

25-Maret-2024

No
Date

"Kalisma"

"Hukum Gauss and Appurad"

Hukum Gauss dalam bentuk Integral.

$$\oint \vec{E} \cdot d\vec{A} = \int (\nabla \cdot \vec{E}) dV \quad \tau = \int$$

$$\oint \vec{E} \cdot d\vec{a} = \oint \frac{q}{4\pi\epsilon_0 r^2} \sin \theta \, dt \, d\theta$$

$$= \frac{q}{4\pi\epsilon_0} \int_0^r \int_0^\pi \sin \theta \, d\theta \, d\phi$$

$$= \frac{4\pi q}{4\pi\epsilon_0}$$

$$\boxed{\oint \vec{E} \cdot d\vec{a} = \frac{q}{\epsilon_0}} \Rightarrow \text{Persamaan Gauss dalam bentuk Integral}$$

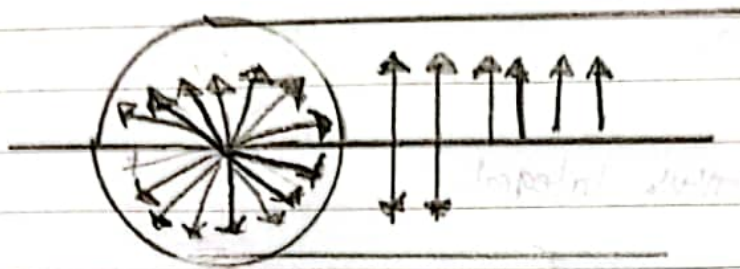
$$\int_V (\nabla \cdot \vec{E}) dV$$

$$Q = \int \rho \, dV$$

$$\int_V (\nabla \cdot \vec{E}) dV = \frac{Q}{\epsilon_0} + \int \rho \, dV$$

$$= \frac{1}{\epsilon_0} \int \rho \, dV$$

$$\boxed{\nabla \cdot \vec{E} = \frac{\rho}{\epsilon_0}} \Rightarrow \text{Hukum Gauss dalam bentuk differensial}$$



$\lambda \Rightarrow$ Rapat kawat dalam muatan

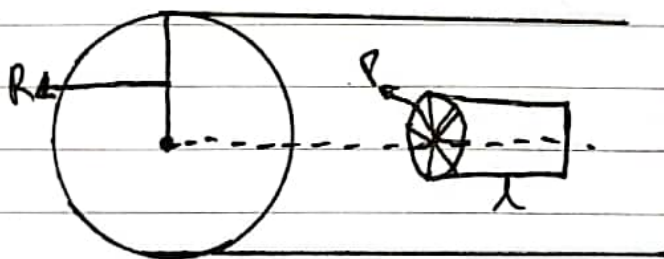
$\lambda \rightarrow$ Kecepatan dalam muatan

$$\oint \vec{E} \cdot d\vec{a} = \frac{q}{\epsilon_0}$$

$$\vec{E}(2\pi r l) = \frac{\lambda l}{\epsilon_0}$$

$$\vec{E} = \frac{\lambda}{2\pi\epsilon_0 r} \hat{r}_0$$

Example

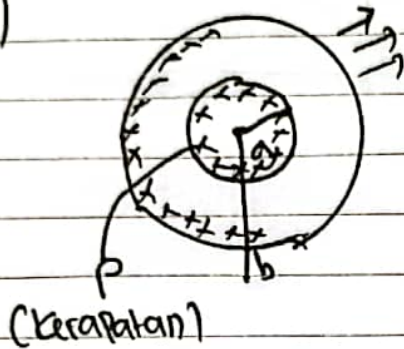


$$\oint \vec{E} \cdot d\vec{a} = \frac{Q}{\epsilon_0}$$

$$\vec{E}(2\pi r l) = \frac{Q}{\epsilon_0}$$

$$\vec{E} = \frac{Q}{2\pi\epsilon_0 r l} \hat{r}_0$$

i.)

