



$$r < a \rightarrow \vec{E} = 0$$

$$a < r < b$$

$$\oint \vec{E} \cdot d\vec{a} = \frac{Q}{\epsilon_0}$$

$$E(4\pi r^2) = \frac{1}{\epsilon_0} \iiint \rho \, d\tau$$

$$\vec{E}(4\pi r^2) = \frac{1}{\epsilon_0} \int_0^a \int_0^\pi \int_0^{2\pi} r^2 \sin \theta \, d\phi \, d\theta \, dr$$

$$\vec{E}(4\pi r^2) = \frac{4\pi}{\epsilon_0} \int_0^a r^2 \, dr$$

$$\vec{E}(4\pi r^2) = \frac{4\pi}{\epsilon_0} \left[\frac{1}{3} r^3 \right]_0^a$$

$$\vec{E}(4\pi r^2) = \frac{4\pi}{\epsilon_0} \frac{a^3}{3}$$

$$E = \frac{\rho a^3}{3\epsilon_0 r^2} \hat{r}_0$$

$$\vec{E} \rightarrow \rho > b$$

$$\oint \vec{E} \cdot d\vec{a} = \frac{Q}{\epsilon_0}$$

$$\vec{E}(4\pi r^2) = \frac{1}{\epsilon_0} \int_a^b \int_0^{2\pi} \int_0^\pi \rho r^2 \sin \theta \, d\phi \, d\theta \, dr$$

$$\vec{E}(4\pi r^2) = \frac{\rho}{\epsilon_0} 4\pi \int_a^b r \, dr$$

$$\vec{E}(4\pi r^2) = \frac{\rho 4\pi}{\epsilon_0} \left(\frac{1}{3} r^3 \right) \Big|_a^b$$

$$\vec{E}(4\pi r^2) = \frac{\rho 4\pi}{3\epsilon_0} (b^3 - a^3)$$

$$\vec{E} = \frac{\rho}{3\epsilon_0 r^2} (b^3 - a^3)$$