

Hukum Gauss dan Aplikasi

$$\oint_S \vec{E} \cdot d\vec{a} = \oint_V (\nabla \cdot \vec{E}) d\tau$$

$$\tau = V$$

$$\oint_S \vec{E} \cdot d\vec{a} = \oint \frac{q}{4\pi\epsilon_0 r^2} r^2 \sin\theta d\theta d\phi$$

$$= \frac{q}{4\pi\epsilon_0} \int_0^\pi \int_0^\pi \sin\theta d\theta d\phi$$

$$= \frac{4\pi q}{4\pi\epsilon_0}$$

$$\oint_S \vec{E} \cdot d\vec{a} = \frac{q}{\epsilon_0}$$

Persamaan Gauss dalam bentuk diferensial

$$\int_V (\nabla \cdot \vec{E}) d\tau$$

$$Q = \rho d\tau$$

$$\int_V (\nabla \cdot \vec{E}) d\tau =$$

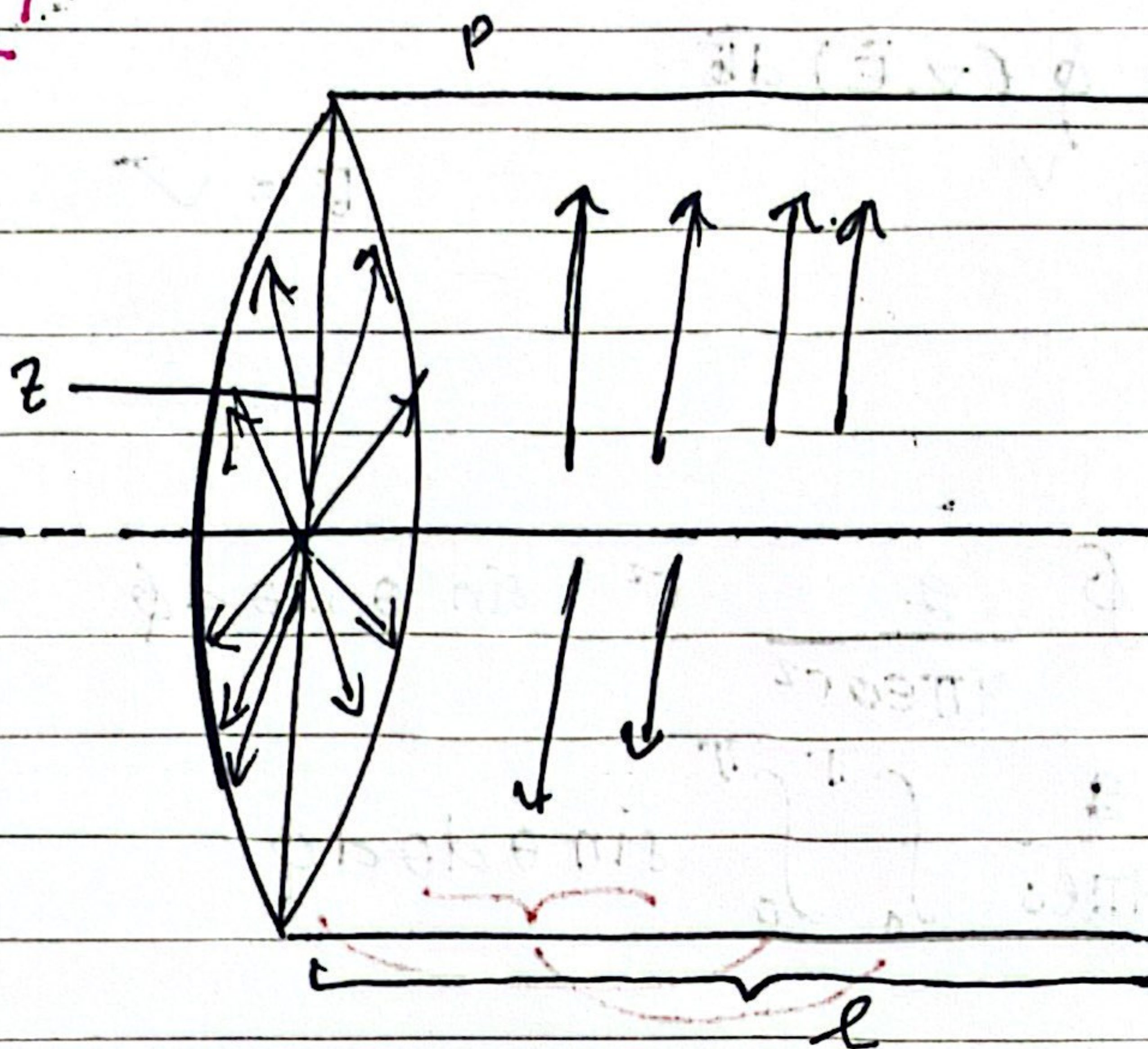
$$\frac{Q}{\epsilon_0}$$

$$= \frac{1}{\epsilon_0} \int_V \rho d\tau$$

asalinya dari $\oint_S \vec{E} \cdot d\vec{a} = \int_V (\nabla \cdot \vec{E}) d\tau$

