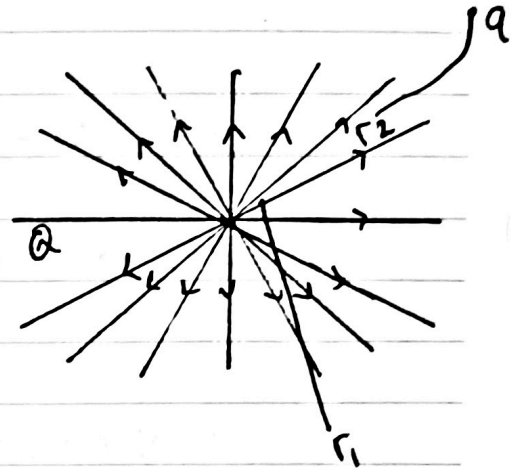
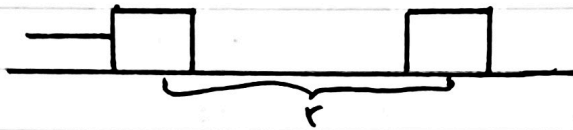


→ Usaha dalam Listrik Statis.

$$W = \int F dr \rightarrow \vec{dr}$$



$$\begin{aligned} W &= \int F dr \\ W &= -q \int E dr \\ W &= -q \left[-k \frac{Q}{r} \right] = qV \end{aligned}$$

$$W = qV$$

NOTE :

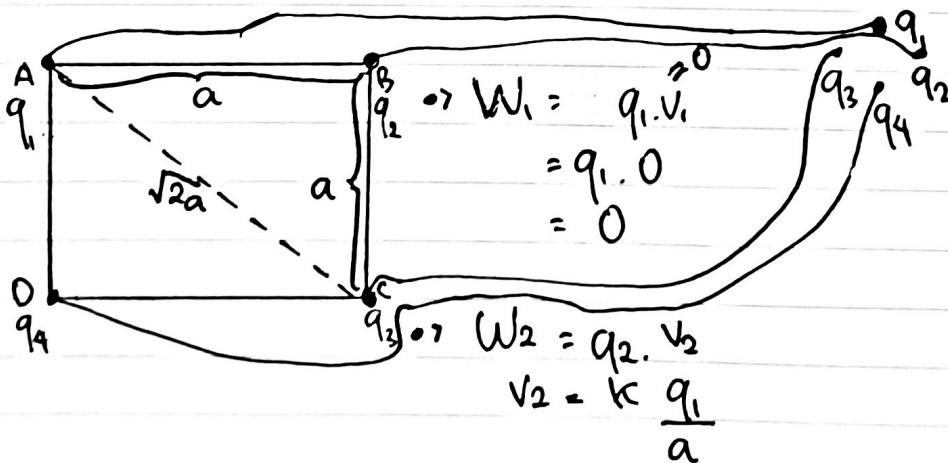
Teorema pythagoras:

$$a^2 = \sqrt{a^2 + a^2}$$

$$a = a\sqrt{2}$$

Contoh :

1.



$$\begin{aligned} \Rightarrow W_1 &= q_1 \cdot V_1 \\ &= q_1 \cdot 0 \\ &= 0 \end{aligned}$$

$$\begin{aligned} \Rightarrow W_2 &= q_2 \cdot V_2 \\ V_2 &= k \frac{q_1}{a} \end{aligned}$$

$$W_2 = k q_2 \frac{q_1}{a} = k \frac{q_1 q_2}{a}$$

$$\rightarrow W_3 = q_3 V_3$$

$$V_3 = k \frac{q_1}{\sqrt{2}a} + k \frac{q_2}{a}$$

$$W_3 = k \left[\frac{q_1 q_3}{\sqrt{2}a} + \frac{q_2 q_3}{a} \right]$$

$$\rightarrow W_4 = q_4 V_4$$

$$V_4 = k \left[\frac{q_1}{a} + \frac{q_2}{\sqrt{2}a} + \frac{q_3}{a} \right]$$

$$W_4 = k \left[\frac{q_1 q_4}{a} + \frac{q_2 q_4}{\sqrt{2}a} + \frac{q_3 q_4}{a} \right]$$

$$\rightarrow W_t = W_1 + W_2 + W_3 + W_4$$

$$W_t = \sum_{i=1}^n \sum_{j \neq i}^n q_i \frac{q_j}{4\pi\epsilon_0 r_{ij}}$$

$$W_t = \frac{1}{84\epsilon_0} \sum_{i=1}^n q_i \sum_{j \neq i}^n \frac{q_j}{r_{ij}}$$

$$W_t = \frac{1}{2} \sum_{i=1}^n q_i \sum_{j \neq i}^n \frac{1}{4\pi\epsilon_0 r_{ij}} q_j$$

$$W_t = \frac{1}{2} \sum_{i=1}^n q_i \sum_{j \neq i}^n V_j$$

$$W = \frac{1}{2} \sum_{i=1}^n q_i \sum_{j \neq i}^n V_j$$

$$\rightarrow W = \frac{1}{2} \int \lambda v d\vec{r}$$

$\Rightarrow$ potensial oleh muatan pada garis. $\rightarrow$ (lipat 1)

$$\rightarrow W = \frac{1}{2} \int \sigma v d\vec{s}$$

$\Rightarrow$ potensial oleh muatan pada permukaan. $\rightarrow$ (lipat 2)

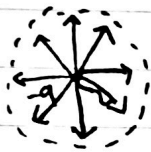
$$\rightarrow W = \frac{1}{2} \int \rho v d\sigma$$

$\Rightarrow$ potensial oleh muatan pada volume. $\rightarrow$ (lipat 3).

