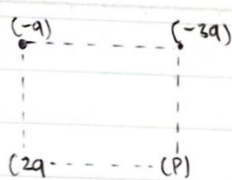


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1. a. 

Gaya-gaya : - Dari $-3q$ arah ke atas

$-q$ arah ke kiri atas (diagonal)

$2q$ arah ke kanan (karena tolak-mendorong)

b. - gaya muatan $-3q$ (jarak a)

- gaya muatan $-q$ (jarak)

$$F_1 = k_e \cdot \frac{1(-3q)q}{a^2} = \frac{3k_e q^2}{a^2}, \text{ arah ke atas}$$

$$F_3 = k_e \cdot \frac{1(-q)q}{(2a)^2} = \frac{k_e q^2}{2a^2}$$

- gaya muatan $2q$ (jarak a)

- diagonal kiri atas $\rightarrow$ ubah ke komponen

$$F_2 = k_e \cdot \frac{1(2q)q}{a^2} = \frac{2k_e q^2}{a^2}, \text{ arah ke kanan}$$

$$F_{3x} = \frac{k_e q^2}{2a^2} \cdot \cos(45^\circ) = -\frac{k_e q^2}{2a^2} \cdot \frac{\sqrt{2}}{2} = -\frac{k_e q^2 \sqrt{2}}{4a^2}$$

$$F_{3y} = \frac{k_e q^2 \sqrt{2}}{4a^2}$$

- gabungan semua gaya :

Komponen-x : $F_x = F_2 + F_{3x} = \frac{2k_e q^2}{a^2} - \frac{k_e q^2 \sqrt{2}}{4a^2}$

Komponen-y : $F_y = F_1 + F_{3y} = \frac{3k_e q^2}{a^2} + \frac{k_e q^2 \sqrt{2}}{4a^2}$

total gaya $|\vec{F}| = \sqrt{F_x^2 + F_y^2}$

c. $E_x = \frac{F_x}{q}, E_y = \frac{F_y}{q}$

d. $|\vec{E}| = \frac{|\vec{F}|}{q} = \sqrt{E_x^2 + E_y^2}$

e. $V = k_e \cdot \left(\frac{-q}{\sqrt{2}a} + \frac{-3q}{a} + \frac{2q}{a} \right)$

$$V = k_e q \left(-\frac{1}{\sqrt{2}a} - \frac{3}{a} + \frac{2}{a} \right) = k_e q \left(-\frac{1}{\sqrt{2}a} - \frac{1}{a} \right)$$

2. a. $E = \frac{\lambda}{4\pi\epsilon_0} \int_0^L \frac{1}{(z-z')^2} dz'$

batas integral :

$$z' = 0 \Rightarrow u = z$$

$$z' = L \Rightarrow u = z - L$$

substitusi $u = z - z' \Rightarrow dz' = -du$

$$E = \frac{\lambda}{4\pi\epsilon_0} \int_{z-L}^z \frac{1}{u^2} du = \frac{\lambda}{4\pi\epsilon_0} \left[-\frac{1}{u} \right]_{z-L}^z = \frac{\lambda}{4\pi\epsilon_0} \left(\frac{1}{z-L} - \frac{1}{z} \right)$$

b. $E = \frac{\lambda}{4\pi\epsilon_0} \int_{-L/2}^{L/2} \frac{1}{(z-z')^2} dz'$

substitusi $u = z - z' \Rightarrow dz' = -du$

batas : $z' = -L/2 \Rightarrow u = z + L/2$

$z' = +L/2 \Rightarrow u = z - L/2$

$$E = \frac{\lambda}{4\pi\epsilon_0} \int_{z-L/2}^{z+L/2} \frac{1}{u^2} du = \frac{\lambda}{4\pi\epsilon_0} \left[-\frac{1}{u} \right]_{z-L/2}^{z+L/2} = \frac{\lambda}{4\pi\epsilon_0} \left(\frac{1}{z-L/2} - \frac{1}{z+L/2} \right)$$

3. di dalam bola konduktor ($r < R$), medan listrik : 0

di luar bola konduktor ($r > R$), medan listrik dihitung menggunakan hukum gauss

luas permukaan bola : $A = 4\pi R^2$

total muatan Q pada bola : $Q = \sigma \cdot A = \sigma \cdot 4\pi R^2$

- medan listrik di luar bola ($r > R$) $\rightarrow$ hukum gauss

$$\oint \vec{E} \cdot d\vec{A} = \frac{Q_{\text{dalam}}}{\epsilon_0} \quad E = \frac{\sigma R^2}{\epsilon_0 r^2}$$

$$E \cdot 4\pi r^2 = \frac{\sigma \cdot 4\pi R^2}{\epsilon_0}$$

- medan listrik di dalam bola ($r < R$) } karena ini bola konduktor, seluruh muatan berada di permukaan
 @ dalam : $0 \rightarrow E = 0$ } maka tidak ada muatan di dalamnya

Jadi $E(r) = \begin{cases} 0 & \text{untuk } r < R \\ \frac{Q R^2}{\epsilon_0 r^2} & \text{untuk } r > R \end{cases}$

④ direkt : medan listrik : $\vec{E} = k r^3 \hat{r}$

Jawab : a. menggunakan hukum gauss

$$\nabla \cdot \vec{E} = \frac{\rho}{\epsilon_0}$$

Dalam koordinat bola, letak medan radial $\vec{E} = E(r) \hat{r}$:

$$\nabla \cdot \vec{E} = \frac{1}{r^2} \cdot \frac{d}{dr} (r^2 E(r))$$

Substitusi $E(r) = k r^3$:

$$\nabla \cdot \vec{E} = \frac{1}{r^2} \cdot \frac{d}{dr} (r^2 k r^3) = \frac{1}{r^2} \cdot \frac{d}{dr} (k r^5) = \frac{1}{r^2} \cdot 5 k r^4 = 5 k r^2$$

$$\text{rapat muatan : } \rho(r) = \epsilon_0 \nabla \cdot \vec{E} = 5 k \epsilon_0 r^2$$

$$b. Q = \int_V \rho(r) dv$$

Menggunakan volume elemen bola :

$$dv = 4\pi r^2 dr$$

$$Q = \int_0^R \rho(r) \cdot 4\pi r^2 dr = \int_0^R (5 k \epsilon_0 r^2) \cdot 4\pi r^2 dr = 20\pi k \epsilon_0 \int_0^R r^4 dr$$

$$Q = 20\pi k \epsilon_0 \cdot \left(\frac{r^5}{5} \right)_0^R = 20\pi k \epsilon_0 \cdot \frac{R^5}{5}$$

$$Q = 4\pi k \epsilon_0 R^5$$