

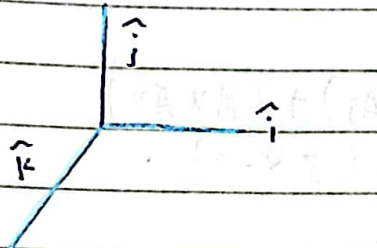
Kelistrikan dan Kemagnetan.

Vektor.

$$\vec{X} = X_1 \hat{i} + X_2 \hat{j} + X_3 \hat{k}$$

$$\vec{V} = V_1 \hat{i} + V_2 \hat{j} + V_3 \hat{k}$$

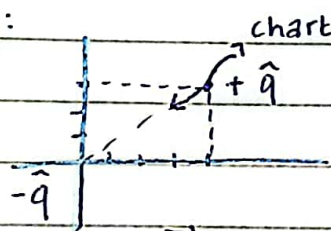
$$\begin{vmatrix} \hat{i} \cdot \hat{i} \\ \hat{j} \cdot \hat{j} \\ \hat{k} \cdot \hat{k} \end{vmatrix} = K$$



$$\hat{r} = \frac{\vec{r}}{|\vec{r}|} = \frac{X\hat{i} + Y\hat{j} + Z\hat{k}}{\sqrt{X^2 + Y^2 + Z^2}}$$

ex:

①



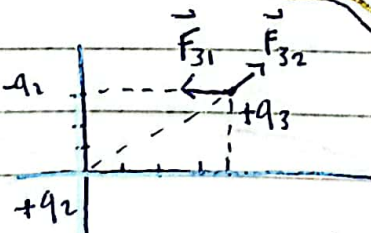
$$\vec{F}_{12} = K \frac{q_1 q_2}{r^2} \vec{r}$$

$$= K \frac{q_1 q_2}{3^2 + 4^2} \left(\frac{4\hat{i} - 3\hat{j}}{5^2} \right)$$

$$\vec{F}_{-q} = K \frac{q_1 q_2}{r^2} \vec{r}$$

$$= K \frac{q_1 q_2}{5^2} \left(\frac{4\hat{i} + 3\hat{j}}{5^2} \right)$$

②



$$\vec{F}_{q3} = \vec{F}_{31} + \vec{F}_{32}$$

$$= K q_3 \left[\frac{q_1 (-\hat{i})}{4^2} + \frac{q_2}{5^2} \left(\frac{4\hat{i} + 3\hat{j}}{5} \right) \right]$$

$$\hat{r} = \frac{-4\hat{i} + 0 + 0}{\sqrt{4^2 + 0 + 0}} = -\hat{i}$$

$$\vec{v}_1 = 4\hat{i} + 2\hat{j} + \hat{k}$$

$$\vec{v}_2 = 2\hat{j} + 3\hat{k}$$

$$\vec{v}_1 \cdot \vec{v}_2 =$$

$$A \cdot B = (A_i B_i) + (A_j B_j) + (A_k B_k)$$

$$(A_k B_k)$$

$$= (4 \times 2) + (2 \times 0) +$$

$$(1 \times 3)$$

$$= 8 + 0 + 3$$

$$= 11.$$

$$\vec{a} = 3\hat{i} + 4\hat{j} - 3\hat{k}$$

$$\vec{b} = 2\hat{i} - 3\hat{j} + 2\hat{k}$$

a) $\vec{a} \cdot \vec{a}$

b) $\vec{a} \times \vec{b}$

c) $\vec{a} \cdot \vec{b}$

Jawab:

$$\begin{aligned} \text{a) } \vec{a} \cdot \vec{a} &= (A_i \times A_i) + (A_j \times A_j) + (A_k \times A_k) \\ &= (3 \times 3) + (4 \times 4) + (-3 \times -3) \\ &= 9 + 16 + 9 = 34. \end{aligned}$$

$$\text{b) } \vec{a} \times \vec{b} = \begin{vmatrix} \hat{i} & \hat{j} & \hat{k} \\ 3 & 4 & -3 \\ 2 & -3 & 2 \end{vmatrix} =$$

$$\begin{aligned} \text{c) } \vec{a} \cdot \vec{b} &= (A_i B_i) + (A_j B_j) + (A_k B_k) \\ &= (3 \times 2) + (4 \times -3) + (-3 \times 2) \\ &= 6 - 12 - 6 \\ &= -12 \end{aligned}$$

$$\begin{aligned} \vec{b} &= \hat{i} (8+9) + \hat{j} (6+6) + \hat{k} (-9-8) \\ &= 17\hat{i} + 12\hat{j} - 17\hat{k} \end{aligned}$$

$$\vec{a} = 4\hat{i} - 5\hat{j} + \hat{k}$$

$$\vec{b} = 2\hat{i} + 3\hat{j} - 2\hat{k}$$

$$\begin{aligned} \vec{a} \times \vec{b} &= \begin{vmatrix} \hat{i} & \hat{j} & \hat{k} \\ 4 & -5 & 1 \\ 2 & 3 & -2 \end{vmatrix} = \hat{i} (10+3) + \hat{j} (-8+2) + \hat{k} (12-10) \\ &= 13\hat{i} - 6\hat{j} + 2\hat{k} \end{aligned}$$