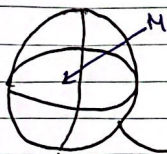


Potensial Listrik (elektrik potensial) sacara analog



$$W = G \frac{Mm}{r}$$

$$V = G \frac{M}{r}$$

$$V = \frac{W}{m}$$

$$V = \frac{W}{M} = G \frac{M}{r}$$

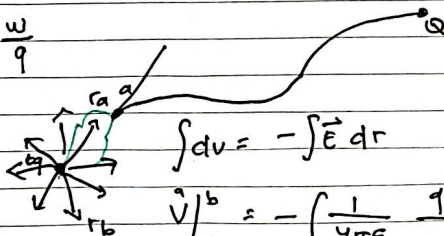
$$V = \frac{W}{q} = \frac{F \cdot r}{q}$$

$$= \frac{k \frac{q \cdot Q \cdot r}{r^2}}{Q}$$

$$V = k \frac{q}{r}$$

sacara Fisika

$$V = \frac{w}{q}$$



$$\int dv = - \int \vec{E} \cdot d\vec{r}$$

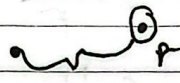
$$V|_a^b = - \int \frac{1}{4\pi\epsilon_0} \frac{q}{r^2} q_r$$

$$= - \frac{q}{4\pi\epsilon_0} \int_{r_a}^{r_b} \frac{1}{r^2} dr$$

$$= - \frac{q}{4\pi\epsilon_0} \left(-\frac{1}{r} \right) \Big|_{r_a}^{r_b}$$

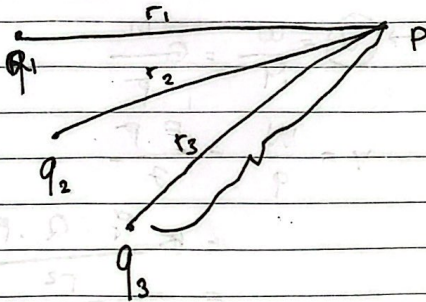
$$= V_b - V_a = \frac{q}{4\pi\epsilon_0} \left(\frac{1}{r_b} - \frac{1}{r_a} \right)$$

$$V = k \frac{q}{r}$$

Kasus $\rightarrow$ 

$$V = \frac{W}{Q} \rightarrow K = \frac{qQ}{r}$$

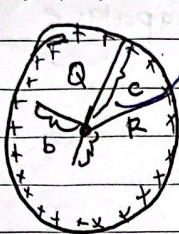
Jika SEBANYAK tidak vektor



$$V = \frac{W}{q} = \frac{\vec{P} \cdot \vec{S}}{q} = k \frac{q}{r}$$

$$V_r = k \left[\frac{q_1}{r_1} + \frac{q_2}{r_2} + \frac{q_3}{r_3} \right]$$

$$= k \sum_{i=1}^n \frac{q_i}{r_i}$$



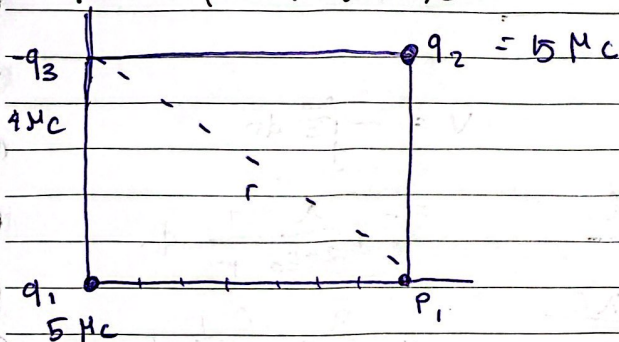
$$V_b - V_a = \frac{q}{4\pi\epsilon_0} \left(\frac{1}{r_b} - \frac{1}{r_a} \right)$$

$$V_b - V_a = k \frac{Q}{R}$$

Berapa Potensial luar

$$V = k \frac{Q}{r}, r > R$$

Dua muatan titik positif sama besarnya $+5 \text{ Mc}$ pada sumbu x . Satu dipusat $(0,0)$ dan yg lain pada $(8,0) \text{ cm}$. Tentukan potensial di (a) titik e , pada posisi $(8,6) \text{ cm}$