Hitunglah $\vec{E}$

1.) $P < a \rightarrow \vec{E} = 0$

2.) $a < P < b$

3.) $P > b$

2.) $\oint \vec{E} \cdot d\vec{a} = \frac{Q}{\epsilon_0}$

$\oint \vec{E} \cdot d\vec{a}$

$$\vec{E}(4\pi r^2) = \frac{1}{\epsilon_0} \iiint \rho d\epsilon_0$$

$$= \frac{1}{\epsilon_0} \int_0^{\pi} \int_0^{2\pi} \int_0^P \rho r^2 \sin \theta d\theta d\phi dr$$

$$= \frac{4\pi\rho}{\epsilon_0} \int_0^P r^2 dr = \frac{4\pi\rho}{\epsilon_0} \left(\frac{1}{3} r^3 \Big|_0^P \right)$$

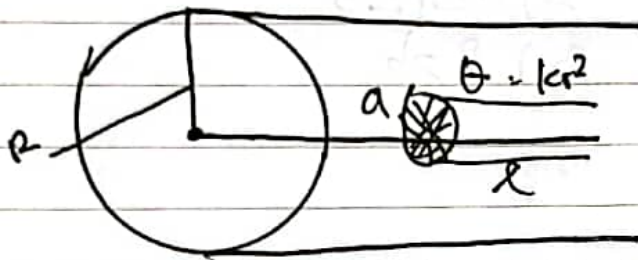
$$\int_0^{\pi} \int_0^{2\pi} \sin \theta d\theta d\phi = 4\pi$$

3.) $\oint \vec{E} \cdot d\vec{a} = \frac{1}{\epsilon_0} \iiint \rho d\epsilon_0$

$$= \frac{1}{\epsilon_0} \iiint \rho r^2 \sin \theta d\theta d\phi dr$$

$$= \frac{4\pi P}{\epsilon_0} \int_a^b p^2 dp = \frac{4\pi P}{\epsilon_0} \left(\frac{1}{3} r^3 \Big|_a^b \right)$$

Silinder dengan kerapatan



1). $P < R$

$$\oint \vec{E} \cdot d\vec{a} = \frac{1}{\epsilon_0} \iiint \rho d\epsilon_0$$

$$\vec{E} (2\pi r l) = \frac{1}{\epsilon_0} \int_0^l \int_0^{2\pi} \int_0^R (kr^2) r^2 d\phi dz dr$$

$$= \frac{2\pi k}{\epsilon_0} \int_0^l dz \int_0^R r^3 dr$$

2) $P > R$

$$\oint \vec{E} \cdot d\vec{a} =$$

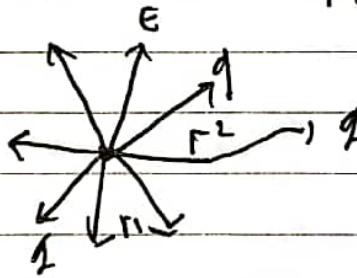
Potensial Listrik

Secara Matematis

$$W = F \cdot S$$

$$V = \frac{W}{q} = \frac{F \cdot S}{q} = \frac{k \frac{q_1 q_2}{r^2} \cdot r}{q}$$

$$V = k \frac{q}{r} \cdot dV = - \int_{r_1}^{r_2} \vec{E} \cdot d\vec{r}$$



$$V_1 - V_2 = \int_{r_1}^{r_2} \vec{E} \cdot d\vec{r}$$

$$\Delta V = - \int_{r_1}^{r_2} \frac{q}{4\pi\epsilon_0 r^2} \cdot dr$$

$$= \frac{q}{4\pi\epsilon_0} \int_{r_1}^{r_2} r^{-2} dr$$

$$\Delta V \neq dV$$

$$= -\square \int_{r_1}^{r_2} r^{-2} dr$$

$$= -\square \left(-\frac{1}{r} \Big|_{r_1}^{r_2} \right) = \square \left(\frac{1}{r_2} - \frac{1}{r_1} \right)$$

$$V = \frac{1}{4\pi\epsilon_0} \frac{q}{r} = k \frac{q}{r}$$