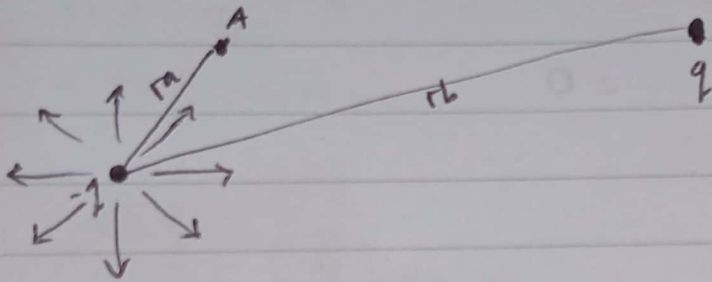


Elektrik dan Kemagnetan.

USAHA DAN ENERGI

• Usaha oleh muatan titik q



$$W = \int - \vec{F} d\vec{r}$$

(-) negatif karena melawan muatan sumber

$$W = \int_A^B \vec{F} d\vec{r}$$

$$= -q \int \vec{E} d\vec{r}$$

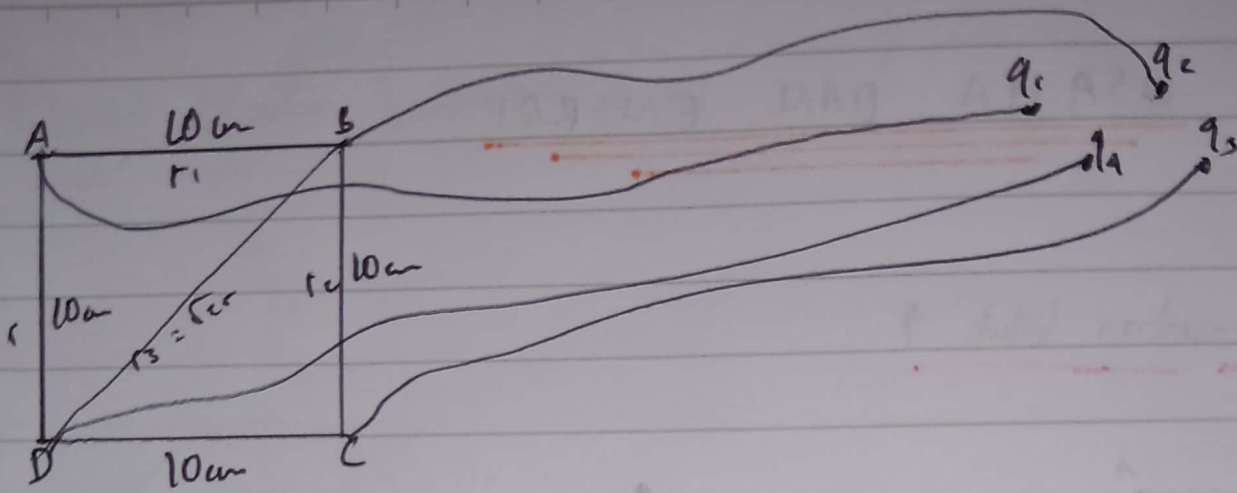
$$= -q \left[\int \frac{1}{4\pi\epsilon_0} - \frac{1}{r^2} dr \right]$$

$$= -q \left[- \frac{1}{4\pi\epsilon_0 r} \right]$$

↳ ganti q

$$= Q [V]$$

$$= QV$$



Dikak : q_1 pindah ke A = 0

q_2 — | — B

q_3 — | — C

q_4 — | — D

Muatan = 2 μC

Pajanan = 10 cm

Jawab:

$$W_1 = q_1 V_1 = 0 \quad (\text{karena belum ada muatan}).$$

$$\begin{aligned} W_2 &= q_2 V_2 \\ &= q_2 \left[k \frac{q_1}{r} \right] \\ &= q_2 V_2 \end{aligned}$$

$$\begin{aligned} W_3 &= q_3 V_3 \\ &= q_3 \left[k \frac{q_1}{r_1} + k \frac{q_2}{r_2} \right] \end{aligned}$$

$$\begin{aligned} W_4 &= q_4 V_4 \\ &= q_4 \left[k \frac{q_1}{r_1} + k \frac{q_2}{r_2} + k \frac{q_3}{r_3} \right] \end{aligned}$$

