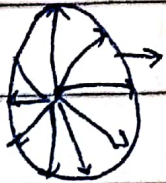


Hukum Gauss and applied

$$\oint \vec{E} \cdot d\vec{a} = \int_V (\nabla \cdot \vec{E}) dV$$



sur face of Gauss

$$\oint \vec{E} = \oint \frac{q}{4\pi \epsilon_0 r^2} \sin \theta \, d\theta \, d\phi$$

$$= \frac{q}{4\pi \epsilon_0} \int_0^\pi \int_0^{2\pi} \sin \theta \, d\theta \, d\phi$$

$$= \frac{4\pi q}{4\pi \epsilon_0}$$

$$\oint \vec{E} \cdot d\vec{a} = \frac{q}{\epsilon_0}$$

→ persamaan Gauss dalam bentuk diferensial.

$$\int (\nabla \cdot \vec{E}) dV$$

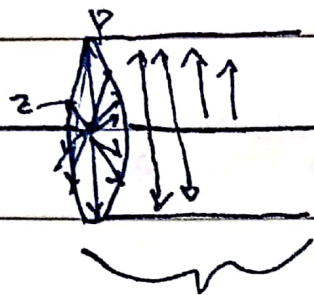
$$Q = \rho \, dV$$

$$\oint \vec{E} \cdot d\vec{a} = \int (\nabla \cdot \vec{E}) dV$$

$$\int (\nabla \cdot \vec{E}) dV = \frac{Q}{\epsilon_0}$$

$$\nabla \cdot \vec{E} = \frac{\rho}{\epsilon_0}$$

→ Hukum Gauss dalam bentuk diferensial.



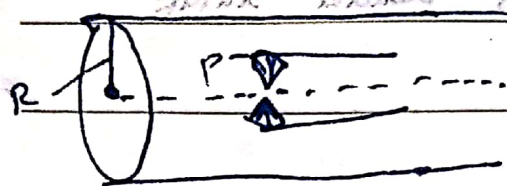
$$\vec{E} \Rightarrow \vec{V}$$

$$\oint \vec{E} \cdot d\vec{a} = \frac{q}{\epsilon_0}$$

$$E(2\pi r d) = \frac{\lambda \cdot l}{\epsilon_0}$$

$$\vec{E} = \frac{\lambda}{2\pi \epsilon_0 r} \hat{r}_0$$

Contoh:

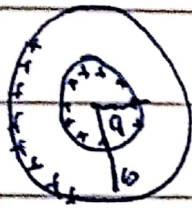


$$\oint \vec{E} \cdot d\vec{a} = \frac{Q}{\epsilon_0}$$

$$\vec{E} (2\pi r l) = \frac{Q}{\epsilon_0}$$

$$\vec{E} = \frac{Q}{2\pi r l \epsilon_0}$$

Contoh 1



calculate $\vec{E}$

~~Contoh 2~~

1 $r < a$

2 $a < r < b$

3 $r > b$

1 $\vec{E} = 0$

2 $\oint \vec{E} \cdot d\vec{a} = \frac{Q}{\epsilon_0}$

$\oint \vec{E} \cdot d\vec{a}$

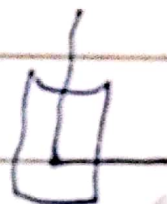
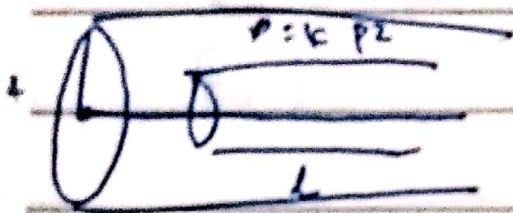
$$\vec{E} \cdot (4\pi r^2) = \frac{1}{\epsilon_0} \iiint_V \rho d\tau$$

$$= \frac{1}{\epsilon_0} \int_0^\pi \int_0^{2\pi} \int_a^b \rho r^2 \sin\theta d\theta d\phi dr$$

$$= \frac{4\pi r}{\epsilon_0} \int_a^b r^2 dr$$

$$= \frac{4\pi r}{\epsilon_0} \left[\frac{1}{3} r^3 \right]_a^b$$

$$= \frac{4\pi \rho}{\epsilon_0} \left(\frac{1}{3} r^3 \right) \Big|_a^b$$



$$\textcircled{1} r < R$$

$$\textcircled{2} r > R$$

$$\oint \vec{E} \cdot d\vec{a} = \frac{1}{\epsilon_0} \iiint_V \rho \, dV$$

$$\vec{E} (2\pi r \cdot L) = \frac{1}{\epsilon_0} \iiint_V (kr^2) r \, d\phi \, dz \, dr$$

$$= \frac{2\pi k R}{\epsilon_0} \int_0^L dz \int_0^R r^3 \, dr$$