2 q_4}{r_{24}} \hat{r}_{24}$$

$$= k q_2 q_4 \hat{i}$$

$$U_{34} = k \frac{q_3 q_4}{r_{34}} \hat{r}_{34}$$

$$= k \frac{q_3 q_4}{9} \hat{j}$$

$$U_{\text{total}} = U_{12} + U_{13} + U_{14} + U_{23} + U_{24} + U_{34}$$

$$= k \left[\frac{q_1 q_2}{4} + \frac{3q_1 q_3}{25} + \frac{4q_1 q_4}{125} + \frac{q_2 q_4}{9} + \frac{q_2 q_3}{5} + \frac{q_3 q_4}{9} \right]$$

$$V_{\text{tot}} = V_{q_1} + V_{q_2} + V_{q_3}$$

$$= k \frac{q_1}{5} \left(\frac{3\hat{i} + 4\hat{j}}{5} \right) + k \frac{q_2}{3} \hat{i} + k \frac{q_3}{4} \hat{j}$$

$$= k \left[\left(\frac{3q_1}{25} + \frac{q_2}{3} \right) \hat{i} + \left(\frac{4q_1}{25} + \frac{q_3}{4} \right) \hat{j} \right]$$

2. Medan potensial Usaha dan energi oleh muatan kontinu.

e. Hitung medan listrik sejauh z diatas kawat lurus panjang sekali dg rapat muatan per satuan panjang λ .

f. Sebuah silinder pejal panjang sekali dengan jari-jari silinder R , rapat muatannya $\rho = kr$, hitung medan listrik $\vec{E}$ dalam ($r < R$), $\vec{E}$ permukaan ($r > R$) dan $\vec{E}$ luar silinder ($r > R$)



Permukaan Gauss

g. Hitung potensial listrik sejauh z diatas pusat lingkaran oleh muatan kontinu σ pada plat logam tipis berbentuk lingkaran dg jari-jari R

h. Sebuah bola konduktor dg muatan permukaan q , jari-jarinya R , hitung berapa energi yg tersimpan dalam bola tsb!

Jawaban.

$$\oint \vec{E} \cdot d\vec{A} = \frac{q_{in}}{\epsilon_0}$$

Rapat muatan

$$Q_{in} = \lambda \cdot L$$

$$\oint \vec{E} \cdot d\vec{A} = E(2\pi rL)$$

$$E(2\pi rL) = \frac{\lambda L}{\epsilon_0}$$

$$E = \frac{\lambda}{2\pi\epsilon_0 r} \Rightarrow E = \frac{\lambda}{2\pi\epsilon_0 z}$$

f) di dalam silinder ($r < R$)

$$\oint \vec{E} \cdot d\vec{A} = \frac{Q_{in}}{\epsilon_0} = \int \rho \, dV$$

$$E 2\pi rL = \frac{1}{\epsilon_0} \int_0^R \int_0^{2\pi} \int_0^L (kr) r \, dr \, d\phi \, dz$$

$$= \frac{2\pi kL}{\epsilon_0} \int_0^R r^2 \, dr$$

$$\vec{E} 2\pi rL = \frac{2\pi kL}{\epsilon_0} \left[\frac{1}{3} r^3 \right]_0^R$$

$$\vec{E} 2\pi rL = \frac{2\pi kL R^3}{3\epsilon_0}$$

$$E = \frac{k R^2}{3\epsilon_0}$$

di luar silinder

$$\begin{aligned} Q_{tot} &= \int_0^R \rho \, dV \\ &= \int_0^R kr(2\pi rL) \, dr \\ &= 2\pi kL \int_0^R r^2 \, dr \\ &= 2\pi kL \left[\frac{1}{3} r^3 \right]_0^R \\ &= \frac{2\pi kL R^3}{3} \end{aligned}$$

$r > R$

$$\oint \vec{E} \cdot d\vec{A} = \frac{Q_{tot}}{\epsilon_0}$$

$$\vec{E} = \frac{k R^2}{3\epsilon_0 r}$$

g. Elemen luas

$$dA = 2\pi r' dr'$$

Elemen muatan

$$da = \delta \cdot dA = \delta \cdot 2\pi r' dr'$$

jadi

$$|\vec{r} - \vec{r}'| = \sqrt{r'^2 + z^2}$$

Potensial muatan

$$dV = \frac{1}{4\pi\epsilon_0} \frac{da}{\sqrt{r'^2 + z^2}}$$

$$= \frac{\delta}{2\epsilon_0} \frac{r'}{\sqrt{r'^2 + z^2}} dr'$$

$$V(z) = \int_0^R dV$$

$$= \frac{\delta}{2\epsilon_0} \int_0^R \frac{r'}{\sqrt{r'^2 + z^2}} dr'$$

$$= \frac{\delta}{2\epsilon_0} \int_{z^2}^{R^2 + z^2} \frac{1}{2\sqrt{u}} du$$

$$= \frac{\delta}{2\epsilon_0} \int_{z^2}^{R^2 + z^2} u^{-1/2} du$$

$$= \frac{\delta}{4\epsilon_0} (2\sqrt{u})^{R^2 + z^2} = \frac{\delta}{2\epsilon_0} (\sqrt{R^2 + z^2} - z)$$

H. Energi Total

$$U = \frac{1}{2} \int \rho(\vec{r}) V(\vec{r}) d^3r$$

$$U = \frac{1}{2} qV$$

$$V = \frac{1}{4\pi\epsilon_0} \frac{q}{R}$$

maka

$$U = \frac{1}{2} q \cdot V$$

$$= \frac{1}{2} q \left(\frac{1}{4\pi\epsilon_0} \right) \cdot \frac{q}{R}$$

$$= \frac{1}{8\pi\epsilon_0} \cdot \frac{q^2}{R}$$

$$= \frac{q^2}{8\pi\epsilon_0 R}$$

$$8\pi\epsilon_0 R$$