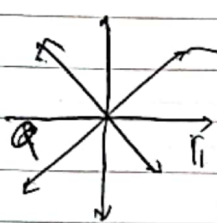


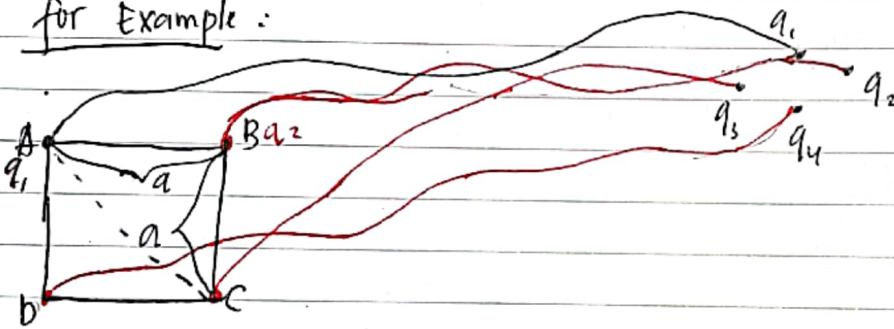
Usaha dan Energi

$$W = \int F dr$$



$$\begin{aligned} W &= \int F dr \\ &= -q \int E dr \\ &= -q \left[-k \frac{q}{r} \right] \\ &= qV \end{aligned}$$

for Example :



$$\begin{aligned} W_1 &= q_1 V_1 \\ &= 0 \end{aligned}$$

$$\begin{aligned} W_3 &= q_3 V_3 \\ V_3 &= k \frac{q_1}{\sqrt{2}a} + k \frac{q_2}{a} \end{aligned}$$

di dapat dari teorema pythagoras

$$\begin{aligned} W_2 &= q_2 V_2 \\ V_2 &= k \frac{q_1}{a} \end{aligned}$$

$$W_3 = k \left[\frac{q_1 q_3}{\sqrt{2}a} + \frac{q_2 q_3}{a} \right]$$

$$W_2 = k q_2 \frac{q_1}{a} = k \frac{q_1 q_2}{a}$$

$$\begin{aligned} W_4 &= q_4 V_4 \rightarrow V_4 = k \left[\frac{q_1}{a} + \frac{q_2}{\sqrt{2}a} + \frac{q_3}{a} \right] \\ &= k \left[\frac{q_1 q_4}{a} + \frac{q_2 q_4}{\sqrt{2}a} + \frac{q_3 q_4}{a} \right] \end{aligned}$$

$$W_{\text{total}} = W_1 + W_2 + W_3 + W_4$$

$$= \sum_{i=1}^n \sum_{j \neq i}^m \frac{q_i q_j}{4\pi\epsilon_0 r_{ij}}$$

$$= \frac{1}{8\pi\epsilon_0} \sum_{i=1}^n q_i \sum_{j \neq i}^n \frac{q_j}{r_{ij}}$$

$$= \frac{1}{2} \sum_{i=1}^n q_i \sum \frac{1}{4\pi\epsilon_0 r_{ij}}$$

$$W = \frac{1}{2} \sum_{i=1}^n q_i \sum_{j \neq i}^n V_j$$

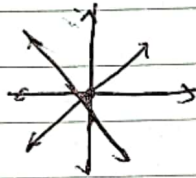
$$W = \frac{1}{2} \sum_{i=1}^n q_i \sum_{j \neq i}^n V_j$$

$$W = \frac{1}{2} \int \rho V d\tau \rightarrow \text{potensial oleh muatan pada garis}$$

$$W = \frac{1}{2} \int \sigma V dS \rightarrow \text{potensial oleh muatan pada permukaan}$$

$$W = \frac{1}{2} \int \rho V d\tau \rightarrow \text{volume}$$

$$\rho = \epsilon_0 \nabla \cdot \vec{E} \rightarrow \nabla \cdot \vec{E} = \frac{\rho}{\epsilon_0} \rightarrow \text{persamaan Hk. Gauss}$$



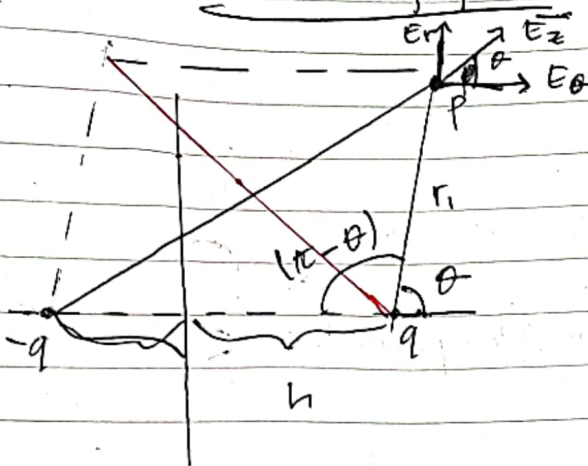
$$\oint \vec{E} \cdot d\vec{a} = \frac{Q}{\epsilon_0}$$

sehingga

$$W = \frac{\epsilon_0}{2} \int (\nabla \cdot \vec{E}) V d\tau$$

$$W = \frac{\epsilon_0}{2} \int E^2 d\tau$$

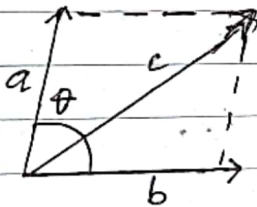
Metode Bayangan



$$V_P = K \left[\frac{q}{r} + \frac{-q}{r'} \right]$$

$$= Kq \left[\frac{1}{r} - \frac{1}{(r^2 + (2h)^2 + 4hr \cos(\pi - \theta))^{1/2}} \right]$$

$$V_P = Kq \left[\frac{1}{r} - \frac{1}{(r^2 + 4h^2 + 4hr \cos \theta)^{1/2}} \right]$$



$$\vec{E}_r = -\frac{\partial V}{\partial r}$$

$$= \frac{\partial}{\partial r} \left[\frac{1}{r} - \frac{1}{(r^2 + 4h^2 + 4hr \cos \theta)^{1/2}} \right]$$

$$= Kq \left[-\frac{1}{r^2} - \frac{-1/2 (r^2 + 4h^2 + 4hr \cos \theta)^{-3/2} (2r + 4h \cos \theta)}{(r^2 + 4h^2 + 4hr \cos \theta)^1} \right]$$

$$= Kq \left[\frac{1}{r^2} - \frac{(r + 2h \cos \theta)}{(r^2 + 4h^2 + 4hr \cos \theta)^{3/2}} \right]$$

$$\begin{aligned} E_{\theta} &= \frac{\partial V}{\partial \theta} \\ &= -Kq \left[-\frac{\frac{1}{2} (r^2 + 4h^2 + 4hr \cos \theta)^{-1/2} 2hr \sin \theta}{(r^2 + 4h^2 + 4hr \cos \theta)^{1/2}} \right] \end{aligned}$$

$$= Kq \left[\frac{2h r \sin \theta}{(r^2 + 4h^2 + 4hr \cos \theta)^{3/2}} \right]$$