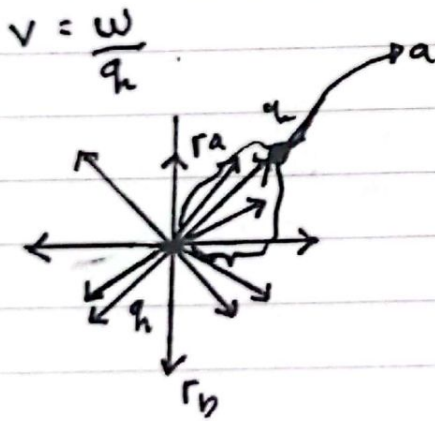
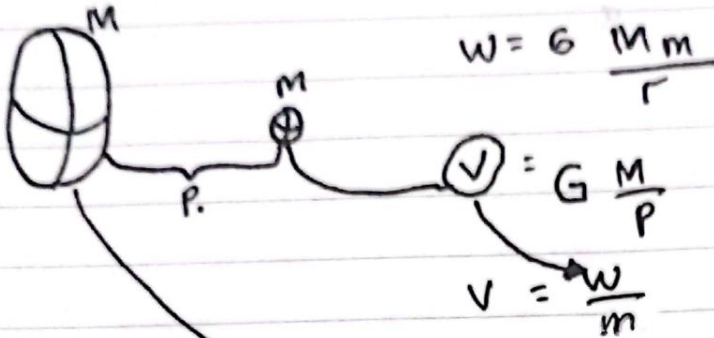


Potensial Listrik (Electric Potential)



$$\int_a^b dv = - \int \vec{E} dp$$

$$V \Big|_a^b = - \int \frac{1}{4\pi\epsilon_0} \frac{q}{p^2} dp$$

$$= - \frac{q}{4\pi\epsilon_0} \int_{r_a}^{r_b} \frac{1}{p^2} dp = - \frac{q}{4\pi\epsilon_0}$$

$$\left(-\frac{1}{r} \Big|_{r_a}^{r_b} \right)$$

$$V_b - V_a = \frac{q}{4\pi\epsilon_0} \left(\frac{1}{r_b} - \frac{1}{r_a} \right)$$

lanjutan

$$V = \frac{W}{q_h} = \frac{F_i P}{\partial}$$

$$= K \frac{q_i q_h}{r^2} P$$

$$= \frac{r^2}{q}$$

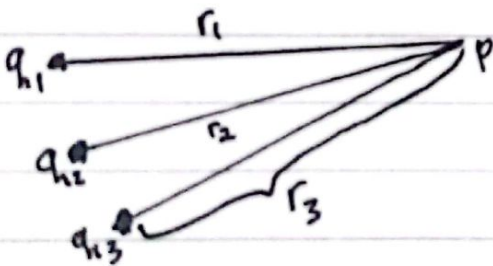
$$= V = K \frac{q_h}{P}$$

$\int \Delta V$

$$V = K \frac{q_h}{r}$$

$$V = \frac{W}{q_h} \xrightarrow{Kq_h}$$

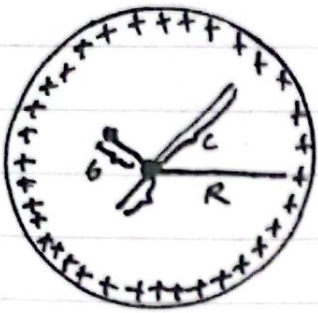
$$q_h \text{ --- } P = K \frac{q_h}{r}$$



$$V_P = K \left[\frac{q_1}{r_1} + \frac{q_2}{r_2} + \frac{q_3}{r_3} \right]$$

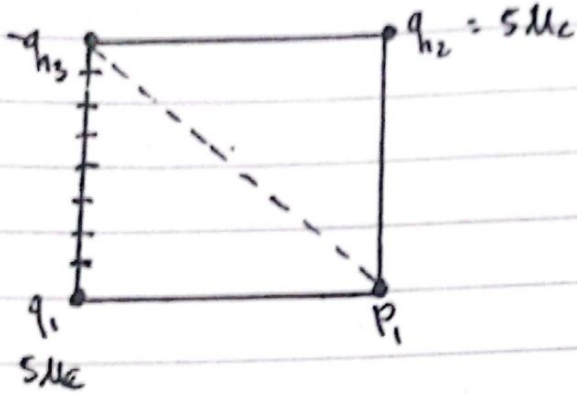
$$= K \sum_{i=1}^n \frac{q_{hi}}{r_i}$$

$$V = \frac{W}{q_h} = \frac{P \cdot S}{q_h} = K \frac{q_h}{r}$$



$$V = k \frac{Q}{r}, r > R$$

1.) Gambarkan



Jawab : $V = \frac{kq_1}{r_1} + \frac{kq_2}{r_2} + \frac{k(-q_3)}{r_3}$

$$= k \left(\frac{5}{8} + \frac{5}{8} + \frac{(-9)}{\sqrt{8^2 + 8^2}} \right)$$

$$= k \left(\frac{5}{8} + \frac{5}{8} + \frac{(-9)}{\sqrt{128}} \right)$$

Persamaan Poisson

$$\mathbf{E} = -\nabla V$$

$$\nabla \cdot \mathbf{E} = -\nabla^2 V$$

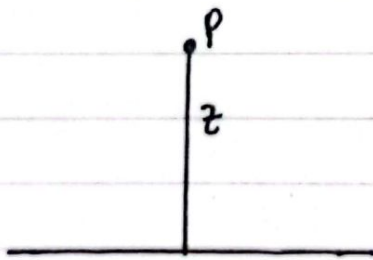
$$\nabla \cdot \mathbf{E} = \frac{\rho}{\epsilon_0}$$

