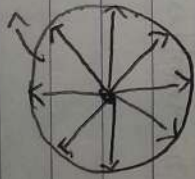


Catatan

Hukum Gauss dan aplikasi

$$\oint_S \vec{E} \cdot d\vec{A} = \int_V (\nabla \cdot \vec{E}) dV$$

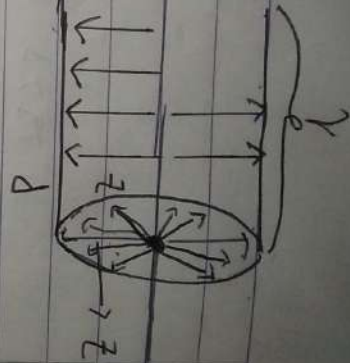


$$\begin{aligned} \oint_S \vec{E} \cdot d\vec{A} &= \oint \frac{q}{4\pi\epsilon_0} \frac{1}{r^2} \sin\theta \, r^2 \sin\theta \, d\theta \, d\phi \\ &= \frac{q}{4\pi\epsilon_0} \int_0^\pi \int_0^{2\pi} \sin\theta \, d\theta \, d\phi \\ &= 4\pi q \end{aligned}$$

$$\oint_S \vec{E} \cdot d\vec{A} = \frac{q}{\epsilon_0} \quad \rightarrow \text{Persamaan Gauss dalam bentuk Integral}$$

$$\begin{aligned} \int_V (\nabla \cdot \vec{E}) dV &= \int_V \left(\frac{\rho}{\epsilon_0} \right) dV \rightarrow \rho dV \\ Q &= \int_V \rho dV \end{aligned}$$

$$\oint_S \vec{E} \cdot d\vec{A} = (\nabla \cdot \vec{E}) dV \quad \nabla \cdot \vec{E} = \frac{1}{\epsilon_0} \rho \quad \text{Persamaan Gauss dalam bentuk diferensial}$$



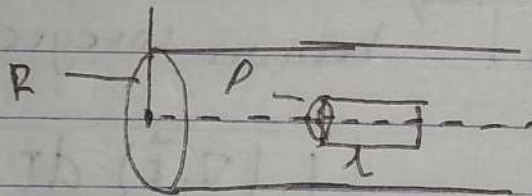
$$\oint \vec{E} \cdot d\vec{A} = \frac{q}{\epsilon_0}$$

$$\vec{E} \cdot (2\pi R \cdot l) = \frac{\lambda \cdot l}{\epsilon_0}$$

$$\vec{E} = \frac{\lambda}{2\pi \epsilon_0 R}$$

Solusi:

Langkah 1: Menampilkan atau menggambarakan Model di keramu



$$\oint \vec{E} \cdot d\vec{A} = \frac{q}{\epsilon_0}$$

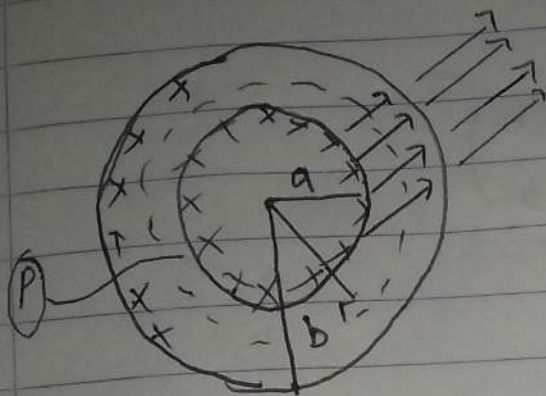
$$\vec{E} (2\pi r \cdot l) = \frac{q}{\epsilon_0}$$

$$\vec{E} = \frac{Q}{2\pi \epsilon_0 r l}, \text{ dimana } r < R$$

Pada $r = R$,

$$\text{Maka } \vec{E} (2\pi R l) = \frac{q}{\epsilon_0}$$

sehingga $\vec{E} = \frac{q}{4\pi\epsilon_0 R^2} \hat{r}_0$



Medan listrik.

