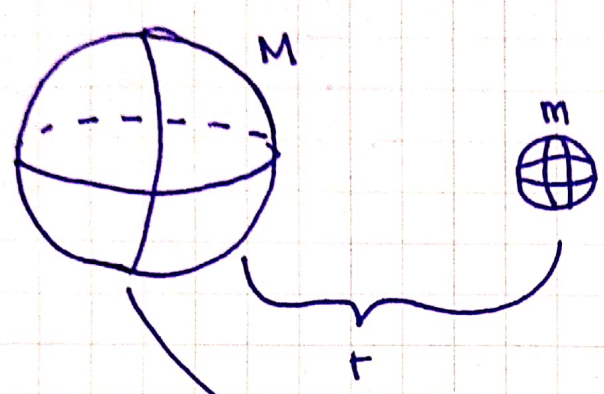


"Potensial Listrik"

electric potential



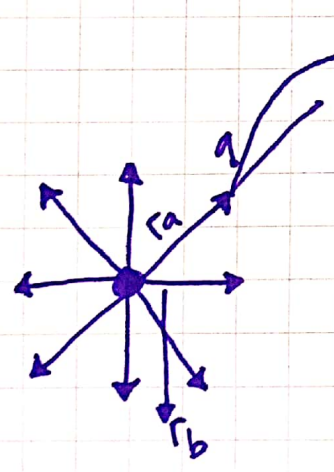
$$W = G \frac{M \cdot m}{r}$$

$$V = G \frac{M}{r}$$

$$V = \frac{W}{m}$$

$$V = \frac{W}{M} = G \frac{M}{r}$$

$$V = \frac{W}{q} = \frac{F \cdot r}{q} = \frac{kq \cdot Q \cdot r}{r^2} = \frac{kqQ}{r}$$



$$\int_a^b dv = - \int_a^b \vec{E} \cdot d\vec{r}$$

$$V = k \frac{q}{r} = \frac{W}{q}$$

$$V \Big|_a^b = - \int \frac{1}{4\pi\epsilon_0} \frac{q}{r^2} dr$$

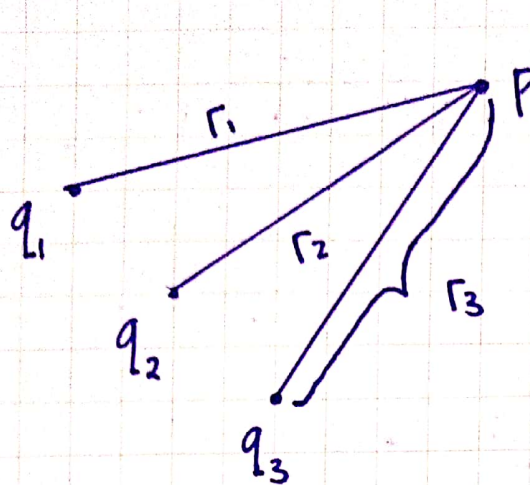
$$= - \frac{q}{4\pi\epsilon_0} \int_{r_a}^{r_b} \frac{1}{r^2} dr = - \frac{q}{4\pi\epsilon_0} \left(-\frac{1}{r} \Big|_{r_a}^{r_b} \right)$$

$$V_b - V_a = \frac{q}{4\pi\epsilon_0} \left(\frac{1}{r_b} - \frac{1}{r_a} \right)$$

q → p

$$V = k \frac{q}{r}$$

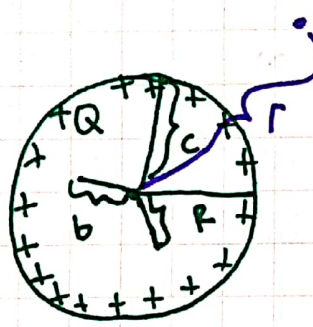
$$V = \frac{W}{q} \quad \left| = k \frac{q}{r} \right|$$