$$\nabla \cdot \vec{E} = \frac{\rho}{\epsilon_0}$$

Hukum Gauss dalam bentuk differensial



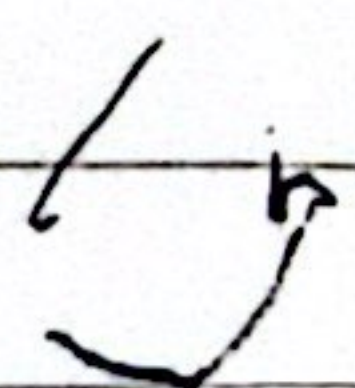
$$\oint \vec{E} \cdot d\vec{a} = \frac{q}{\epsilon_0}$$

$$\vec{E} \cdot (2\pi r \cdot l) = \frac{\lambda \cdot l}{\epsilon_0}$$

misalkan ϵ_0 dan l

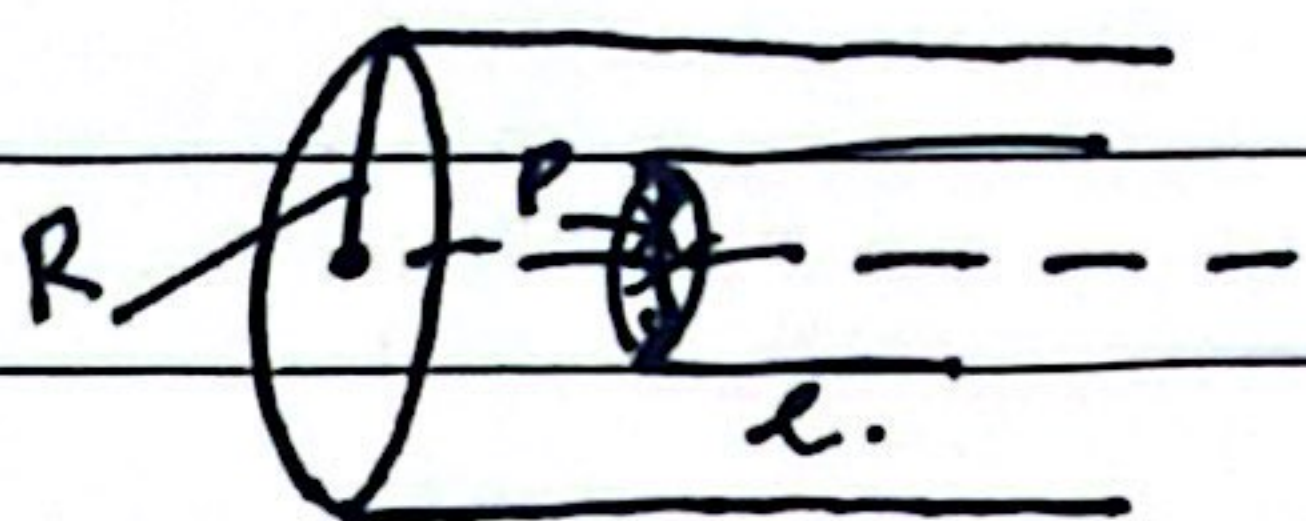
$$\vec{E} = \frac{\lambda}{2\pi\epsilon_0 r} \hat{r}_0$$