$$V = k \left(\frac{q_1}{r_1} + \frac{q_2}{r_2} + \frac{(-q_3)}{r_3} \right)$$

$$= k \left(\frac{5}{8} + \frac{5}{8} + \frac{(-4)}{\sqrt{8^2+8^2}} \right)$$

$$= k \left(\frac{5}{8} + \frac{5}{8} + \frac{(-4)}{\sqrt{128}} \right)$$

• Persamaan Poisson dan persamaan Laplace

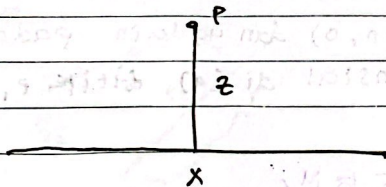
$$\vec{E} = -\nabla V$$

$$\nabla \cdot \vec{E} = -\nabla^2 V$$

$$\nabla \cdot \vec{E} = \frac{\rho}{\epsilon_0}$$

$$\nabla^2 V = \frac{\rho}{\epsilon_0} \quad (\text{Poisson})$$

$$\nabla^2 V = 0 \quad (\text{Laplace})$$



$$\vec{E} = \frac{\lambda}{2\pi\epsilon_0 r}$$

$$V = -\int \vec{E} \, dr$$

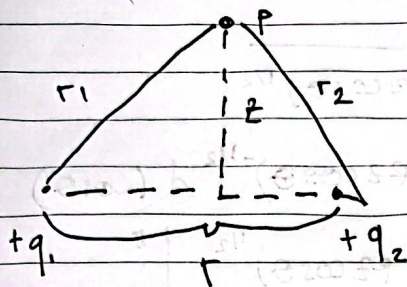
$$\oint \vec{E} \, da = \frac{\lambda l}{\epsilon_0}$$

$$= -\int \frac{\lambda}{2\pi\epsilon_0} \frac{1}{r} \, dr$$

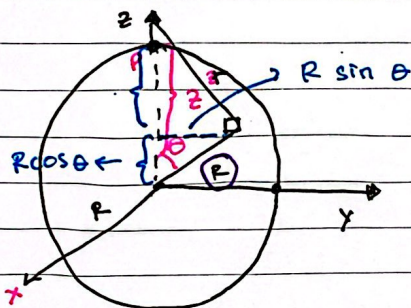
$$\vec{E} (2\pi\epsilon_0 r l) = \frac{\lambda l}{\epsilon_0}$$

$$= -\frac{\lambda}{2\pi\epsilon_0} \int \frac{1}{r} \, dr$$

$$\boxed{\vec{E} = \frac{\lambda}{2\pi\epsilon_0 r}}$$



$$V_P = K \left[\frac{q_1}{\sqrt{(\frac{1}{2}r)^2 + z^2}} + \frac{q_2}{\sqrt{(\frac{1}{2}r)^2 + z^2}} \right]$$



$$r = \sqrt{(R \sin \theta)^2 + (z - R \cos \theta)^2}$$

$$r = \sqrt{R^2 \sin^2 \theta + z^2 - 2zR \cos \theta}$$

$$r = \sqrt{R^2 (\sin^2 \theta + \cos^2 \theta) + z^2 - 2zR \cos \theta}$$

$$r = \sqrt{R^2 + z^2 - 2zR \cos \theta}$$

$$r^2 = R^2 + z^2 - 2zR \cos \theta$$

$$V(P) = \frac{1}{4\pi\epsilon_0} \int \frac{\sigma}{r} da$$

$$= \frac{1}{4\pi\epsilon_0} \iint \frac{\sigma da}{(R^2 + z^2 - 2zR \cos \theta)^{\frac{1}{2}}}$$

$$= \frac{\sigma}{4\pi\epsilon_0} \int_0^\pi \int_0^{2\pi} \frac{R^2 \sin \theta d\theta d\phi}{(R^2 + z^2 - 2zR \cos \theta)^{\frac{1}{2}}}$$

$$= \frac{\sigma R^2 2\pi}{4\pi\epsilon_0} \int_0^\pi \frac{\sin \theta d\theta}{(R^2 + z^2 - 2zR \cos \theta)^{\frac{1}{2}}}$$

$$V_p = \frac{\sigma R 2\pi}{4\pi \epsilon_0} \int_0^\pi \frac{d(\cos \theta)}{(R^2 + z^2 - 2Rz \cos \theta)^{1/2}}$$

$$= \frac{\sigma R 2\pi}{4\pi \epsilon_0} \int_0^\pi (R^2 + z^2 - 2Rz \cos \theta)^{-1/2} d(\cos \theta)$$

$$= \frac{\sigma R 2\pi}{4\pi \epsilon_0} \left[2(R^2 + z^2 - 2Rz \cos \theta)^{1/2} \right]_0^\pi$$

$\left(\frac{1}{2} : 2\right) = 2$

