

Senin, 25 Maret 2024.

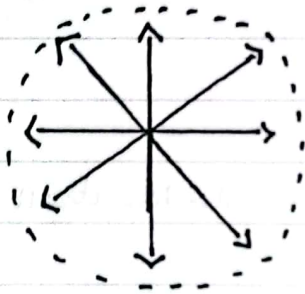
Nama: puput - Rahayu

Kelistrikan dan Kemagnetan.

Hukum Gauss

$\Delta v \neq dv$

$$\oint_S \vec{E} \cdot d\vec{a} : \int_V (\nabla \cdot \vec{E}) dG$$



$$\oint \vec{E} \cdot d\vec{a} : \oint \frac{q}{4\pi\epsilon_0 r^2} \sin \theta d\theta d\phi$$

$$: \frac{q}{4\pi\epsilon_0} \int_0^\pi \int_0^{2\pi} \sin \theta d\theta d\phi$$

$$: \frac{q(2\pi)}{4\pi\epsilon_0} \int_0^\pi \sin \theta d\theta$$

$$\oint \vec{E} \cdot d\vec{a} : \frac{4\pi q}{4\pi\epsilon_0}$$

$$\oint \vec{E} \cdot d\vec{a} : \frac{q}{\epsilon_0}$$

$$\int_V (\nabla \cdot \vec{E}) dG$$

$$Q_{\text{tot}} : \int \rho dG$$

$$: \int \sigma dA$$

$$: \int \lambda dl$$

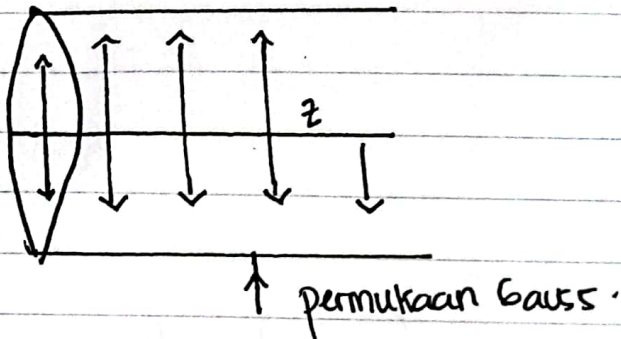
$$\iiint \nabla \cdot \vec{E} dG : \iiint \rho \cdot \frac{dG}{\epsilon_0}$$

$$\nabla \cdot \vec{E} : \frac{\rho}{\epsilon_0}$$

Differensial (Turunan)

↪ kecepatan, percepatan.

Contoh:



Gauss

Fluks yang muncul pada daerah tertentu karena ada muatan

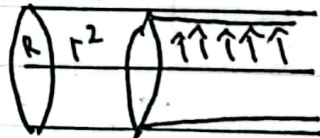
$$\oint \vec{E} \cdot d\vec{a} = \frac{q}{\epsilon_0}$$

$$\oint \vec{E} \cdot d\vec{q} = \frac{\lambda l}{\epsilon_0}$$

$$\vec{E} \cdot (2\pi r \cdot l) = \frac{\lambda l}{\epsilon_0}$$

$$\vec{E} = \frac{\lambda}{2\pi \epsilon_0 r} \hat{r}_0$$

$$\oint \vec{E} \cdot d\vec{q} = \frac{q}{\epsilon_0}$$



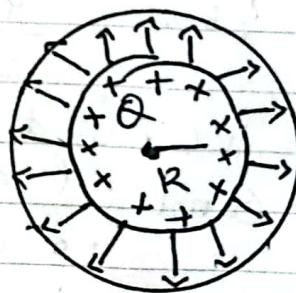
Hitung $\vec{E}$ pada

a. $r < R$

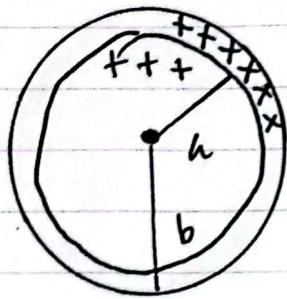
b. $r > R$

$$\oint \vec{E} \cdot d\vec{q} = \frac{Q_{inc}}{\epsilon_0}$$

$$\vec{E} (4\pi r^2) = \frac{Q_{inc}}{\epsilon_0}$$



↳ permukaan Gauss



$$r < a \rightarrow \vec{E} = 0$$

$$a < r < b$$

$$\oint \vec{E} \cdot d\vec{a} = \frac{Q}{\epsilon_0}$$

$$\int_0^\pi \int_0^{2\pi} \sin \theta \, d\theta \, d\phi$$

$$= 4\pi$$

$$E(4\pi r^2) = \frac{1}{\epsilon_0} \iiint \rho \, dV$$

$$= \frac{1}{\epsilon_0} \int_0^a \int_0^\pi \int_0^{2\pi} r^2 \sin \theta \, d\theta \, d\phi \, dr$$

$$= \frac{4\pi}{\epsilon_0} \int_0^a r^2 \, dr$$

$$\vec{E}(4\pi r^2) = \frac{4\pi}{\epsilon_0} \int_0^a r^2 \, dr$$

$$= \frac{4\pi}{\epsilon_0} \left(\frac{1}{3} r^3 \right) \Big|_0^a$$

$$\vec{E}(4\pi r^2) = \frac{4}{3} \frac{\pi r^3}{\epsilon_0} = \vec{E} \cdot \frac{\rho a^3}{3\epsilon_0 r^2}$$

$$\vec{E} \cdot (4\pi r^2) = \frac{1}{\epsilon_0} \int_a^b \int_0^{2\pi} \int_0^\pi \rho \sin \theta \, d\theta \, d\phi \, dr$$

$$\vec{E} \cdot (4\pi r^2) = \frac{\rho}{\epsilon_0} 4\pi \int_a^b r^2 \, dr$$

$$= \frac{\rho 4\pi}{\epsilon_0} \left(\frac{1}{3} r^3 \right) \Big|_a^b$$

$$= \frac{\rho \cdot 4\pi}{3\epsilon_0} (b^3 - a^3)$$

$$E = \frac{\rho}{3\epsilon_0 r^2} (b^3 - a^3)$$