λ = rapat muatan pada kawat



latihan

no. 2 hal 61

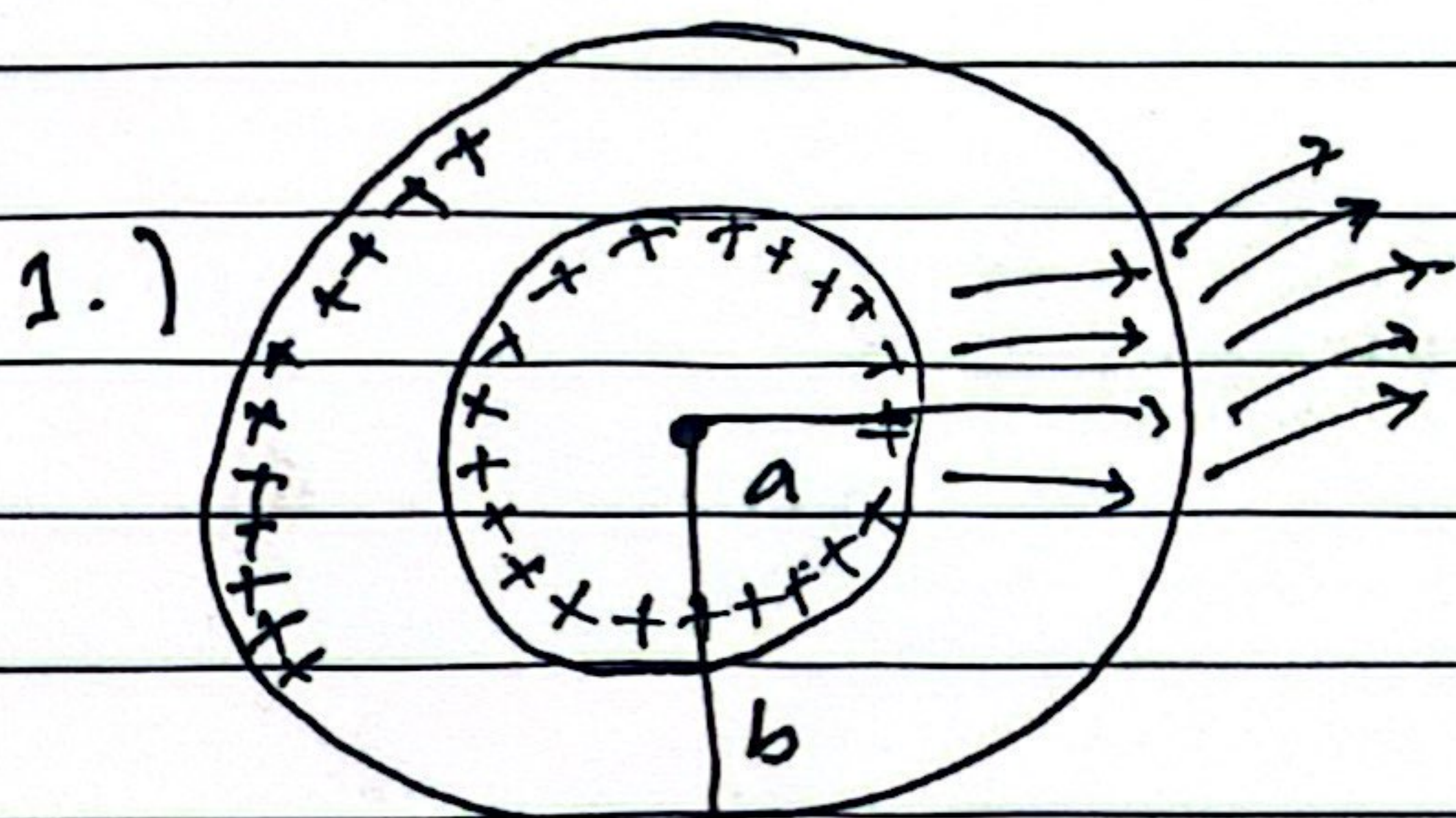


$$\oint \vec{E} \cdot d\vec{a} = \frac{Q}{\epsilon_0}$$

$$\vec{E} (2\pi r \cdot l) = \frac{Q}{\epsilon_0}$$

$$\vec{E} = \frac{Q}{2\pi \epsilon_0 r l} \hat{r}_0$$

menggunakan r kecil karena yang dihitung medan magnet berarti didalam

calculate of $\vec{E}$

1. $r < a$

2. $a < r < b$

3. $r > b$

1. $\vec{E} = 0$

2. $\oint \vec{E} \cdot d\vec{a} = \frac{Q}{\epsilon_0}$

$\oint \vec{E} \cdot d\vec{a}$

$$\vec{E} \cdot (4\pi r^2) = \frac{1}{\epsilon_0} \iiint \rho d\tau$$

$$= \frac{1}{\epsilon_0} \int_0^a \int_0^{2\pi} \int_0^\pi \rho r^2 \sin \theta d\theta d\phi dr$$

$$= \frac{4\pi \rho}{\epsilon_0} \int_0^a r^2 dr = \frac{4\pi \rho}{\epsilon_0} \left(\frac{1}{3} r^3 \Big|_0^a \right)$$

