

Hukum Gauss $\rightarrow$ fluks yang muncul pada daerah tertentu

$$\Delta V \neq dV$$

$$\oint_S \vec{E} d\vec{a} = \int_V (\nabla \cdot \vec{E}) dV$$

$$\oint \vec{E} d\vec{a} = \oint \frac{q}{4\pi\epsilon_0 r^2} r^2 \sin\theta d\theta d\phi$$

$$= \frac{q}{4\pi\epsilon_0} \int_0^\pi \int_0^{2\pi} \sin\theta d\theta d\phi$$

$$= \frac{q(2\pi)}{4\pi\epsilon_0} \int_0^\pi \sin\theta d\theta$$

$$\oint \vec{E} d\vec{a} = \frac{q(2\pi)}{4\pi\epsilon_0}$$

$$\oint \vec{E} d\vec{a} = \frac{q}{\epsilon_0}$$

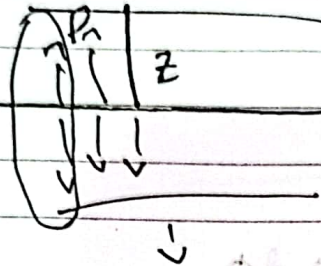
$$\int_V (\nabla \cdot \vec{E}) dV$$

$$\left. \begin{aligned} Q_{enc} &= \rho dV \\ &= \sigma da \\ &= \lambda dl \end{aligned} \right\}$$

$$\iiint \nabla \cdot \vec{E} dV = \iiint \frac{\rho dV}{\epsilon_0}$$

$$\nabla \cdot \vec{E} = \frac{\rho}{\epsilon_0}$$

Contoh



Permukaan Gauss

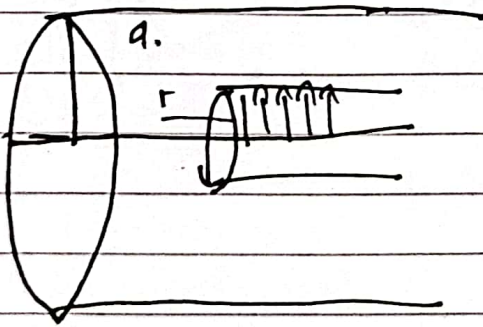
$$\oint \vec{E} \cdot d\vec{a} = \frac{q}{\epsilon_0} \quad \lambda \cdot l$$

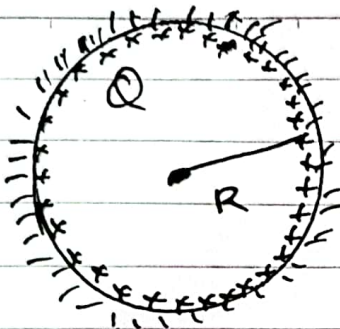
$$\vec{E}(2\pi r \cdot l) = \frac{\lambda l}{\epsilon_0}$$

$$\oint \vec{E} \cdot d\vec{a} = \frac{\lambda l}{\epsilon_0}$$

$$\vec{E} = \frac{\lambda}{2\pi\epsilon_0 r} \cdot \hat{r}_0$$

$$\oint \vec{E} \cdot d\vec{a} = \frac{q}{\epsilon_0}$$





Muatan = 0 (teoritis keluar)

Hitung $\vec{E}$ pada

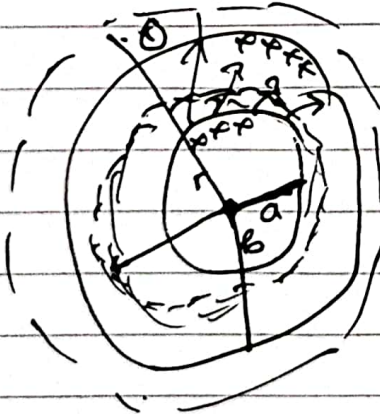
a) $r < R$

b) $r > R$

$$\oint \vec{E} \cdot d\vec{a} = \frac{Q_{enc}}{\epsilon_0}$$

$$\vec{E} (4\pi r^2) = \frac{Q_{enc}}{\epsilon_0}$$

$$\vec{E} = \frac{Q}{4\pi\epsilon_0 r^2} \hat{r}$$



$$r < a \rightarrow \vec{E} = 0$$

$$a < r < b$$

$$\oint \vec{E} \cdot d\vec{a} = \frac{Q}{\epsilon_0}$$

$$E \cdot (4\pi r^2) = \frac{1}{\epsilon_0} \iiint \rho d\tau$$

$$= \frac{\rho}{\epsilon_0} \int_0^a \int_0^\pi \int_0^{2\pi} r^2 \sin\theta d\phi dr$$

$$= \frac{\rho}{\epsilon_0} \int_0^\pi \int_0^{2\pi} \sin\theta d\theta d\phi = 4\pi$$

$$= \frac{4\pi}{\epsilon_0} \int_0^r r^2 dr$$

$$= \frac{1}{4\pi\epsilon_0 R}$$

P1

r2

q2

Tugas

Tiga buah muatan masing-masing dua muatan pada sudut yang berlawanan pada bujur sangkar pada sudut yang besarnya $-4 \mu\text{C}$ terletak pada sudut yang kosong!

No.

Date

$$\vec{E} (4\pi r^2) = \frac{4\pi}{\epsilon_0} \int_0^a r^2 dr$$

$$= \frac{4\pi}{\epsilon_0} \left(\frac{1}{3} r^3 \Big|_0^a \right)$$

$$\vec{E} (4\pi r^2) = \frac{4\pi a^3}{3 \epsilon_0}$$

$$\vec{E} = \frac{\rho a^3}{3\epsilon_0 r^2} \hat{r}$$

$$\vec{E} \rightarrow r > b$$

$$\oint \vec{E} \cdot d\vec{a} = \frac{Q}{\epsilon_0}$$

$$\vec{E} \cdot (4\pi r^2) = \frac{1}{\epsilon_0} \int_a^b \int_0^{2\pi} \int_0^\pi \rho r^2 \sin \theta d\theta d\phi dr$$

$$\vec{E} (4\pi r^2) = \frac{\rho}{\epsilon_0} 4\pi \Big|_a^b r^2 dr$$

$$= \frac{\rho 4\pi}{\epsilon_0} \left(\frac{1}{3} r^3 \Big|_a^b \right)$$

$$= \frac{\rho 4\pi}{3\epsilon_0} (b^3 - a^3)$$

$$\vec{E} = \frac{\rho}{3\epsilon_0 r^2} (b^3 - a^3)$$