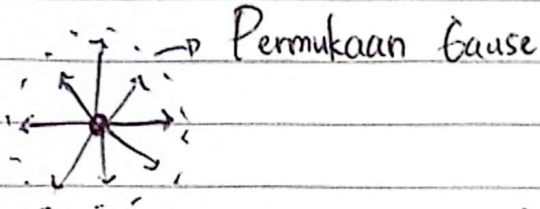


Kalisma

Integral Lipat Tiga

Medan Listrik $\rightarrow$ Simetri lingkaran (panjang banget / Bulet)

$$\Delta V \neq dV$$

$$\oint \vec{E} \cdot d\vec{a} = \int (\nabla \cdot \vec{E}) d\tau$$

$$\oint \vec{E} \cdot d\vec{a} = \oint \frac{q}{4\pi\epsilon_0 r^2} r^2 \sin \theta d\theta$$

$$= \frac{q}{4\pi\epsilon_0} \int_0^\pi \int_0^{2\pi} \sin \theta d\theta d\phi$$

$$= \frac{q(2\pi)}{4\pi\epsilon_0} \int_0^\pi \sin \theta d\theta$$

$$\oint \vec{E} \cdot d\vec{a} = \frac{4\pi q}{4\pi\epsilon_0}$$

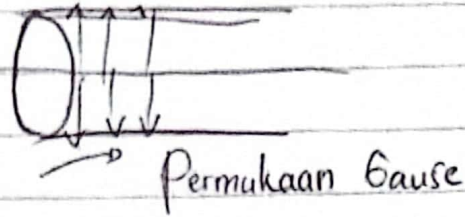
$$\vec{E} \cdot 4\pi r^2 = \frac{q}{\epsilon_0}$$

$\nabla = \text{divergensi}$
(Dari bawah ke atas - perubahan)

$$\iiint \nabla \cdot \vec{E} d\tau = \iiint \frac{\rho}{\epsilon_0} d\tau \rightarrow \boxed{\nabla \cdot \vec{E} = \frac{1}{\epsilon_0} \rho} \text{ hal. 56}$$

$$\nabla \cdot \vec{E} = \frac{\rho}{\epsilon_0}$$

Contoh soal:



$$\oint \vec{E} \cdot d\vec{a} = \frac{q}{\epsilon_0} \rightarrow \lambda L$$

$$\oint \vec{E} \cdot d\vec{a} = \frac{\lambda L}{\epsilon_0}$$

$$E (2\pi r L) = \frac{\lambda L}{\epsilon_0}$$

$$\vec{E} = \frac{\lambda}{2\pi \epsilon_0 r} \hat{r}_0$$

2. Sebuah silinder pejal panjang sekali, dengan jari-jari silinder R , rapat muatannya ρ , hitung medan listrik di dalam silinder!

(pada halaman 61)

$\vec{E}(r)$ pada $r < R$

$$\oint \vec{E} \cdot d\vec{x} = \frac{q}{\epsilon_0}$$

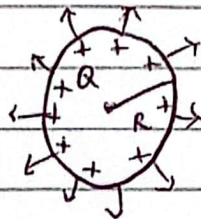
$$\vec{E}(2\pi r l) = \frac{q}{\epsilon_0}$$

$$E = \frac{q}{2\pi \epsilon_0 r l} \hat{r}_0 \quad \text{dimana } r < R$$

Pada $r = R$ maka $E(2\pi R l) = \frac{q}{\epsilon_0} R$

$$\vec{E} = \frac{q}{2\pi \epsilon_0 r l} \hat{r}_0$$

3. Bola



Hitung E pada

a. $r < R$

b. $r > R$

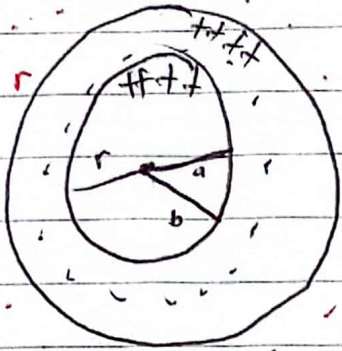
$$\oint \vec{E} \cdot d\vec{a} = \frac{Q_{\text{net}}}{\epsilon_0}$$

$$E(4\pi r^2) = \frac{Q_{\text{net}}}{\epsilon_0} \quad \vec{E} = \frac{Q}{4\pi \epsilon_0 r^2} \hat{r}_0$$

Contoh soal hal-62 dan 63

Kanan = muatan

kiri = medan



$$r < a \rightarrow \vec{E} = 0$$

$$a < r < b$$

$$\oint \vec{E} \cdot d\vec{a} = \frac{Q}{\epsilon_0}$$

$$E (4\pi r^2) = \frac{1}{\epsilon_0} \iiint \rho \, dV$$

$$\int_0^\pi \int_0^{2\pi} \sin\theta \, d\theta \, d\phi = 4\pi$$

$$= \frac{1}{\epsilon_0} \int_0^a \int_0^\pi \int_0^{2\pi} r^2 \sin\theta \, d\theta \, d\phi \, dr$$

$$= \frac{4\pi}{\epsilon_0} \int_0^a r^2 \, dr$$

$$\vec{E} (4\pi r^2) = \frac{4\pi}{\epsilon_0} \int_0^a r^2 \, dr$$

$$= \frac{4\pi}{\epsilon_0} \left(\frac{1}{3} r^3 \right) \Big|_0^a$$

$$\vec{E} (4\pi r^2) = \frac{4}{3} \frac{\pi a^3}{\epsilon_0}$$

$$\vec{E} = \frac{\rho a^3}{3\epsilon_0 r^2} \hat{r}_0$$

$$\vec{E} \rightarrow r > b$$

$$\oint \vec{E} \cdot d\vec{a} = \frac{Q}{\epsilon_0}$$

$$E (4\pi r^2) = \frac{1}{\epsilon_0} \int_a^b \int_0^\pi \int_0^{2\pi} \rho \sin\theta \, d\theta \, d\phi \, dr$$

$$\rho > b$$

$$E (4\pi r^2) = \frac{\rho}{\epsilon_0} 4\pi \int_a^b r^2 \, dr$$

$$= \frac{\rho 4\pi}{\epsilon_0} \left(\frac{1}{3} r^3 \right) \Big|_a^b$$

$$= \frac{\rho 4\pi}{3\epsilon_0} (b^3 - a^3)$$

$$\vec{E} = \frac{\rho}{3\epsilon_0 r^2} (b^3 - a^3)$$