

Hukum Gauss dan Aplikasi

$$\oint \vec{E} \cdot d\vec{a} = \int_V (\nabla \cdot \vec{E}) d\tau$$

$$\begin{aligned} \oint \vec{E} \cdot d\vec{a} &= \oint \frac{q}{4\pi\epsilon_0 r^2} r^2 \sin\theta d\theta d\phi \\ &= \frac{q}{4\pi\epsilon_0} \int_0^\pi \int_0^{2\pi} \sin\theta d\theta d\phi \\ &= \frac{4\pi q}{4\pi\epsilon_0} \end{aligned}$$

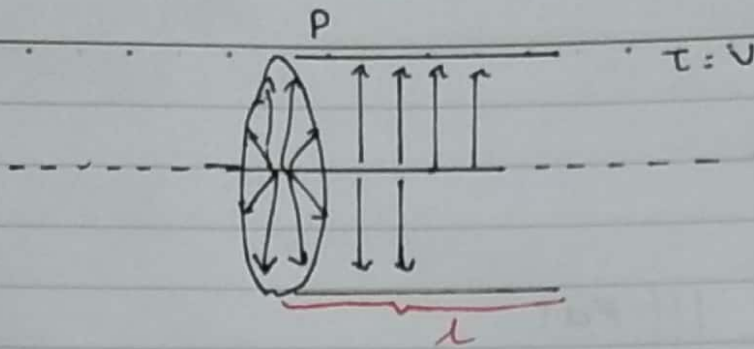
$$\boxed{\oint \vec{E} \cdot d\vec{a} = \frac{q}{\epsilon_0}} \quad \text{Persamaan Gauss dalam bentuk differensial}$$

$$\int_V (\nabla \cdot \vec{E}) d\tau$$

$$Q = \rho d\tau$$

$$\begin{aligned} \int_V (\nabla \cdot \vec{E}) d\tau &= \frac{Q}{\epsilon_0} \quad \text{asalnya dr } \oint \vec{E} \cdot d\vec{a} = \int_V (\nabla \cdot \vec{E}) d\tau \\ &= \frac{1}{\epsilon_0} \int_V \rho d\tau \end{aligned}$$

$$\boxed{\nabla \cdot \vec{E} = \frac{\rho}{\epsilon_0}} \quad \text{Hk. Gauss dalam bentuk differensial}$$



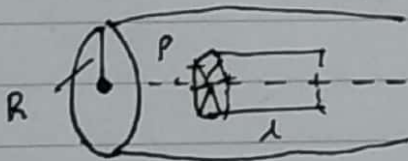
$$\oint \vec{E} \cdot d\vec{a} = \frac{q}{\epsilon_0}$$

λ = rapat muatan pada kawat

$$\vec{E} \cdot (2\pi r \cdot l) = \frac{\lambda \cdot l}{\epsilon_0}$$

$$\vec{E} = \frac{\lambda}{2\pi \epsilon_0 r} \hat{r}_0$$

latihan : no 2. hal 61



$$\oint \vec{E} \cdot d\vec{a} = \frac{q}{\epsilon_0}$$

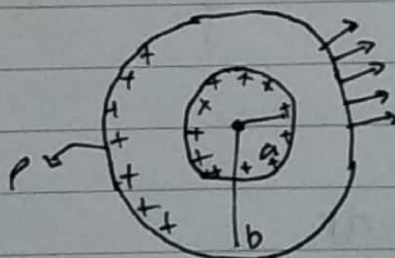
menggunakan r kecil krna yg dihitung

$$\vec{E} (2\pi r \cdot l) = \frac{Q}{\epsilon_0}$$

medan magnet brti didalam

$$\vec{E} = \frac{Q}{2\pi \epsilon_0 r l} \hat{r}_0$$

1).



Calculate of $\vec{E}$.

1. $r < a$

2. $a < r < b$

3. $r > b$.