$$W = \frac{1}{4 \pi \epsilon_0} \sum_{i=1}^n \sum_{j \neq i}^n \frac{q_i q_j}{r_{ij}}$$

$$W_1 = 0$$

$$\begin{aligned} W_2 &= V_2 \cdot q_2 \\ &= k \frac{q_1}{r_{ab}} \cdot q_2 \\ &= 1 \cdot \frac{2}{10} \cdot 2 \\ &= 0.4 \text{ dyne-cm} \end{aligned}$$

$$\begin{aligned} W_3 &= V_3 q_3 \\ &= \left(k \frac{q_1}{r_{ac}} + k \frac{q_2}{r_{bc}} \right) q_3 \\ &= \left(1 \cdot \frac{2}{10} + 1 \cdot \frac{2}{10\sqrt{2}} \right) 2 \\ &= 0.683 \text{ dyne-cm} \end{aligned}$$

$$\begin{aligned} W_4 &= V_4 \cdot q_4 \\ &= \left(k \frac{q_1}{r_{ad}} + k \frac{q_2}{bd} + k \frac{q_3}{r_{cd}} \right) q_4 \\ &= \left(1 + \frac{2}{10\sqrt{2}} + 1 \cdot \frac{2}{10} + 1 \cdot \frac{2}{10} \right) 2 \\ &= 1.08 \text{ dyne-cm} \end{aligned}$$

$$W = \frac{1}{4\pi\epsilon_0} \sum_{i=1}^n \sum_{\substack{j=1 \\ j \neq i}}^n \frac{q_i q_j}{r_{ij}}$$

$$W = \frac{1}{8\pi\epsilon_0} \sum_{i=1}^n \sum_{\substack{j=1 \\ j \neq i}}^n \frac{q_i q_j}{r_{ij}}$$

$$W = \frac{1}{2} \sum_{i=1}^n q_i V_i$$

- Energi dari muatan distribusi kontinu

Garis $\rightarrow \frac{1}{2} \int \lambda V dl$

Permukaan $\rightarrow \frac{1}{2} \int \sigma V dA$

Volume $\rightarrow \frac{1}{2} \int \rho V dV$

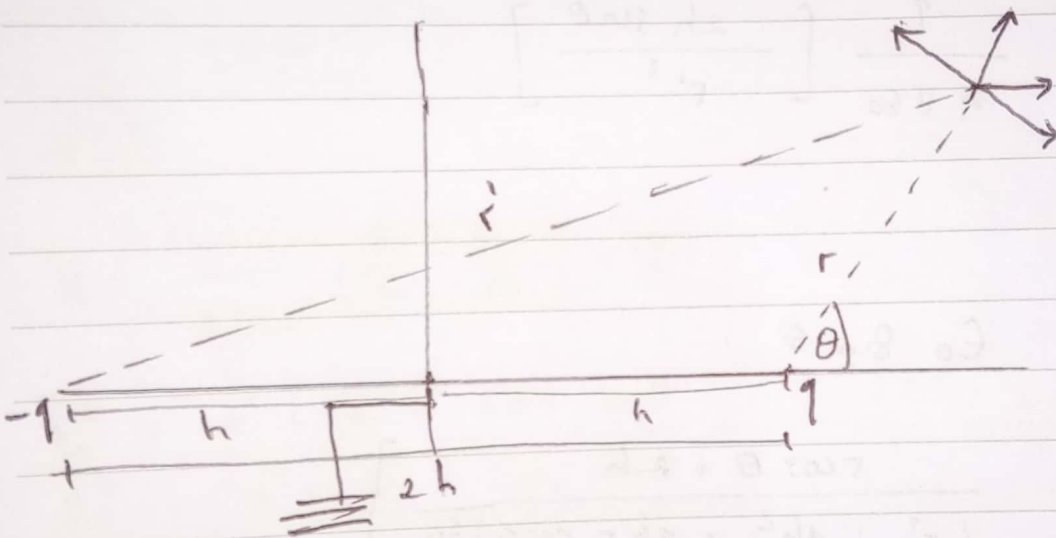
$$W = \frac{\epsilon_0}{2} \int_{\text{surface}} E^2 dA$$

