

Potensial Listrik

1. Pengenalan Potensial Melalui Analogi

Potensial listrik analogikan sebagai potensial

gravitasi yang didefinisikan sebagai perubahan

energi potensial persatuan massa.

$$V = \frac{W}{m} = G \frac{M \cdot m}{r} = G \frac{m}{r}$$

Potensial gravitasi merupakan besaran skalar, yaitu

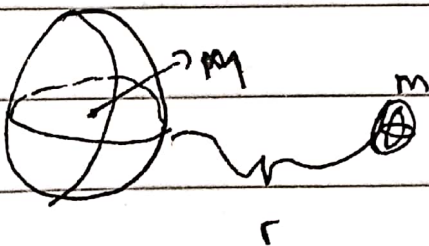
suatu besaran yang hanya mempunyai nilai.

Saja tanpa arah, jika ada lebih dari satu

massa benda sumber, maka potensial gravitasinya

adalah:

$$V = G \frac{m_1}{r_1} + G \frac{m_2}{r_2} + \dots + G \frac{m_n}{r_n} = \sum_{i=1}^n G \frac{m_i}{r_i}$$



$$V = G \frac{Mm}{r}$$

$$V = G \frac{m}{r}$$

$$V = \frac{W}{m}$$

$$V = \frac{W}{M}$$

$$G = \frac{m}{r}$$

$$V = \frac{W}{q} = \frac{F \cdot r}{q}$$

$$= \frac{kq \cdot q_2 \cdot r}{r^2}$$

$$V = k \cdot \frac{q}{r}$$

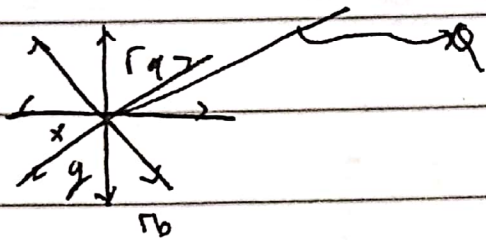
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$$\int_q dv = - \int \vec{E} \cdot d\vec{r}$$

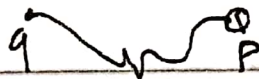
$$V \Big|_a^b = - \int_a^b \frac{1}{4\pi\epsilon_0} \frac{q}{r^2} dr$$

$$= \frac{q}{4\pi\epsilon_0} \int_a^b \frac{1}{r^2} dr$$

$$= \frac{-q}{4\pi\epsilon_0} \left(-\frac{1}{r} \Big|_a^b \right)$$

$$= V_b - V_a = \frac{q}{4\pi\epsilon_0} \left(\frac{1}{r_b} - \frac{1}{r_a} \right)$$

$$V = k \frac{q}{r}$$



$$V = \frac{W}{Q}$$

Q

$$P = k \frac{q}{r}$$

1-4-2029.

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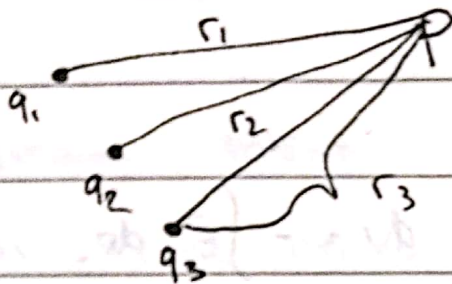
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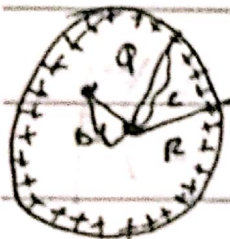
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$$V = \frac{W}{q} = \frac{\vec{P} \cdot \vec{S}}{q} = k \frac{q}{r}$$

$$V_P = k \left[\frac{q_1}{r_1} + \frac{q_2}{r_2} + \frac{q_3}{r_3} \right]$$

$$= k \sum_{i=1}^n \frac{q_i}{r_i}$$



$$V_b - V_a = \frac{Q}{4\pi\epsilon_0} \left(\frac{1}{r} - \frac{1}{r_a} \right)$$

$$V_b = k \frac{Q}{r}$$

$$V = k \frac{Q}{r}, \quad r > R$$

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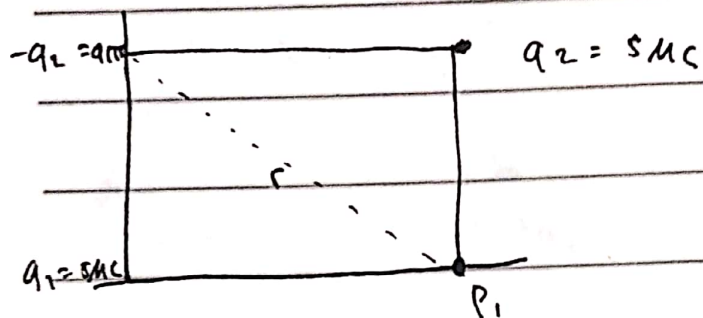
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(Contoh Soal 1:

Gambarakan Step up Model pada kasusnya.



