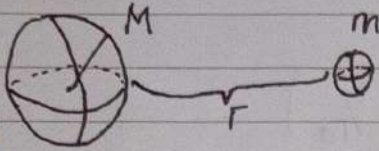


Potensial Listrik (Electric Potential)

→ Potensial adalah massa persatuan muatan



$$W = G \frac{Mm}{r}$$

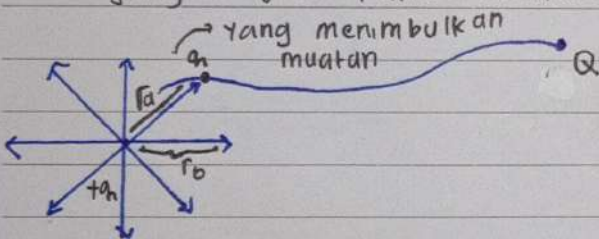
$$V = G \frac{M}{r}$$

$$V = \frac{W}{M} = G \frac{m}{r}$$

$$V = \frac{W}{M}$$

$$V = \frac{W}{q} = \frac{F \cdot r}{q} \rightarrow = \frac{k q_1 \cdot r}{\frac{r^2}{Q}} = \boxed{V = k \frac{q_1}{r}}$$

potensial listrik (V) adalah usaha listrik setiap satuan muatan yang terjadi ketika muatan uji dipindahkan ke suatu titik.

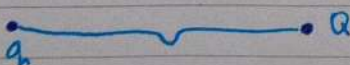


$$\int_a^b V = - \int \vec{E} \cdot d\vec{r}$$

$$V|_a^b = - \int \frac{1}{4\pi\epsilon_0} \frac{q}{r^2} dr$$

$$= - \frac{q}{4\pi\epsilon_0} \int_{r_a}^{r_b} \frac{1}{r^2} dr = - \frac{q}{4\pi\epsilon_0} \left(-\frac{1}{r} \right) \Big|_{r_a}^{r_b}$$

$$= V_b - V_a = \frac{q}{4\pi\epsilon_0} \left(\frac{1}{r_b} - \frac{1}{r_a} \right)$$

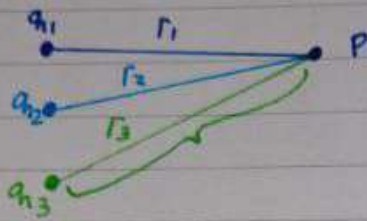


$$V = k \frac{q_1}{r}$$

$$V = \frac{W}{Q}$$

$$k \frac{q_1 Q}{r}$$

$$\rightarrow V = k \frac{q_1}{r}$$



$$V_P = k \left[\frac{q_1}{r_1} + \frac{q_2}{r_2} + \frac{q_3}{r_3} \right]$$

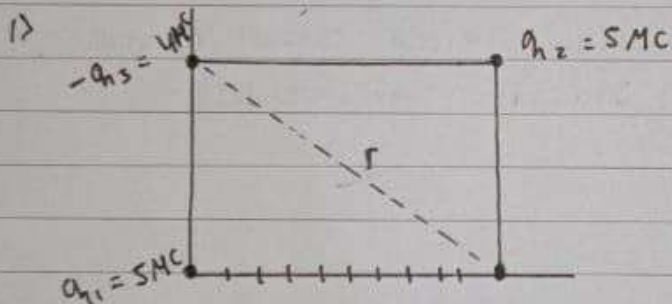
$$= k \sum_{i=1}^n \frac{q_i}{r_i}$$



$$V_b - V_a = \frac{q}{4\pi\epsilon_0} \left(\frac{1}{r_b} - \frac{1}{r_a} \right)$$

$$V_b - V_a = k \frac{Q}{R} \quad (\text{didalam})$$

$$\text{keluar diluar } V_b = V_a = k \frac{Q}{r}$$



$$V = k \frac{q_1}{r_1} + k \frac{q_2}{r_2} + k \frac{(-q_3)}{r_3}$$

$$= k \left(\frac{5}{8} + \frac{5}{8} + \frac{(-4)}{\sqrt{8^2 + 10^2}} \right)$$

$$= k \left(\frac{5}{8} + \frac{5}{8} + \frac{(-4)}{r_{128}} \right)$$

► Persamaan Poisson dan Persamaan Laplace

$$\vec{E} = -\nabla V$$

$$\nabla \cdot \vec{E} = -\nabla^2 V$$

$$\nabla \cdot V = \frac{\rho}{\epsilon_0}$$

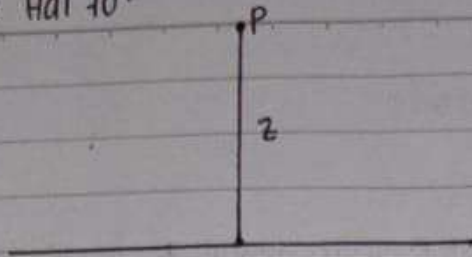
$$\nabla^2 V = -\frac{\rho}{\epsilon_0} \quad \text{Poisson}$$

$$\nabla^2 V = 0 \quad \text{Laplace}$$

Poisson.