1. $\vec{E} = 0$

2. $\oint \vec{E} \cdot d\vec{a} = \frac{Q}{\epsilon_0}$

$\oint \vec{E} \cdot d\vec{a}$

$E \cdot (4\pi r^2) = \frac{1}{\epsilon_0} \iiint \rho d\tau$

$= \frac{1}{\epsilon_0} \int_0^a \int_0^{2\pi} \int_0^\pi \rho r^2 \sin\theta d\theta d\phi dr$

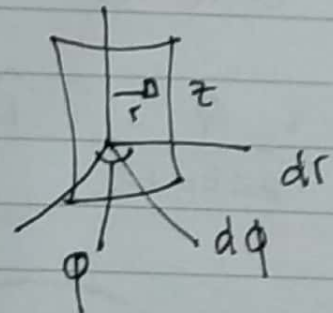
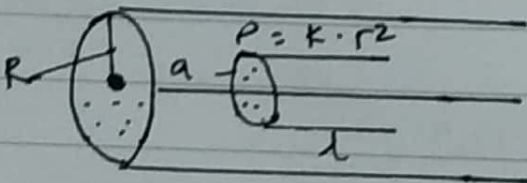
$= \frac{4\pi\rho}{\epsilon_0} \int_0^a r^2 dr = \frac{4\pi\rho}{\epsilon_0} \left(\frac{1}{3} r^3 \Big|_0^a \right)$

3. $\oint \vec{E} \cdot d\vec{a} = \frac{1}{\epsilon_0} \iiint \rho d\tau$

$= \frac{1}{\epsilon_0} \iiint \rho r^2 \sin\theta d\theta d\phi dr$

$= \frac{4\pi\rho}{\epsilon_0} \int_a^b r^2 dr$

$= \frac{4\pi\rho}{\epsilon_0} \left(\frac{1}{3} r^3 \Big|_a^b \right)$



$\oint \vec{E} \cdot d\vec{a} = \frac{1}{\epsilon_0} \iiint \rho d\tau$

$\vec{E} (2\pi r \cdot l) = \frac{1}{\epsilon_0} \int_0^{2\pi} \int_0^l \int_0^R (kr^2) r d\phi dz dr$

$$= \frac{2\pi K}{E_0} \int_0^L dz \int_0^R r^3 dr$$

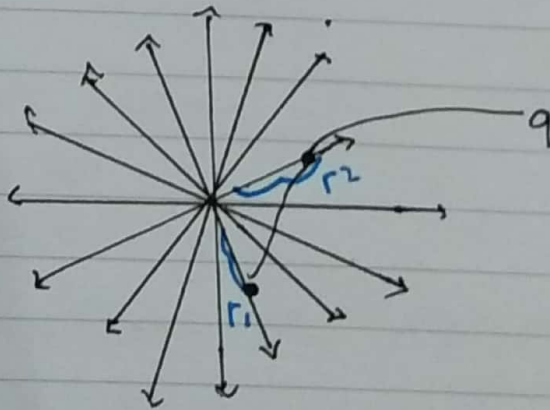
Potensial

- > Potensial oleh muatan listrik
- > beda Potensial oleh arus listrik
- > Potensial listrik (usaha memindahkan muatan dari jauh ke titik tertentu).

$$W = F \cdot S$$

$$V = \frac{W}{q} = \frac{F \cdot S}{q} = k \frac{q \cdot q}{r} \cdot \frac{1}{q}$$

$$V = k \frac{q}{r}$$



$$dv = - \oint_{r_1}^{r_2} \vec{E} \cdot d\vec{r}$$

$$V_1 - V_2 = - \int \vec{E} \cdot d\vec{r}$$

$$\Delta V = - \int_{r_1}^{r_2} \frac{q}{4\pi E_0 r^2} dr$$

$$= - \frac{q}{4\pi\epsilon_0} \int_{r_1}^{r_2} r^{-2} dr$$

$$= \square \int_{r_1}^{r_2} r^{-2} dr$$

$$= \square \left(-\frac{1}{r} \right) \Big|_{r_1}^{r_2}$$

$$= \square \left(\frac{1}{r_2} - \frac{1}{r_1} \right)$$

$$V = \frac{1}{4\pi\epsilon_0} \frac{q}{r} = k \frac{q}{r}$$