

FaBila Aulia Ibnu

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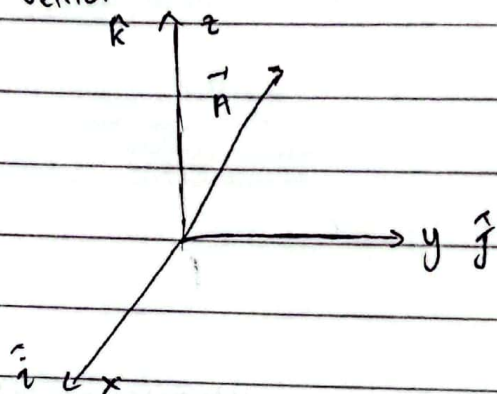
No.:

Date 22/02

Kemagnetan dan Kelistrikan

Operator dalam Fisika

Analisis Vektor



$$A = x\hat{i} + y\hat{j} + z\hat{k}$$

$$A = \frac{\vec{A}}{|\vec{A}|} = \frac{x\hat{i} + y\hat{j} + z\hat{k}}{\sqrt{x^2 + y^2 + z^2}}$$

$$\vec{A} = x^2y\hat{i} + 3yz\hat{j} + 2xy\hat{k}$$

$$\vec{B} = z\hat{i} + 2yx\hat{j} + 2xz\hat{k}$$

$$\vec{A} + \vec{B} = (x^2y + z)\hat{i} + (3yz + 2yx)\hat{j} + (2xy + 3xz)\hat{k}$$

$$\vec{A} \cdot \vec{B} = (x^2y\hat{i} + 3yz\hat{j} + 2xy\hat{k}) \cdot (z\hat{i} + 2yx\hat{j} + 2xz\hat{k})$$

$$= (x^2yz +$$

$$\vec{A} \times \vec{B} = \begin{vmatrix} \hat{i} & \hat{j} & \hat{k} \\ x^2y & 3yz & 2xy \\ z & 2yx & 3xz \end{vmatrix} = \begin{vmatrix} \hat{i} & \hat{j} \\ x^2y & 3yz \\ z & 2yx \end{vmatrix}$$

$$= [(3yz \cdot 3xz) \hat{i} + (2xy \cdot z) \hat{j} + (x^2y \cdot 2yx) \hat{k}]$$

$$- [(x^2y \cdot 3xz) \hat{j} - (2xy \cdot 2yx) \hat{i} - (3yz \cdot z) \hat{k}]$$

$$= (9xyz^2 - 4x^2y^2) \hat{i} + (2x^3y^2 - 3x^3yz) \hat{j} + (x^3 + yz^2 - 3yz^2) \hat{k}$$

Operator Nabla

$$\nabla = \hat{i} \frac{\partial}{\partial x} + \hat{j} \frac{\partial}{\partial y} + \hat{k} \frac{\partial}{\partial z}$$

$$T = x^2 yz + 3y^2 z$$

$$\nabla T = \hat{i} \frac{\partial (x^2 yz + 3y^2 z)}{\partial x} + \hat{j} \frac{\partial (x^2 yz + 3y^2 z)}{\partial y} + \hat{k} \frac{\partial (x^2 yz + 3y^2 z)}{\partial z}$$

$$= \hat{i} (2xy z + 3y^2 z) + \hat{j} (x^2 z + 6y z) + \hat{k} (x^2 y + 3y^2)$$

$$\vec{A} = 2x\hat{i} + 3y\hat{j} - 4z\hat{k}$$

$$\nabla \cdot \vec{A} = \frac{\partial V}{\partial x} + \frac{\partial V}{\partial y} + \frac{\partial V}{\partial z}$$

