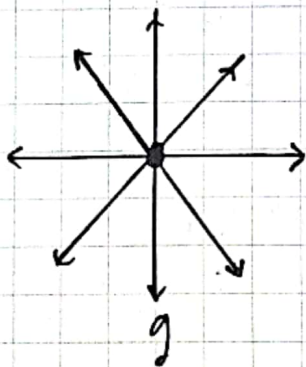


Hukum Gauss

$$\Delta v \neq dv$$

$$\oint \vec{E} \cdot d\vec{a} = \int_V (\nabla \cdot \vec{E}) dV$$



$$\oint \vec{E} \cdot d\vec{a} = \oint \frac{q}{4\pi\epsilon_0 r^2} r^2 \sin\theta d\theta d\phi$$

$$= \frac{q}{4\pi\epsilon_0} \int_0^\pi \int_0^{2\pi} \sin\theta d\theta d\phi$$

$$= \frac{q(2\pi)}{4\pi\epsilon_0} \int_0^\pi \sin\theta d\theta$$

$$= \frac{4\pi q}{4\pi\epsilon_0}$$

$$\oint \vec{E} \cdot d\vec{a} = \frac{q}{\epsilon_0}$$

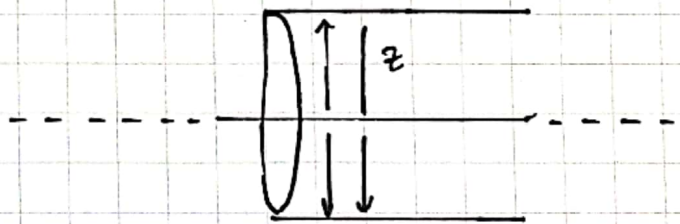
$$\int_V (\nabla \cdot \vec{E}) dV$$

$$\begin{aligned} Q_{enc} &= \rho dV \\ &= \sigma da \\ &= \lambda dp \end{aligned}$$

$$\iiint \nabla \cdot \vec{E} \cdot dV = \iiint \frac{\rho dV}{\epsilon_0}$$

$$\nabla \cdot \vec{E} = \frac{\rho}{\epsilon_0}$$

Contoh:

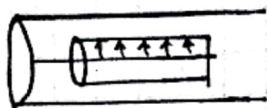


Permukaan Gauss

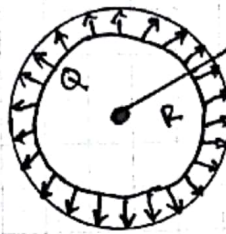
$$\oint \vec{E} \cdot d\vec{a} = \frac{q}{\epsilon_0} \quad E(2\pi r \cdot l) = \frac{N}{\epsilon_0}$$

$$\oint \vec{E} \cdot d\vec{a} = \frac{N}{\epsilon_0} \quad E = \frac{\lambda}{2\pi\epsilon_0 r} \hat{r}$$

$$\oint \vec{E} \cdot d\vec{a} = \frac{Q}{\epsilon_0}$$



$$\vec{E} = \frac{Q}{4\pi\epsilon_0 r^2} \hat{r}_0$$



Hitung E pada

- a). $r < R$
- b). $r > R$

$$\oint \vec{E} \cdot d\vec{a} = \frac{Q_{\text{enc}}}{\epsilon_0}$$

$$\vec{E} (4\pi r^2) = \frac{Q_{\text{enc}}}{\epsilon_0}$$

Medan $< a = 0 \rightarrow \vec{E}$
 $a < r < b$
 $\downarrow$
 medan

$$\oint \vec{E} \cdot d\vec{a} = \frac{Q}{\epsilon_0}$$

$$E (4\pi r^2) = \frac{1}{\epsilon_0} \iiint \rho d\tau$$

$$= \frac{1}{\epsilon_0} \int_0^a \int_0^\pi \int_0^{2\pi} r^2 \sin\theta \, d\phi \, d\theta \, dr$$

$$\vec{E} (4\pi r^2) = \frac{4\pi}{\epsilon_0} \int_0^a r^2 dr$$

$$= \frac{4\pi}{\epsilon_0} \left(\frac{1}{3} r^3 \right)_0^a$$

$$\vec{E} (4\pi r) = \frac{4\pi}{3\epsilon_0} a^3, \quad \vec{E} = \frac{a^3}{3\epsilon_0 r^2} \hat{r}$$

$\vec{E} \rightarrow r > b$

$$\oint \vec{E} \cdot d\vec{a} = \frac{Q}{\epsilon_0}$$

$$E (4\pi r^2) = \frac{1}{\epsilon_0} \int_0^b \int_0^\pi \int_0^{2\pi} \sin\theta \, d\phi \, d\theta \, dr$$

$$\left. \begin{aligned} r > b \\ E (4\pi r^2) &= \frac{\rho}{\epsilon_0} 4\pi \int_0^b r^2 dr \\ &= \frac{\rho 4\pi}{\epsilon_0} \left(\frac{1}{3} r^3 \right)_0^b \\ &= \frac{\rho 4\pi}{3\epsilon_0} (b^3 - a^3) \\ &= \frac{\rho}{3\epsilon_0 r^2} (b^3 - a^3) \end{aligned} \right\}$$