- 1). ~~$r < a$~~ $r < a$
- 2). ~~$a < r < b$~~ $a < r < b$
- 3). ~~$r > b$~~ $r > b$

$\vec{E} = 0$

$\oint \vec{E} \cdot d\vec{A} = \frac{q}{\epsilon_0}$

$\oint \vec{E} \cdot d\vec{A}$

$\vec{E} \cdot (4\pi r^2) = \frac{1}{\epsilon_0} \iiint r \, d\tau$

$= \frac{1}{\epsilon_0} \int_0^a \int_0^{2\pi} \int_0^\pi r \cdot r^2 \sin\theta \, d\tau \, d\phi \, d\theta$

$= \frac{4\pi r}{\epsilon_0} \int_0^a r^2 \, dr$

$= \frac{4\pi r}{\epsilon_0} \left(\frac{1}{3} r^3 \Big|_0^a \right)$

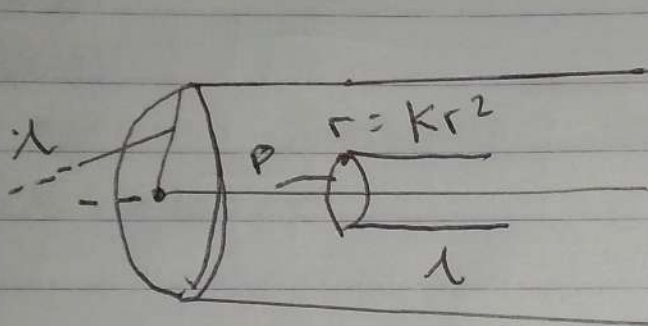
$r > b$

$\oint \vec{E} \cdot d\vec{A} = \frac{1}{\epsilon_0} \iiint r \, d\tau$

$$= \frac{1}{\epsilon_0} \iiint r \epsilon^2 \sin \theta d\theta d\tau d\phi$$

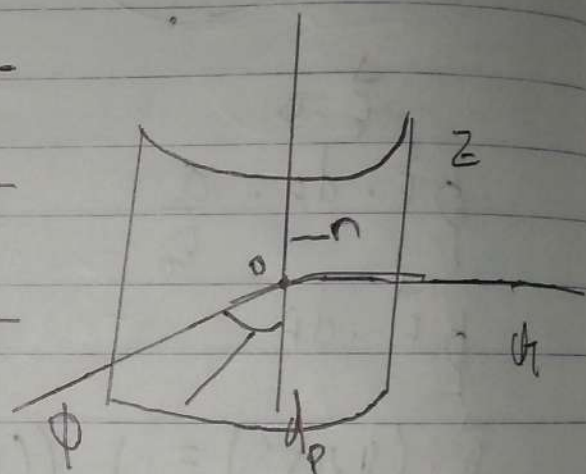
$$= \frac{4\pi r}{\epsilon_0} \int_a^b r^2 dr$$

$$= \frac{4\pi r^4}{\epsilon_0} \left(\frac{1}{3} r^3 \Big|_a^b \right)$$



$$1). P < R$$

$$2). P > R$$



$$\oint \vec{E} \cdot d\vec{A} = \frac{1}{\epsilon_0} \iiint \rho d\tau$$

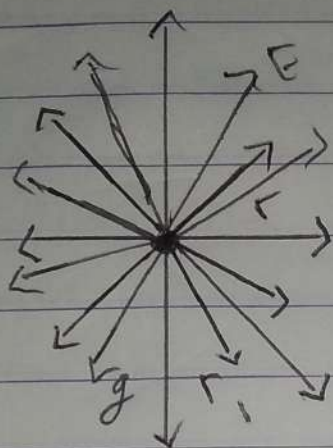
$$\vec{E} (2\pi r \cdot l) = \frac{1}{\epsilon_0} \iiint (Kr)^2 \rho^2 \sin \theta d\theta d\phi d\tau$$

$$= \frac{K (2\pi r)}{\epsilon_0} \int_0^a \rho^4 d\tau$$

$$W = F \cdot S$$

$$V = \frac{W}{g} = \frac{F \cdot S}{g} = K \frac{g \cdot g}{\rho \cdot S} \cdot S$$

$$V = \frac{\partial}{r}$$



$$dV = - \int_{r_1}^{r_2} \vec{E} \cdot d\vec{r}$$

$$= - \int P_1$$

$$V_1 - V_2 = P \int_{r_1}^{r_2} \vec{E}$$

$$\Delta V = - \int_{r_1}^{r_2} \frac{q}{4\pi\epsilon_0 r^2} dr$$

$$= \frac{q}{4\pi\epsilon_0} \int_{r_1}^{r_2} r^{-2} dr$$

$$\Delta V \neq dV$$

$$= - \int_{r_1}^{r_2} dP$$

$$= - \left(-\frac{1}{r} \right) \Big|_{r_1}^{r_2} = \left(\frac{1}{r_2} - \frac{1}{r_1} \right)$$