

listrik & kemagnetan

$$1. \vec{E} = \frac{1}{4\pi\epsilon_0} \frac{q}{r^2} \hat{r}$$

$$= k \frac{q}{r^2} r_0^2 \rightarrow \text{oleh muatan diskrit}$$

$$2. \vec{E} = \frac{1}{4\pi\epsilon_0} \int \frac{x \, dP}{r^2} r_0^2 \rightarrow g = x \, l \rightarrow \text{muatan tes distribusi pada penggaris}$$

$$3. \vec{E} = \frac{1}{4\pi\epsilon_0} \iint \sigma \frac{dA}{r^2} \hat{r}_0^2 \quad \text{merupakan luas permukaan}$$

$$4. \vec{E} = \frac{1}{4\pi\epsilon_0} \iiint \frac{\rho \, dV}{r^2} \hat{r}_0^2$$

Contoh 1:

$$d\vec{E} = d\vec{E}_y +$$

$$d\vec{E} = d\vec{E}_y$$

$$d\vec{E}_y = dE \cos \theta$$

$$\vec{E} = \frac{1}{4\pi\epsilon_0} \int_{-L}^L \frac{x \, dl}{r^2} \cos \theta$$

$$= \frac{2}{4\pi\epsilon_0} \int_0^L \frac{x dx}{(x^2 + z^2)^{3/2}}$$

$$= \frac{2}{4\pi\epsilon_0} \int_0^L \frac{dx}{(x^2 + z^2)^{3/2}} \quad \int \frac{dx}{(x^2 + z^2)^{3/2}} = \frac{x}{z^2 \sqrt{x^2 + z^2}}$$

$$= \frac{2xz}{4\pi\epsilon_0} \left(\frac{x}{z^2 \sqrt{x^2 + z^2}} \right) \Big|_0^L$$

$$= \frac{2xz}{4\pi\epsilon_0} \left[\frac{1}{z^2 \sqrt{x^2 + z^2}} \right]_0^L$$

$$= \frac{2xz}{4\pi\epsilon_0} \left[\frac{1}{z^2 \sqrt{L^2 + z^2}} - \frac{1}{z^2 \sqrt{0 + z^2}} \right]$$

Contoh 2:

$$\vec{E} = \frac{1}{4\pi\epsilon_0} \int_0^L \frac{x dx}{(x_0 - x)^2} \quad \text{diputer & diturunkan}$$

$$= \frac{1}{4\pi\epsilon_0} x \int_0^L (x_0 - x)^{-2} dx$$

$$= \frac{1}{4\pi\epsilon_0} \left((x_0 - x)^{-1} \right) \Big|_0^L$$

$$= \frac{1}{4\pi\epsilon_0} \left(\frac{1}{(x_0 - x)} \right) \Big|_0^L$$

$$= \frac{1}{4\pi\epsilon_0} \left(\frac{1}{(x_0 - L)} - \frac{1}{(x_0 - 0)} \right)$$

untuk meroleh ini, gunakan

$$\int \frac{dx}{x^2} = \int x^{-2} dx$$

$$= 1 x^{-1} \Big|_0^L$$

$$= \frac{1}{x} \Big|_0^L$$

$$= \frac{1}{4\pi\epsilon_0} \left[\frac{x_0 - (x_0 - L)}{x_0 (x_0 - L)} \right] \quad \left. \vphantom{\frac{1}{4\pi\epsilon_0}} \right\} \text{hat rumus}$$

$$= \frac{L}{x_0 (x_0 - L)}$$

Contoh 3 :

$$\vec{E} = \frac{1}{4\pi\epsilon_0} \int_0^{2\pi R} \frac{z \lambda \, dL}{(z^2 + R^2)^{3/2}}$$

$$= \frac{z \lambda}{4\pi\epsilon_0 (z^2 + R^2)^{3/2}} (1) \bigg|_0^{2\pi R}$$

$$= \frac{z \lambda}{4\pi\epsilon_0 (z^2 + R^2)^{3/2}} \int_0^{2\pi R} dL$$

$$= \frac{z \lambda}{4\pi\epsilon_0 (z^2 + R^2)^{3/2}} \int_0^{2\pi R} dL$$

$$= \frac{z \lambda}{4\pi\epsilon_0 (z^2 + R^2)^{3/2}} L \bigg|_0^{2\pi R}$$

$$= \frac{z \lambda}{4\pi\epsilon_0 (z^2 + R^2)^{3/2}} (2\pi R - 0)$$

$$= \frac{z \lambda}{4\pi\epsilon_0 (z^2 + R^2)^{3/2}} 2\pi R$$