

Potensial Listrik (Electric Potential)



$$W = G \frac{Mm}{r}$$

$$V = G \frac{M}{r}$$

$$V = \frac{W}{m}$$

$$V = \frac{W}{M}$$

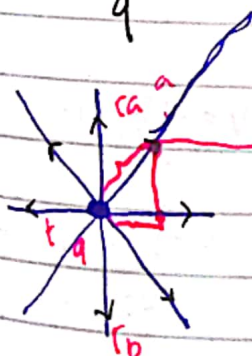
$$= G \frac{M}{r}$$

$$V = \frac{W}{q} = \frac{F \cdot r}{q}$$

$$= k \frac{q \otimes r}{r^2}$$

$$V = k \frac{q}{r}$$

$$V = \frac{W}{q}$$



$$\int_a^b dv = - \int_a^b \vec{E} \cdot d\vec{r}$$

$$v \Big|_a^b = - \int_a^b \frac{1}{4\pi\epsilon_0} \frac{q}{r^2} dr$$

$$= - \frac{q}{4\pi\epsilon_0} \int_a^b \frac{1}{r^2} dr$$

Senin, 1 April 2024

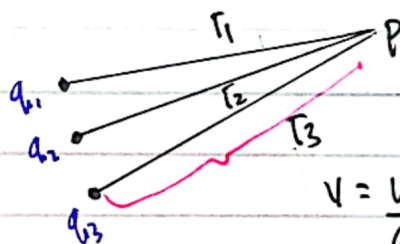
$$= \frac{-q}{4\pi\epsilon_0} \left(-\frac{1}{r} \Big|_{r_a}^{r_b} \right)$$

$$= V_b - V_a = \frac{q}{4\pi\epsilon_0} \left(\frac{1}{r_b} - \frac{1}{r_a} \right)$$

$$V = k \frac{q}{r}$$

$$V = \frac{W}{Q} \rightarrow F = \frac{qQ}{r}$$

$$P = k \frac{q}{r}$$



$$V = \frac{W}{q} = \frac{\vec{P} \cdot \vec{S}}{q} = k \frac{q}{r}$$

$$V_P = k \left[\frac{q_1}{r_1} + \frac{q_2}{r_2} + \frac{q_3}{r_3} \right]$$

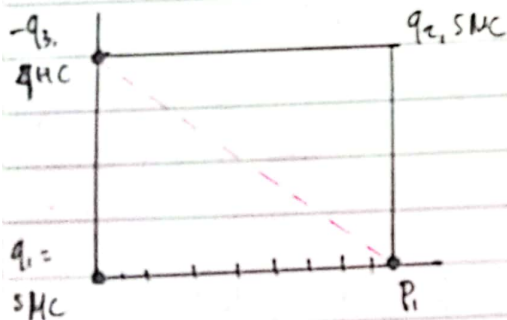
$$= k \sum_{i=1}^n \frac{q_i}{r_i}$$



$$V_b - V_a = \frac{q}{4\pi\epsilon_0} \left(\frac{1}{r_b} - \frac{1}{r_c} \right)$$