$$V = \frac{kq_1}{r_1} + \frac{kq_2}{r_2} + \frac{k(-q_3)}{r_3}$$

$$= k \left(\frac{r}{\rho} + \frac{r}{\rho} + \frac{c-a}{\sqrt{b^2 + b^2}} \right)$$

$$= k \left(\frac{r}{\rho} + \frac{r}{\rho} + \frac{c-a}{128} \right)$$

$$E = -\nabla V$$

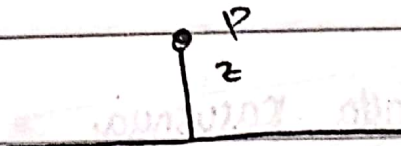
$$\nabla \cdot E = -\nabla^2 V$$

$$\nabla \cdot \vec{E} = \oint_{to} \rightarrow \text{fluxum Gauss}$$

$$\nabla^2 V = -\oint_{to} \text{persen}$$

$$\oint \vec{E} \cdot d\vec{q} = \int (\nabla \cdot \vec{E}) dV$$

$$\nabla^2 V = 0 \quad \text{laplace.}$$



$$\vec{E} = \frac{\lambda}{2\pi\epsilon_0 r}$$

$$2\pi\epsilon_0 r$$

$$\oint \vec{E} \cdot d\vec{q} = \frac{\lambda \cdot l}{\epsilon_0}$$

$$\vec{E} (2\pi r l) = \frac{\lambda \cdot l}{\epsilon_0}$$

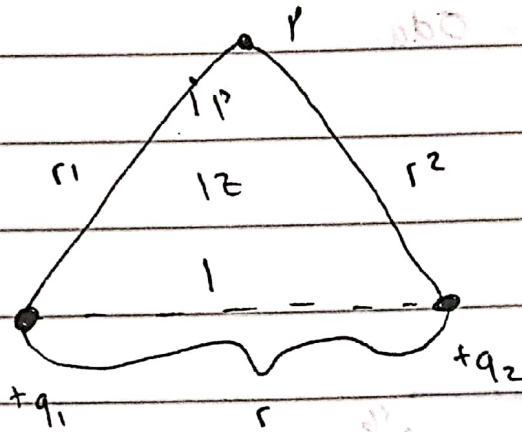
$$\vec{E} = \frac{\lambda}{2\pi\epsilon_0 r}$$

$$V = - \int \vec{E} \cdot d\vec{r}$$

$$V = - \int \frac{\lambda}{2\pi\epsilon_0} \frac{1}{r} dr$$

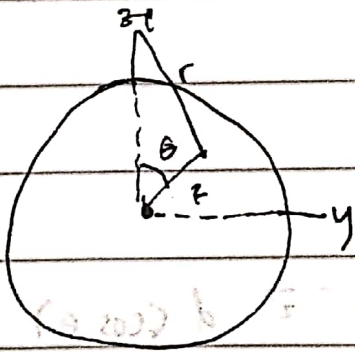
$$= - \frac{\lambda}{2\pi\epsilon_0} \int \frac{1}{r} dr$$

Contoh Soal:



$$V_P = ? \quad k \left[\frac{q_1}{\sqrt{r_1^2 + z^2}} + \frac{q_2}{\sqrt{r_2^2 + z^2}} \right]$$

Contoh Soal:



$$V(r) = \frac{1}{4\pi\epsilon_0} \int \frac{\sigma}{r} da$$

$$r^2 = R^2 + z^2 - 2Rz \cos \theta$$

$$r = \sqrt{R^2 \sin^2 \theta + (z - R \cos \theta)^2}$$

$$= \sqrt{R^2 (\sin^2 \theta + \cos^2 \theta) + z^2 - 2zR \cos \theta}$$

$$= \sqrt{R^2 (\sin^2 \theta + \cos^2 \theta) + z^2 - 2zR \cos \theta}$$

$$= \sqrt{R^2 + z^2 - 2zR \cos \theta}$$

$$V = \frac{1}{4\pi\epsilon_0} \int \frac{\sigma da}{r} \quad r^2 \sin \theta d\theta d\phi$$

$$da = \sigma da.$$

$$= \frac{1}{4\pi\epsilon_0} \iint \frac{\sigma da}{r}$$

$$= \frac{1}{4\pi\epsilon_0} \iint \frac{\sigma da}{(R^2 + z^2 - 2Rz \cos \theta)^{1/2}}$$

$$= \frac{\sigma}{4\pi\epsilon_0} \int_0^\pi \int_0^{2\pi} \frac{r^2 \sin \theta d\theta d\phi}{(R^2 + z^2 - 2Rz \cos \theta)^{1/2}}$$

$$= \frac{\sigma R 2\pi}{4\pi\epsilon_0} \int_0^\pi \frac{\sin \theta d\theta}{(R^2 + z^2 - 2Rz \cos \theta)^{1/2}}$$

$$V_1 = \square \int_0^\pi \frac{d(\cos \theta)}{(R^2 + z^2 - 2Rz \cos \theta)^{1/2}}$$

$$= \square \int_0^\pi (R^2 + z^2 - 2Rz \cos \theta)^{-1/2} d(\cos \theta)$$

$$= \square \left[\frac{(R^2 + z^2 - 2Rz \cos \theta)^{1/2}}{1/2} \right]_0^\pi$$