Persamaan Hukum Gauss dalam bentuk diferensial.

$$\rho = \epsilon_0 \cdot \nabla \cdot \vec{E}$$

$$\rightarrow \nabla \cdot \vec{E} = \frac{\rho}{\epsilon_0}$$



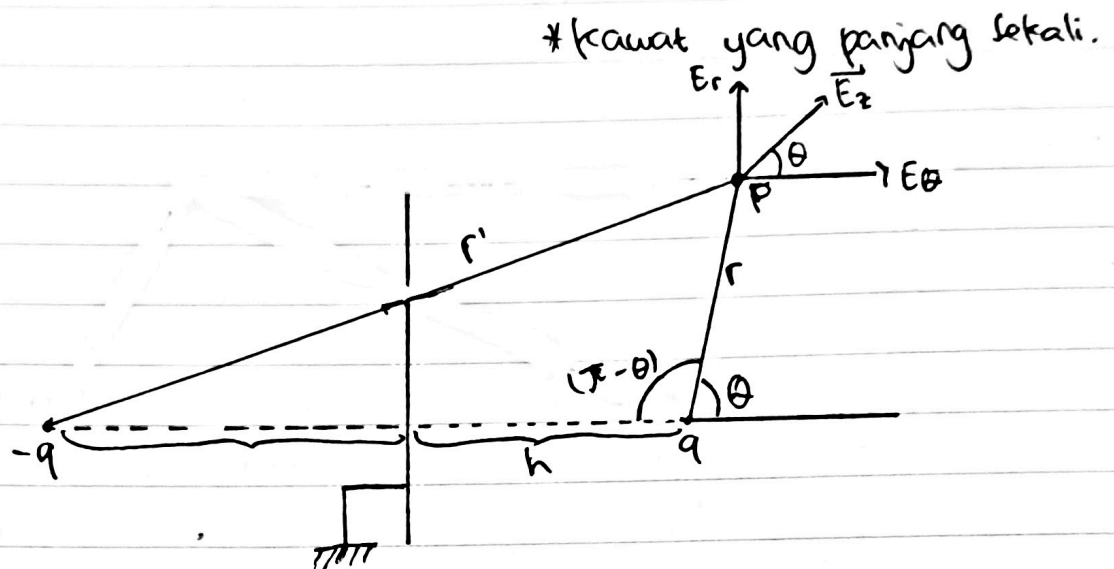
$$\oint \vec{E} d\vec{A} = \frac{Q}{\epsilon_0}$$

Sehingga,

$$W = \frac{\epsilon_0}{2} \int (\nabla \cdot \vec{E}) v d\sigma$$

$$W = \frac{\epsilon_0}{2} \int E^2 d\sigma$$

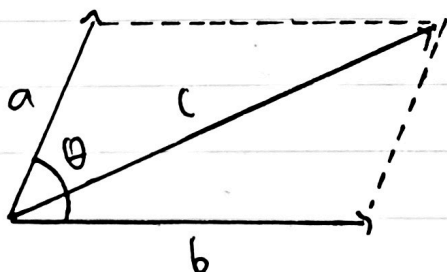
Bab III : "Metode Bayangan"



$$V = k \left[\frac{q}{r} + \frac{-q}{r'} \right]$$

$$V = kq \left[\frac{1}{r} - \frac{1}{(r^2 + (2h)^2 + 4hr \cos(\pi - \theta))^{1/2}} \right]$$

$$V = kq \left[\frac{1}{r} - \frac{1}{(r^2 + 4h^2 + 4hr \cos \theta)^{1/2}} \right]$$



$$\begin{aligned} \frac{1}{r} &= -r^{-1} dr \\ &= -r^{-1-1} \\ &= -r^{-2} = \frac{1}{r^2} \end{aligned}$$

* $\vec{E}_r = - \frac{\partial V}{\partial r}$

$$= -kq \left[\frac{1}{r^2} - \frac{-1/2 (r^2 + 4h^2 + 4hr \cos \theta)^{-1/2} (2r + h \cos \theta)}{(r^2 + 4h^2 + 4hr \cos \theta)} \right]$$

$$\begin{aligned}\vec{E}_r &= kq \left[\frac{1}{r^2} - \frac{(r+2h \cos \theta)}{(r^2+4h^2+4hr \cos \theta)^{3/2}} \right] \\ &= \frac{q}{4\pi\epsilon_0} \left[\frac{1}{r^2} - \frac{(r+2h \cos \theta)}{(r^2+4h^2+4hr \cos \theta)^{3/2}} \right]\end{aligned}$$

$$* \vec{E}_\theta = \frac{\partial V}{\partial \theta}$$

$$\begin{aligned}&= -kq \left[-\frac{1/2 (r^2+4h^2+4hr \cos \theta)^{-1/2} \cdot 4hr \sin \theta}{(r^2+4h^2+4hr \cos \theta)^1} \right] \\ &= kq \left[\frac{2hr \sin \theta}{(r^2+4h^2+4hr \cos \theta)^{3/2}} \right]\end{aligned}$$