Metoda Po

BAB 3. Metoda Penentuan Potensial

Metoda Bayangan

1. Muatan titik dan batang konduktor



$$P = \frac{1}{4\pi\epsilon_0} \frac{1}{r}$$

$$- \frac{q}{4\pi\epsilon_0 r'}$$

$$= \frac{1}{4\pi\epsilon_0} \left[\frac{1}{r} - \frac{1}{r'} \right]$$

$$r' = \sqrt{(2h)^2 + r^2}$$

$$= \sqrt{4h^2 + 4hr \cos \theta + r^2}$$

$$V_P = V(r, \theta) = \frac{q}{4\pi\epsilon_0} \left[\frac{1}{r} - \frac{1}{(r^2 + ah^2 + 2ahr \cos \theta)^{1/2}} \right]$$

Turunan thdp r

$$E_r = -\frac{\partial V}{\partial r} = \frac{1}{4\pi\epsilon_0} \left[\frac{1}{r^2} - \frac{r + ah \cos \theta}{r^3} \right]$$

Turunan thdp θ

$$E_\theta = -\frac{1}{r} \frac{\partial V}{\partial \theta} = \frac{1}{4\pi\epsilon_0} \left[\frac{2ah \sin \theta}{r^3} \right]$$

thdp z

$$E_z = E_r \cos \theta - E_\theta \sin \theta$$

$$= \frac{1}{4\pi\epsilon_0} \left[\frac{\cos \theta}{r^2} - \frac{r \cos \theta + ah}{(r^2 + ah^2 + 2ahr \cos \theta)^{3/2}} \right]$$

$$\text{AB, } r = r' = a$$

$$E_z = \frac{1}{4\pi\epsilon_0} \left[\frac{\cos \theta}{r^2} - \frac{r \cos \theta + ah}{(a)^3} \right]$$

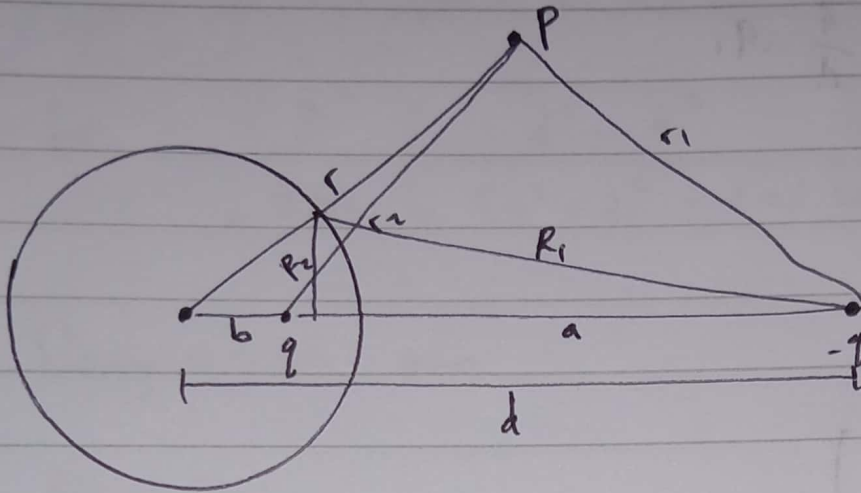
$$= \frac{-1}{4\pi\epsilon_0} \left(\frac{2h}{a^3} \right)$$

$$= \frac{-1}{2\pi\epsilon_0} \left(\frac{h}{a^3} \right) = \frac{1}{\epsilon_0} \sigma_{ca}$$

$$\begin{aligned} \iint \sigma da &= -hq \int_0^\infty \frac{x}{a^3} dx \\ &= -hq \int_h^\infty (ada) \end{aligned}$$

$$= -q \text{ muatan bayangan}$$

2. Muatan titik dengan bola konduktor



$$V = 0$$

$$V = \frac{1}{4\pi\epsilon_0} \left(\frac{q_1}{R_1} - \frac{q_2}{R_2} \right) = 0$$