$$= 2 + 3 - 4$$

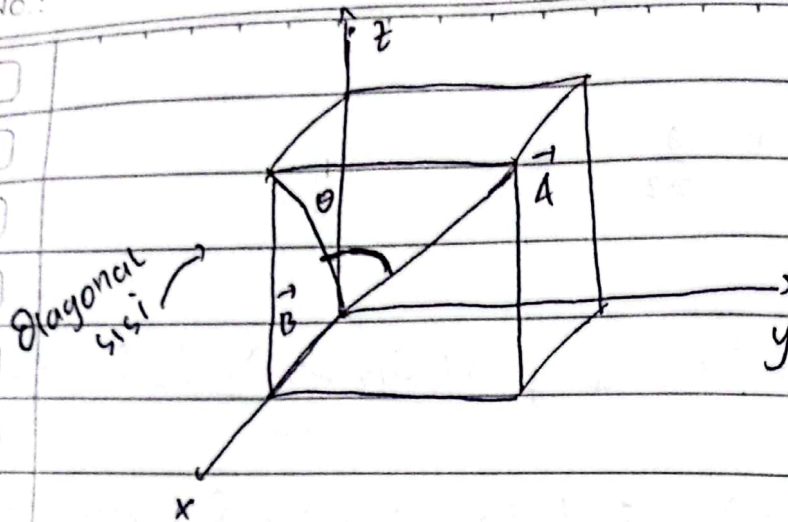
$$= 1$$

$$\nabla \times \vec{A} = \begin{vmatrix} \hat{i} & \hat{j} & \hat{k} \\ \frac{\partial}{\partial x} & \frac{\partial}{\partial y} & \frac{\partial}{\partial z} \\ 2x & 3y & 4z \end{vmatrix} = \begin{vmatrix} \hat{i} & \hat{j} \\ \frac{\partial}{\partial x} & \frac{\partial}{\partial z} \\ 2x & 4z \end{vmatrix} - \begin{vmatrix} \hat{i} & \hat{k} \\ \frac{\partial}{\partial y} & \frac{\partial}{\partial z} \\ 3y & 4z \end{vmatrix} + \begin{vmatrix} \hat{j} & \hat{k} \\ \frac{\partial}{\partial x} & \frac{\partial}{\partial y} \\ 2x & 3y \end{vmatrix}$$

$$= \left(\left(\frac{\partial}{\partial y} \cdot 4z \right) \hat{i} + \left(\frac{\partial}{\partial z} \cdot 2x \right) \hat{j} + \left(\frac{\partial}{\partial x} \cdot 4z \right) \hat{k} \right)$$

$$= \left(\frac{\partial}{\partial x} \cdot 4z \right) \hat{j} - \left(\frac{\partial}{\partial z} \cdot 3y \right) \hat{i} + \left(\frac{\partial}{\partial y} \cdot 2x \right) \hat{k}$$

No.:



sudut antara diagonal ruang

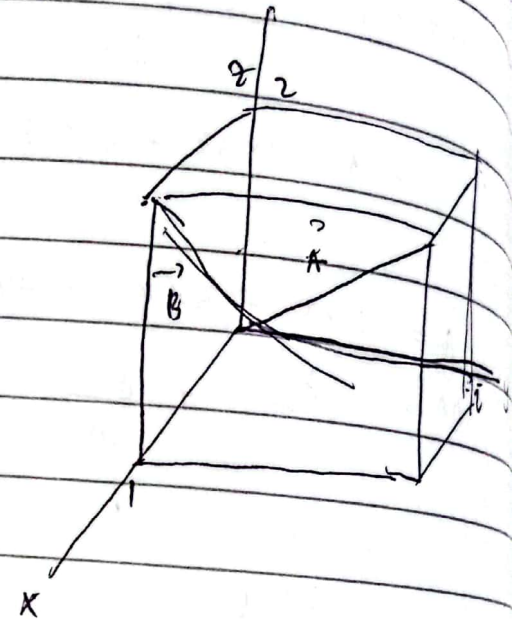
$$\vec{A} = 0\hat{i} + \hat{j} + 2\hat{k}$$

$$\vec{B} = \hat{i} + 0\hat{j} + 2\hat{k}$$

$$\vec{A} \cdot \vec{B} = |\vec{A}| |\vec{B}| \cos \theta$$

$$4 = \sqrt{5} \sqrt{5} \cos \theta$$

$$\cos \theta = \frac{4}{5}$$



$$\vec{A} = \hat{i} + \hat{j} + 2\hat{k}$$

$$\vec{B} = -\hat{i} - \hat{j} + 2\hat{k}$$

$$\vec{A} \cdot \vec{B} = |\vec{A}| |\vec{B}| \cos \theta$$

$$(1-1)\hat{i} + (1-1)\hat{j} + (4)\hat{k} = \sqrt{6} \sqrt{6} \cos \theta$$

$$2 = 6 \cos \theta$$

$$\cos \theta = \frac{2}{6}$$

$$\cos \theta = \frac{1}{3}$$