$$r > b$$

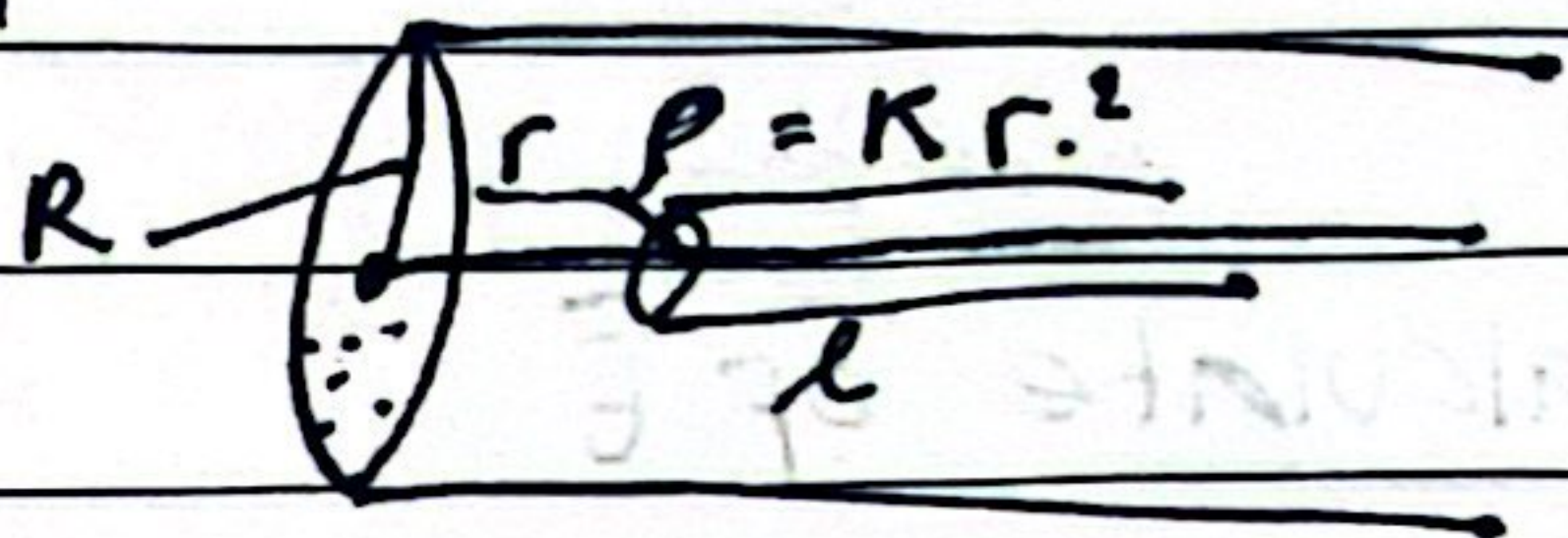
$$\oint \vec{E} \cdot d\vec{a} = \frac{1}{\epsilon_0} \iiint \rho d\tau$$

$$= \frac{1}{\epsilon_0} \iiint \rho r^2 \sin \theta d\theta d\phi dr$$

$$= \frac{4\pi\rho}{\epsilon_0} \int_a^b r^2 dr$$

$$= \frac{4\pi\rho}{\epsilon_0} \left(\frac{1}{3} r^3 \Big|_a^b \right)$$

2.)



$$1. r < R$$

$$2. r > R$$

$$\oint \vec{E} \cdot d\vec{a} = \frac{1}{\epsilon_0} \iiint \rho d\tau$$

$$\vec{E} \cdot (2\pi r \cdot l) = \frac{1}{\epsilon_0} \iiint (\pi r^2) r d\phi dz dr$$

$$= \frac{\pi(4\pi)}{\epsilon_0} \int_0^l / \frac{2\pi\pi}{\epsilon_0} \int_0^l dz \int_0^R r^3 dr$$