$$R_1^2 = a^2 + d^2 - 2ad \cos \theta$$

$$R_2^2 = a^2 + b^2 - 2ab \cos \theta$$

Untuk $V = 0$ maka

$$\frac{q_1}{R_1} = \frac{q_2}{R_2} \rightarrow \frac{q_1^2}{R_1^2} = \frac{R_2^2}{R_1^2} = \frac{a^2 + d^2 - 2ad \cos \theta}{a^2 + b^2 - 2ab \cos \theta}$$

$$\left(\frac{q_1}{q_2} \right)^2 = \left(\frac{R_2}{R_1} \right)^2 = \frac{d}{b} \left(\frac{1/b + d - 2ad \cos \theta}{1/b + b - 2ab \cos \theta} \right)$$

$$1. \quad a^2 = db$$

$$2. \quad \left(\frac{q_1}{q_2} \right)^2 = \frac{d}{b} \quad \text{atau} \quad d > b \quad \text{dan} \quad q_1 > q_2$$

$$\frac{q_1^2}{q_2^2} = \frac{d}{b} = -q_2 = +\sqrt{\frac{b}{d}} \cdot q_1 \quad \text{untuk } b = \frac{q^2}{d}$$

$$q_2 = -\frac{q}{d} \cdot q_1$$

Jadi $V(r, \theta) = V_p$

$$V_p = \frac{1}{4\pi\epsilon_0} \left(\frac{q_1}{r_1} - \frac{q_2}{r_2} \right)$$

$$= \frac{1}{4\pi\epsilon_0} \left(\frac{q_1}{r_1} - \frac{q_1/d}{r_2} \right)$$

$$r_1 = (r^2 + d^2 - 2ard \cos \theta)^{1/2}$$

$$r_2 = (r^2 + b^2 - 2rb \cos \theta)^{1/2}$$

$$\bullet V_p = \frac{q_1}{4\pi\epsilon_0} \left(\frac{1}{(r^2 + d^2 - 2rd \cos \theta)^{1/2}} - \frac{q_1/d}{(r^2 + \frac{q^2}{d^2} - 2\frac{q}{d} \cos \theta)^{1/2}} \right)$$

$$E_r = -\frac{\partial V}{\partial r}$$

$$E_\theta = -\frac{1}{r} \frac{\partial V}{\partial \theta}$$

u/ permukaan bola $r = a$

$$E_r = -\frac{q_1}{4\pi\epsilon_0} \left[\frac{-(a - d \cos \theta)}{(a^2 + d^2 - 2ad \cos \theta)^{3/2}} + \frac{\frac{q}{d} (a - \frac{q}{d} \cos \theta)}{\left(a^2 + \frac{q^2}{d^2} - 2\frac{q}{d} \cos \theta \right)^{3/2}} \right]$$

$$+ \frac{\frac{d^2}{a} (1 - \frac{q}{d} \cos \theta)}{a^5/d^3 (r^2 + q^2 - 2ad \cos \theta)^{3/2}}$$

$$+ \frac{d^2/a (1 - \frac{q}{d} \cos \theta)}{(q^2 + d^2 - 2ad \cos \theta)^{3/2}}$$

$$E_r = -\frac{q_1}{4\pi\epsilon_0} \left[\frac{-(a - d \cos \theta) + \frac{a^2}{d} (1 - \frac{a}{d} \cos \theta)}{(a^2 + d^2 - 2ad \cos \theta)^{3/2}} \right]$$

$$\bullet E_r = -\frac{q_1}{4\pi\epsilon_0} \left(\frac{d^2 - a^2}{(a^2 + d^2 - 2ad \cos \theta)^{3/2}} \right)$$

Dengan cara sama

$$E_\theta = 0$$

Ditemukan terjadi pergerakan listrik $\rightarrow D$

$$D = \epsilon_0 E, \quad -D = \sigma_f = \sigma$$

$$\sigma = \epsilon_0 E_r$$

$$\sigma = -\frac{q_1}{4\pi a} \left(\frac{d^2 - a^2}{(a^2 + d^2 - 2ad \cos \theta)^{3/2}} \right)$$

σ = muatan induksi / satuan luas pd bola konduktor

F : Gaya antara bola dengan q_1

$$F = -\frac{1}{4\pi\epsilon_0} \frac{q_1 q_2}{(d-b)^2}$$

$$F = -\frac{1}{4\pi\epsilon_0} \frac{a q_1^2}{a(a-d)^2}$$