$$V_b - V_a = k \frac{q}{R}$$

$$V = k \frac{q}{r}, r > R$$



$$V = \frac{kq_1}{r_1} + \frac{kq_2}{r_2} + k \frac{(-q_3)}{r_3}$$

$$= k \left(\frac{q}{a} + \frac{q}{b} + \frac{(-q)}{\sqrt{a^2 + b^2}} \right)$$

$$= k \left(\frac{q}{a} + \frac{q}{b} + \frac{(-q)}{\sqrt{a^2 + b^2}} \right)$$

Persamaan Poisson dan Persamaan Laplace

Exam
①

$$\vec{E} = -\nabla V$$

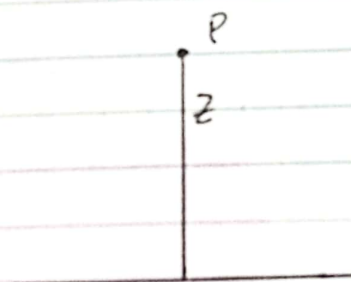
$$\nabla \cdot \vec{E} = -\nabla^2 V$$

$$\nabla \cdot \vec{E} = \frac{\rho}{\epsilon_0}$$

$$\nabla^2 V = -\frac{\rho}{\epsilon_0} \Rightarrow \text{Poisson}$$

$$\nabla^2 V = 0 \Rightarrow \text{Laplace}$$

$$\oint \vec{E} \cdot d\vec{a} = \int_V (\nabla \cdot \vec{E}) dV$$



②

$$\vec{E} = \frac{\lambda}{2\pi\epsilon_0 r}$$

$$\oint \vec{E} \cdot d\vec{a} = \frac{\lambda \cdot l}{\epsilon_0}$$

$$\vec{E}(2\pi r l) = \frac{\lambda \cdot l}{\epsilon_0}$$

$$\vec{E} = \frac{\lambda}{2\pi\epsilon_0 r}$$

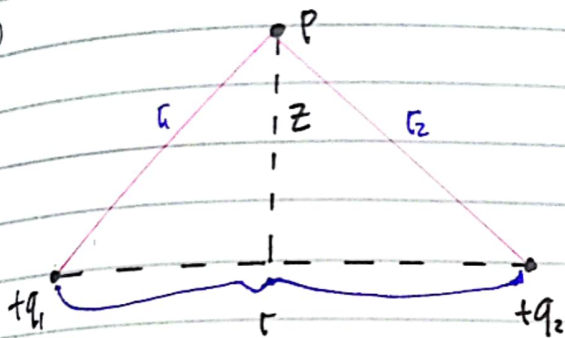
$$V = -\int \vec{E} \cdot d\vec{r}$$

$$= -\int \frac{\lambda}{2\pi\epsilon_0} \frac{1}{r} dr$$

$$= -\frac{\lambda}{2\pi\epsilon_0} \int \frac{1}{r} dr$$

Example:

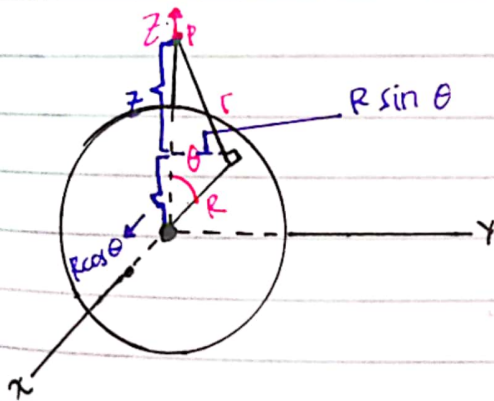
①



$V_P = \dots ?$

$$K = \left[\frac{q_1}{\sqrt{(tr)^2 + z^2}} + \frac{q_2}{\sqrt{(tr)^2 + z^2}} \right]$$

②



$$V(P) = \frac{1}{4\pi\epsilon_0} \int \frac{\sigma}{r} da$$

$$r = \sqrt{(R \sin \theta)^2 + (z - R \cos \theta)^2}$$

$$\begin{aligned} &= \sqrt{R^2 \sin^2 \theta + z^2 + R^2 \cos^2 \theta - 2zR \cos \theta} \\ &= \sqrt{R^2 (\sin^2 \theta + \cos^2 \theta) + z^2 - 2zR \cos \theta} \\ &= \sqrt{R^2 + z^2 - 2zR \cos \theta} \end{aligned}$$

dengan $= \sigma da$

$$V = \frac{1}{4\pi\epsilon_0} \int \frac{\sigma da}{r}$$

$$= \frac{1}{4\pi\epsilon_0} \iint \frac{\sigma da}{(R^2 + z^2 - 2zR \cos \theta)^{\frac{1}{2}}}$$

$$= \frac{\sigma}{4\pi\epsilon_0} \int_0^\pi \int_0^{2\pi} \frac{R^2 \sin \theta d\theta d\phi}{(R^2 + z^2 - 2zR \cos \theta)^{\frac{1}{2}}}$$

$$= \frac{\sigma R 2\pi}{4\pi\epsilon_0} \int_0^\pi \frac{\sin \theta d\theta}{(R^2 + z^2 - 2zR \cos \theta)^{\frac{1}{2}}}$$

$$\begin{aligned} V_P &= \frac{\sigma}{2\epsilon_0} \int_0^\pi \frac{d \cos \theta}{(R^2 + z^2 - 2zR \cos \theta)^{\frac{1}{2}}} \\ &= \frac{\sigma}{2\epsilon_0} \int_0^\pi (R^2 + z^2 - 2zR \cos \theta)^{-\frac{1}{2}} d(\cos \theta) \\ &= \frac{\sigma}{2\epsilon_0} \left(R^2 + z^2 - 2zR \cos \theta \right)^{\frac{1}{2}} \Big|_0^\pi \end{aligned}$$