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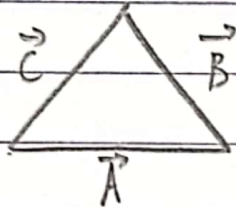
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Test

soal 1



$$\vec{A} = 1\hat{i} + 2\hat{j} + 0\hat{k}$$

$$\vec{B} = -1\hat{i} - 2\hat{j} + 3\hat{k}$$

1. Hitung vektor  $\vec{C}$

2. Hitung sudut  $\hat{A}B$

$$1. \vec{A} + \vec{B} = |\vec{A}| |\vec{B}| \cos \theta$$
$$\vec{C} = 0\hat{i} + 0\hat{j} + 3\hat{k}$$

$$2. \vec{A} = 1\hat{i} + 2\hat{j} + 0\hat{k}$$

$$|\vec{A}| = \sqrt{1^2 + 2^2 + 0^2}$$

$$\hat{A} = \frac{\vec{A}}{|\vec{A}|} = \frac{1\hat{i} + 2\hat{j} + 0\hat{k}}{\sqrt{1^2 + 2^2 + 0^2}}$$

$$\vec{A} + \vec{B} = 1\hat{i} + 2\hat{j} + 0\hat{k} + (-1\hat{i} - 2\hat{j} + 3\hat{k})$$

$$= -\hat{i} - 4\hat{j} + 3\hat{k}$$

$$|\vec{A} + \vec{B}| = \sqrt{(-1)^2 + (-4)^2 + 3^2} = \sqrt{1 + 16 + 9} = \sqrt{26}$$



$$|\vec{B}| = \sqrt{(-1)^2 + (-2)^2 + (3)^2}$$

$$= \sqrt{1+4+9}$$

$$= \sqrt{14}$$

$$\vec{A} \cdot \vec{B} = |\vec{A}| |\vec{B}| \cos \theta$$

$$-5 = \sqrt{5} \sqrt{14} \cos \theta$$

$$\theta = \arccos \frac{-5}{\sqrt{5} \sqrt{14}}$$

$$2. \vec{A} + \vec{B} = \vec{C}$$

$$\vec{A} = 2x\hat{i} + 3x^2\hat{j} + 4xy\hat{k}$$

$$\vec{B} = xy\hat{i} + 2x\hat{j} + 3x\hat{k}$$

$$\vec{A} \times \vec{B} = \begin{vmatrix} 2x\hat{i} & 3x^2\hat{j} & 4xy\hat{k} \\ xy\hat{i} & 2x\hat{j} & 3x\hat{k} \end{vmatrix}$$

$$= \hat{i}(9x^3 - 8x^2y) - \hat{j}(6x^2y^2) - \hat{k}(3x^3y - 4x^2)$$

3. Hitung divergensi Vektor berikut.

a.  $U_1 = x^2 \hat{i} + 3xz^2 \hat{j} - 2xz \hat{k}$

b.  $U_2 = xy \hat{i} + 2yz \hat{j} + 2xz \hat{k}$

c.  $U_3 = y^2 \hat{i} + (2xy + z^2) \hat{j} - 2yz \hat{k}$

Jawab :

a.  $\nabla U_1 = \hat{i} \left( \frac{\partial}{\partial x} \right) + \hat{j} \left( \frac{\partial}{\partial y} \right) + \hat{k} \left( \frac{\partial}{\partial z} \right)$

$$= 2x + 0 - 2x$$

$$= 2x + 0\hat{j} - 2x$$

b.  $\nabla U_2 = y + 2z + 2x$

c.  $\nabla U_3 = 0\hat{i} + (2x + 2z) + -2y$