$$\nabla^2 V = -\frac{\rho}{\epsilon_0} \quad \text{Poisson}$$

Yang berarti ada sumber medan listrik. Dalam banyak kasus, kita harus memecahkan persamaan ini di wilayah yang tidak mencakup distribusi muatan, yaitu untuk daerah bebas muatan $\rho = 0$

$$\nabla^2 V = 0 \rightarrow \text{persamaan Laplace}$$

Potensial muatan terdistribusi



$$\vec{E} = \frac{\lambda}{2\pi\epsilon_0 r}$$

$$\oint \vec{E} \cdot d\mathbf{a} = \frac{\lambda l}{\epsilon_0}$$

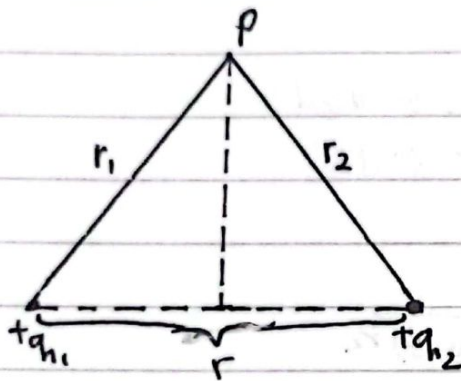
$$\vec{E} (2\pi r/k) = \frac{\lambda k}{\epsilon_0}$$

$$\boxed{\vec{E} = \frac{\sigma}{2\pi\epsilon_0 r}}$$

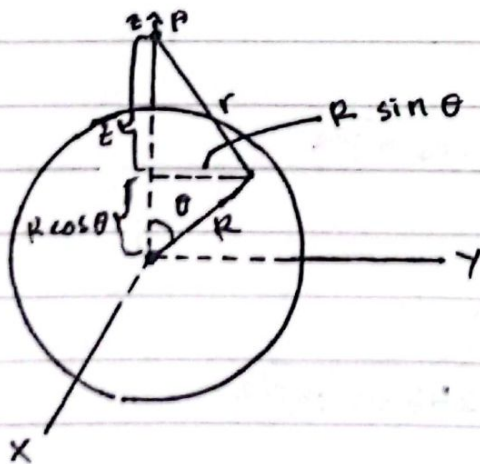
$$V = -\int \vec{E} \cdot d\vec{r}$$

$$= -\int \frac{\lambda}{2\pi\epsilon_0} \frac{1}{r} dr$$

$$= -\frac{\sigma}{2\pi\epsilon_0} \int \frac{1}{r} dr$$



$$V_P = ? K \left[\frac{q_1}{\sqrt{(1/2 r)^2 + z^2}} + \frac{q_2}{\sqrt{(1/2 r)^2 + z^2}} \right]$$



$$V(P) = \frac{1}{4\pi\epsilon_0} \int \frac{\sigma}{r} da$$

$$r^2 = R^2 + z^2 - 2Rz \cos \theta$$

$$r = \sqrt{(R \sin \theta)^2 + (z - R \cos \theta)^2}$$

$$= \sqrt{R^2 \sin^2 \theta + z^2 + R^2 \cos^2 \theta - 2 z R \cos \theta}$$

$$= \sqrt{R^2 (\sin^2 \theta + \cos^2 \theta) + z^2 - 2 z R \cos \theta}$$

$$= \sqrt{R^2 + z^2 - 2 z R \cos \theta}$$

$$V = \frac{1}{4\pi\epsilon_0} \int \frac{\sigma da}{r}$$

$\rightarrow R^2 \sin \theta d\theta d\phi$
 $da = \sigma da$

$$= \frac{1}{4\pi\epsilon_0} \iint \frac{\sigma da}{(R^2 + z^2 - 2 z R \cos \theta)^{1/2}}$$

$$= \frac{\sigma}{4\pi\epsilon_0} \int_0^\pi \int_0^{2\pi} \frac{R^2 \sin \theta d\theta d\phi}{(R^2 + z^2 - 2 z R \cos \theta)^{1/2}}$$

$$= \frac{\sigma R 2\pi}{4\pi\epsilon_0} \int_0^\pi \frac{\sin \theta d\theta}{(R^2 + z^2 - 2 z R \cos \theta)^{1/2}}$$

$$V_p = \frac{1}{4\pi\epsilon_0} \int_0^\pi \frac{d(\cos \theta)}{(R^2 + z^2 - 2 z R \cos \theta)^{1/2}}$$

$$= \frac{1}{4\pi\epsilon_0} \int_0^\pi (R^2 + z^2 - 2 z R \cos \theta)^{-1/2} d(\cos \theta)$$

$$= \frac{1}{4\pi\epsilon_0} (R^2 + z^2 - 2 z R \cos \theta)^{1/2} \Big|_0^\pi$$