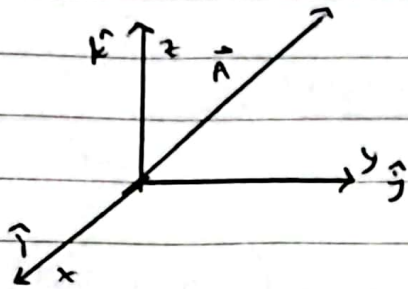


KALISMA

* operator dalam fisika

1.) Analisis vektor



$$\vec{A} = x\hat{i} + y\hat{j} + z\hat{k}$$

$$\hat{A} = \frac{\vec{A}}{|\vec{A}|} = \frac{x\hat{i} + y\hat{j} + z\hat{k}}{\sqrt{x^2 + y^2 + z^2}}$$

$$\hat{A} = x^2y\hat{i} + 3yz\hat{j} + 2xy\hat{k}$$

$$\hat{B} = 2\hat{i} + 2yx\hat{j} + 3xz\hat{k}$$

$$A + B =$$

$$A \cdot B =$$

$$A \times B =$$

$$\begin{aligned} A + B &= (x^2y + 2)\hat{i} + (3yz + 2yx)\hat{j} + (2xy + 3xz)\hat{k} \\ &= x^2yz\hat{i} + 5yzx\hat{j} + 5x^2yz\hat{k} \end{aligned}$$

$$\begin{aligned} A \cdot B &= (x^2y + 2)\hat{i} \cdot (3yz + 2yx)\hat{j} + (2xy + 3xz)\hat{k} \\ &= x^2yz + 3xyz + 6x^2yz \end{aligned}$$

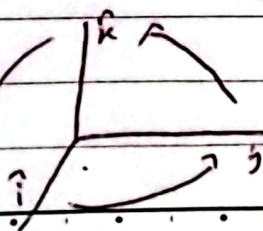
$$A \times B = \begin{vmatrix} \hat{i} & \hat{j} & \hat{k} \\ x^2y & 3yz & 2xy \\ 2 & 2yx & 3xz \end{vmatrix}$$

$$\hat{i} = \hat{j} \cdot \hat{k} - \hat{k} \cdot \hat{j}$$

$$\hat{j} = \hat{k} \cdot \hat{i} - \hat{i} \cdot \hat{k}$$

$$\hat{k} = \hat{i} \cdot \hat{j} - \hat{j} \cdot \hat{i}$$

$$= \hat{i} (9x^2yz - 4x^2yz) + \hat{j} (2xyz - 3x^3yz) + \hat{k} (2x^3yz - 3xyz)$$



$$\hat{i} \cdot \hat{i} = 1$$

$$\hat{j} \cdot \hat{j} = 1$$

$$\hat{k} \cdot \hat{k} = 1$$

Operator malar

$$\nabla = \hat{i} \frac{\partial}{\partial x} + \hat{j} \frac{\partial}{\partial y} + \hat{k} \frac{\partial}{\partial z}$$

gradien

$$T = x^2 yz + 3y^2 z$$

$$\nabla T = \hat{i} \frac{\partial (x^2 yz + 3y^2 z)}{\partial x} + \hat{j} \frac{\partial (x^2 yz + 3y^2 z)}{\partial y} + \hat{k} \frac{\partial (x^2 yz + 3y^2 z)}{\partial z}$$

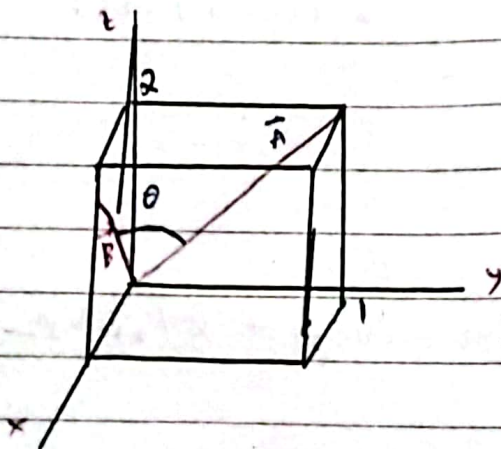
$$= \hat{i} (2xy z) + \hat{j} (x^2 z + 6yz) + \hat{k} (x^2 y + 3y^2)$$

$$A = 2x\hat{i} + 3y\hat{j} - 4z\hat{k}$$

$$\nabla \cdot \vec{A} =$$

$$\nabla \times \vec{A} = \begin{vmatrix} \hat{i} & \hat{j} & \hat{k} \\ \frac{\partial}{\partial x} & \frac{\partial}{\partial y} & \frac{\partial}{\partial z} \\ 2x & 3y & -4z \end{vmatrix}$$

$$= \hat{i} \left(\frac{\partial 4z}{\partial y} - \frac{\partial 3y}{\partial z} \right) + \hat{j} \left(\frac{\partial 2x}{\partial z} - \frac{\partial 4z}{\partial x} \right) + \hat{k} \left(\frac{\partial 3y}{\partial x} - \frac{\partial 2x}{\partial y} \right)$$



$$\vec{A} = 0\hat{i} + \hat{j} + 2\hat{k}$$

$$\vec{B} = \hat{i} + 0\hat{j} + 2\hat{k}$$

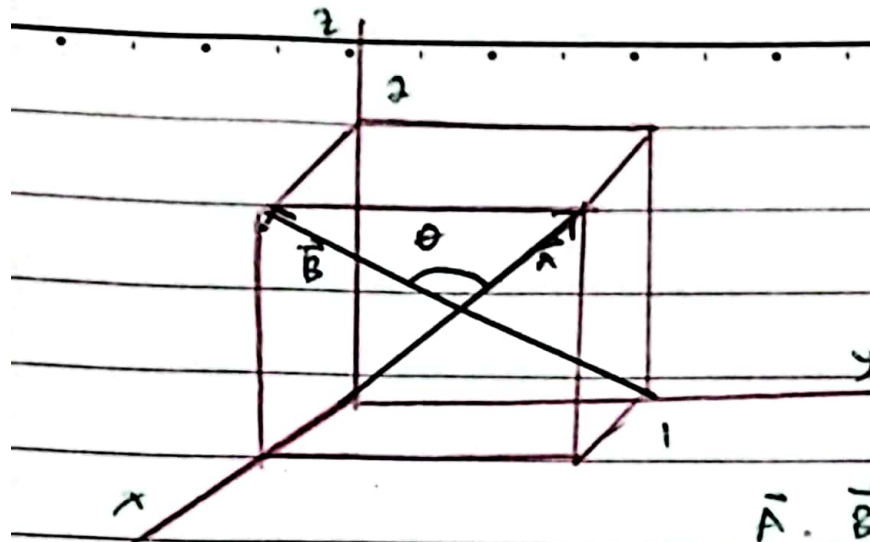
$$\vec{A} \cdot \vec{B} = |\vec{A}| |\vec{B}| \cos \theta$$

$$4 = \sqrt{5} \cdot \sqrt{5} \cos \theta$$

$$\cos \theta = \frac{4}{5} \quad \theta = \cos^{-1} \frac{4}{5}$$

No

Date



$$\vec{A} = \hat{i} + \hat{j} + 2\hat{k}$$

$$\vec{B} = -\hat{i} - \hat{j} + 2\hat{k}$$

$$\vec{A} \cdot \vec{B} = |\vec{A}| |\vec{B}| \cos \theta$$

$$2 = \sqrt{6} \sqrt{4} \cos \theta$$

$$2 = \sqrt{6} \cdot 2 \cos \theta$$