Tugas Hal 70.

1. a)



$$\vec{E} = \frac{\lambda}{2\pi\epsilon_0 r}$$

$$\oint \vec{E} \cdot d\vec{a} = \frac{\lambda \cdot l}{\epsilon_0}$$

$$\vec{E} (2\pi r l) = \frac{\lambda \cdot l}{\epsilon_0}$$

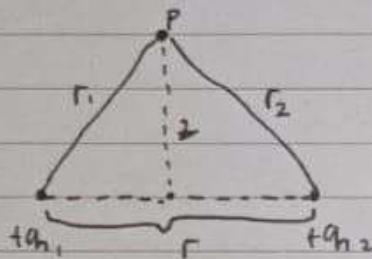
$$\vec{E} = \frac{\lambda}{2\pi\epsilon_0 r}$$

$$V = - \int \vec{E} \cdot d\vec{r}$$

$$= - \int \frac{\lambda}{2\pi\epsilon_0} \frac{1}{r} dr$$

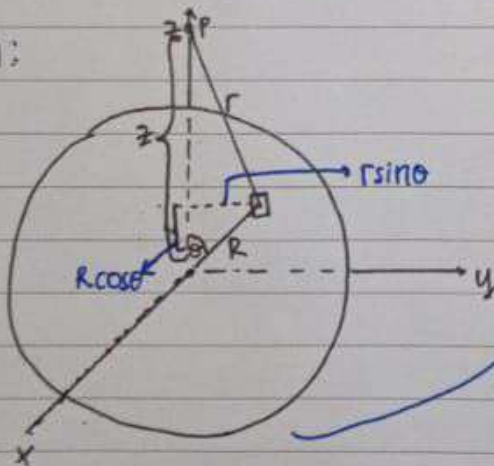
$$= - \frac{\lambda}{2\pi\epsilon_0} \int \frac{1}{r} dr$$

b)



$$V_P = k \left[\frac{q_1}{\sqrt{(\frac{1}{2}r)^2 + z^2}} + \frac{q_2}{\sqrt{(\frac{1}{2}r)^2 + z^2}} \right]$$

Contoh soal:



$$V(P) = \frac{1}{4\pi\epsilon_0} \int \frac{\sigma}{r} da$$

$$r^2 = R^2 + z^2 - 2Rz \cos \theta$$

$$r = \sqrt{(R \sin \theta)^2 + (z - R \cos \theta)^2}$$

$$r = \sqrt{R^2 \sin^2 \theta + z^2 + R^2 \cos^2 \theta - 2Rz \cos \theta}$$

$$r = \sqrt{R^2 (\sin^2 \theta + \cos^2 \theta) + z^2 - 2Rz \cos \theta}$$

$$r = \sqrt{R^2 + z^2 - 2Rz \cos \theta}$$

$$\begin{aligned}
 V &= \frac{1}{4\pi\epsilon_0} \int \frac{\sigma da}{r} \\
 &= \frac{1}{4\pi\epsilon_0} \iint \frac{\sigma (da) \rightarrow R^2 \sin\theta d\theta d\phi}{(R^2 + z^2 - 2Rz\cos\theta)^{1/2}} \\
 &= \frac{\sigma}{4\pi\epsilon_0} \int_0^\pi \int_0^{2\pi} \frac{R^2 \sin\theta d\theta d\phi}{(R^2 + z^2 - 2Rz\cos\theta)^{1/2}} \rightarrow R \text{ disini adalah } R \text{ besar digambar} \\
 &= \frac{\sigma R 2\pi}{4\pi\epsilon_0} \int_0^\pi \frac{\sin\theta d\theta}{(R^2 + z^2 - 2Rz\cos\theta)^{1/2}} \rightarrow R \text{ disini adalah } R \text{ kecil digambar} \\
 &= \frac{\sigma R 2\pi}{4\pi\epsilon_0} \frac{d(\cos\theta)}{(R^2 + z^2 - 2Rz\cos\theta)^{1/2}} \\
 &= \frac{\sigma R 2\pi}{4\pi\epsilon_0} \int_0^\pi (R^2 + z^2 - 2Rz\cos\theta)^{-1/2} d(\cos\theta) \\
 &= \frac{\sigma R 2\pi}{4\pi\epsilon_0} 2 \left(R^2 + z^2 - 2Rz\cos\theta \right)^{\frac{1}{2}} \Big|_0^\pi
 \end{aligned}$$