

Hukum Gauss and applied

$$\oint_S \vec{E} \cdot d\vec{a} = \int_V (\nabla \cdot \vec{E}) d\tau$$

$$\oint \vec{E} \cdot d\vec{a} = \oint \frac{q}{4\pi\epsilon_0} r^2 \sin\theta d\theta d\phi$$

$$= \frac{q}{4\pi\epsilon_0} \int_0^\pi \int_0^{2\pi} \sin\theta d\theta d\phi$$

$$= \frac{4\pi q}{4\pi\epsilon_0}$$

$$\boxed{\oint_S \vec{E} \cdot d\vec{a} = \frac{q}{\epsilon_0}}$$

→ Persamaan Gauss dalam bentuk diferensial

$$\int_V (\nabla \cdot \vec{E}) d\tau$$

$$Q = \rho d\tau$$

$$\int (\nabla \cdot \vec{E}) d\tau = \left(\frac{Q}{\epsilon_0} \right)$$

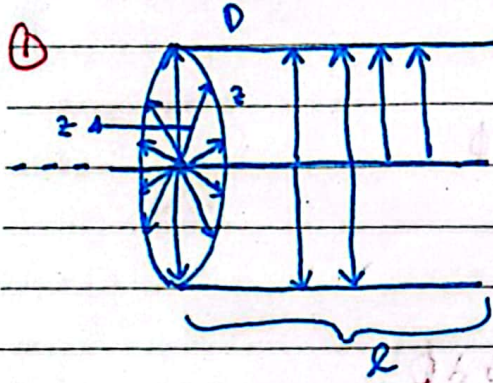
$$\rightarrow \rho d\tau$$

$$\hookrightarrow = \frac{1}{\epsilon_0} \int_V \rho d\tau$$

$$\nabla \cdot \vec{E} = \frac{\rho}{\epsilon_0}$$

→ Hukum Gauss dalam bentuk diferensial

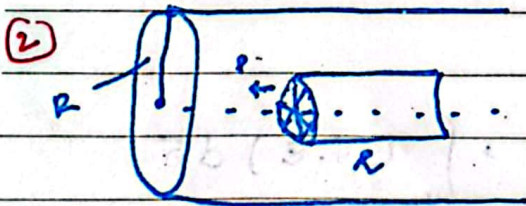
Example :



$$\oint \vec{E} \cdot d\vec{a} = \frac{q}{\epsilon_0}$$

$$\vec{E} \cdot (2\pi r \cdot 2z) = \frac{\lambda \cdot 2z}{\epsilon_0}$$

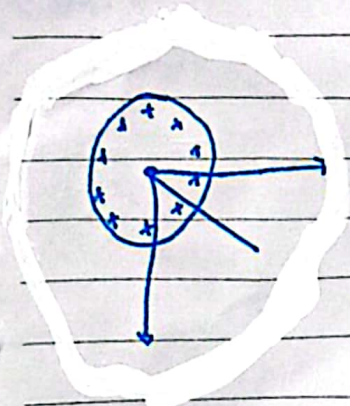
$$E = \frac{\lambda}{2\pi \epsilon_0 r}$$



$$\oint \vec{E} \cdot d\vec{a} = \frac{Q}{\epsilon_0}$$

$$E(2\pi r \cdot l) = \frac{Q}{\epsilon_0}$$

$$E = \frac{Q}{2\pi \epsilon_0 r l}$$



$$1. \vec{E} = 0$$

$$2. \oint \vec{E} \cdot d\vec{a} = \frac{Q}{\epsilon_0}$$

$$\oint \vec{E} \cdot d\vec{a}$$

$$\vec{E} \cdot (4\pi r^2) = \frac{1}{\epsilon_0} \iiint \rho d\tau$$

Calculation $\vec{E}$

$$1. r < a$$

$$2. a < r < b$$

$$3. r > b$$

$$= \frac{1}{\epsilon_0} \int_0^a \int_0^{2\pi} \int_0^\pi \rho r^2 \sin \theta d\theta d\phi dr$$

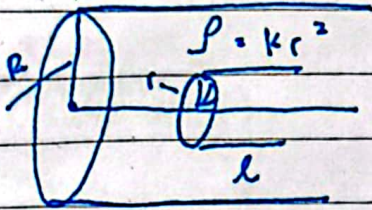
$$= \frac{4\pi\rho}{\epsilon_0} \int_0^a r^2 dr$$

$$\int_0^\pi \int_0^{2\pi} \sin \theta d\theta d\phi = 4\pi \quad \therefore \frac{4\pi\rho}{\epsilon_0} \left(\frac{1}{3} r^3 \Big|_0^a \right)$$

$$\int dx$$

$$= \int x^0 dx$$

$$= x \Big|_{\dots}$$



$$1. r < R$$

$$2. r > R$$

$$\oint \vec{E} \cdot d\vec{a} = \frac{1}{\epsilon_0} \iiint \rho d\tau$$

$$\vec{E} \cdot (2\pi r \cdot l) = \frac{1}{\epsilon_0} \int_0^l \int_0^{2\pi} \int_0^r (kr^2) r d\phi dz dr$$

$$= \frac{4\pi\epsilon_0}{\epsilon_0} \int_0^b r^2 dr$$

$$= \frac{4\pi\epsilon_0}{\epsilon_0} \left(\frac{1}{3} r^3 \Big|_0^b \right)$$

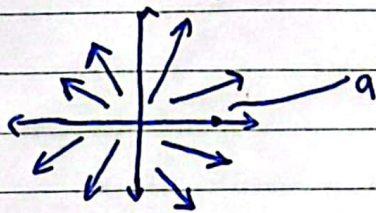
POTENSIAL LISTRIK

$$W = F \cdot s$$

$$V = \frac{W}{q} = \frac{F \cdot s}{q} = k \frac{q \cdot q}{r} s$$

$$V = k \frac{q}{r}$$

$$dV = - \int_{r_1}^{r_2} \vec{E} \cdot d\vec{r}$$



$$= - \int_{r_1}^{r_2} E \cdot dr$$

$$V_1 - V_2 = - \int_{r_2}^{r_1} \vec{E} \cdot d\vec{r}$$

$$\Delta V = - \int_{r_1}^{r_2} \frac{q}{4\pi\epsilon_0 r^2} dr$$

$$= \frac{q}{4\pi\epsilon_0} \int_{r_1}^{r_2} r^{-2} dr$$

$$\Delta V \neq dV$$

$$= - \int_{r_1}^{r_2} r^{-2} dr$$

$$= - \left[- \frac{1}{r} \right]_{r_1}^{r_2} = \left(\frac{1}{r_2} - \frac{1}{r_1} \right)$$

$$V = \frac{1}{4\pi\epsilon_0} \frac{q}{r} = k \frac{q}{r}$$