$$2.) \oint \vec{E} \cdot d\vec{a} = \frac{Q}{\epsilon_0}$$

$$\vec{E} \cdot (2\pi r \cdot l) = \frac{1}{\epsilon_0} \int_0^R \int_0^\pi$$

$$W = F \cdot s$$

$$V = \frac{W}{q} = \frac{F \cdot s}{q} = k \frac{q \cdot q}{r} s$$

$$s = r$$

$$V = k \frac{q}{r}$$

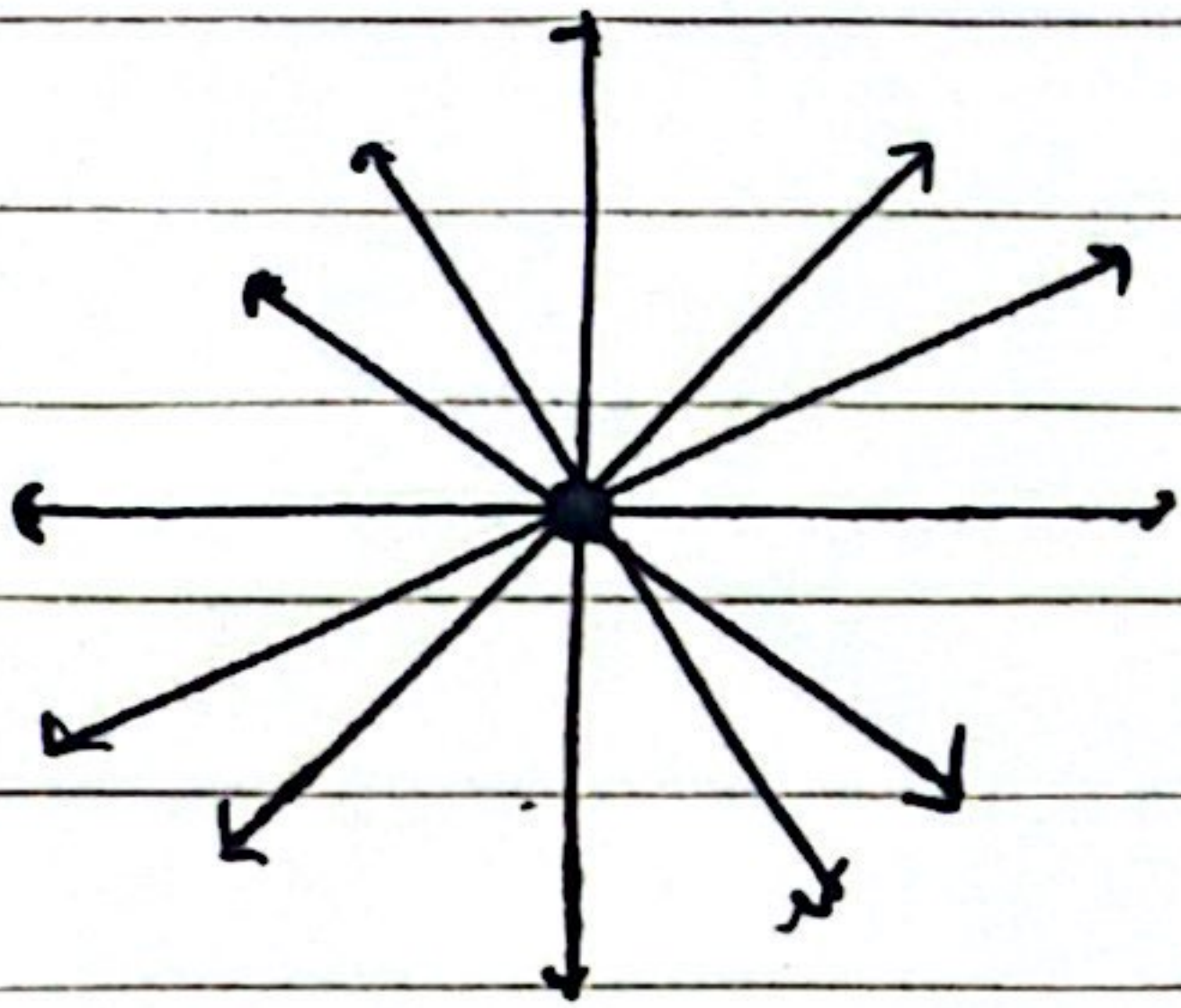
$$V = - \int \vec{E} dr$$

Potensial

> potensial oleh muatan listrik

> beda potensial oleh arus listrik

Potensial listrik (usaha memindahkan muatan dari jauh ke titik tertentu.)



$$\Delta V \neq dV$$

$$dV = - \oint_{r_1}^{r_2} \vec{E} dr$$

$$V_1 - V_2 = - \int \vec{E} dr$$

$$\Delta V = - \int_{r_1}^{r_2} \frac{Q}{4\pi\epsilon_0 r^2} dr$$

$$= \frac{Q}{4\pi\epsilon_0} \int_{r_1}^{r_2} r^{-2} dr$$

$$= \frac{Q}{4\pi\epsilon_0} \int_{r_1}^{r_2} r^{-2} dr$$

$$= \frac{Q}{4\pi\epsilon_0} \left(-\frac{1}{r} \right) \Big|_{r_1}^{r_2}$$

$$= \frac{Q}{4\pi\epsilon_0} \left(\frac{1}{r_2} - \frac{1}{r_1} \right)$$

$$V = \frac{1}{4\pi\epsilon_0} \frac{Q}{r} = k \frac{Q}{r}$$