$$V = \frac{W}{q} = \frac{\vec{P} \cdot \vec{S}}{q} = k \frac{q}{r}$$

$$V_P = k \left[\frac{q_1}{r_1} + \frac{q_2}{r_2} + \frac{q_3}{r_3} \right]$$

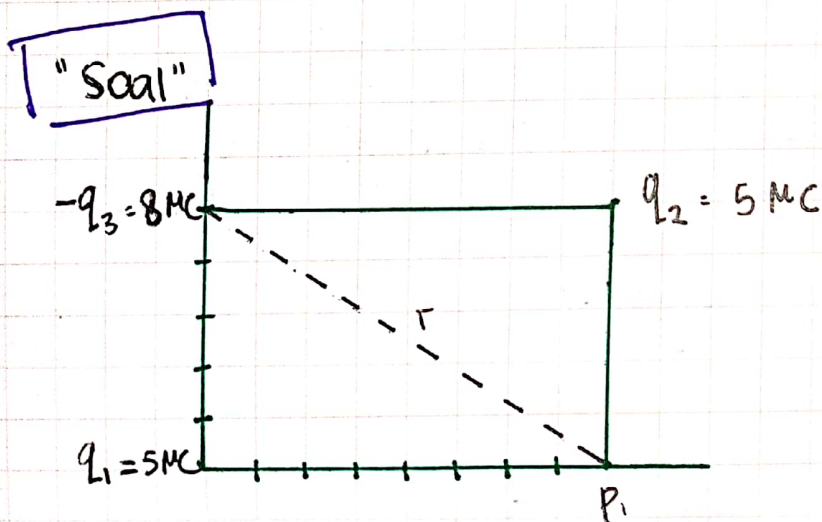
$$= k \sum_{i=1}^n \frac{q_i}{r_i}$$



$$V_b - V_a = \frac{R}{4\pi\epsilon_0} \left(\frac{1}{r_b} - \frac{1}{r_a} \right) \stackrel{=0}{=}$$

$$V_b = V_a = k \frac{Q}{R}$$

$$V = k \frac{Q}{r} \Rightarrow P > R$$



$$V = \frac{kq_1}{r_1} + \frac{kq_2}{r_2} + \frac{k(-q_3)}{r_3}$$

$$= k \left(\frac{5}{8} + \frac{5}{8} + \frac{(-4)}{\sqrt{8^2 + 8^2}} \right)$$

$$= k \left(\frac{5}{8} + \frac{5}{8} + \frac{(-4)}{\sqrt{128}} \right)$$

"Persamaan Poisson" dan Persamaan Laplace

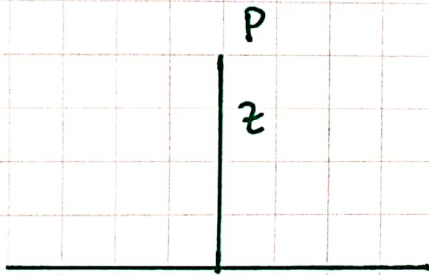
$$\vec{E} = -\nabla V$$

$$\nabla \cdot \vec{E} = -\nabla^2 V$$

$$\nabla \cdot \vec{E} = \frac{\rho}{\epsilon_0}$$

$$\boxed{\nabla^2 V = -\frac{\rho}{\epsilon_0}} \rightarrow \text{Poisson}$$

$$\boxed{\nabla^2 V = 0} \rightarrow \text{Laplace}$$



$$\vec{E} = \frac{q}{2\pi\epsilon_0 r}$$

$$\oint \vec{E} \cdot d\vec{a} = \frac{q \cdot l}{\epsilon_0}$$

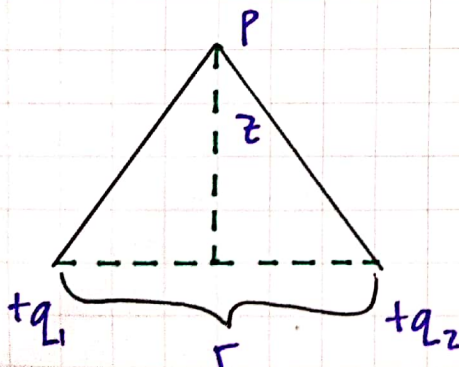
$$\vec{E} (2\pi r l) = \frac{q \cdot l}{\epsilon_0}$$

$$\boxed{\vec{E} = \frac{q}{2\pi\epsilon_0 r}}$$

$$V = \int \vec{E} \cdot d\vec{r}$$

$$= - \int \frac{q}{2\pi\epsilon_0} \frac{1}{r} dr$$

$$= - \frac{q}{2\pi\epsilon_0} \int \frac{1}{r} dr$$

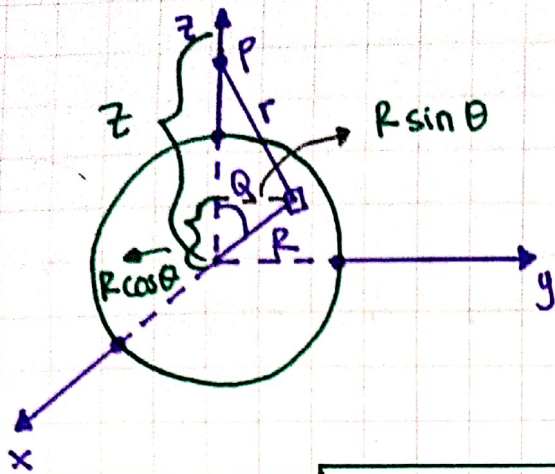


(Skalar)

$$V_P = ?$$

$$V_P = k \left[\frac{q_1}{\sqrt{(tr)^2 + z^2}} + \frac{q_2}{\sqrt{(tr)^2 + z^2}} \right]$$

"Contoh Soal"



$$V(P) = \frac{1}{4\pi\epsilon_0} \int \frac{\sigma}{r} da$$

$$r^2 = R^2 + z^2 - 2Rz \cos \theta$$

$$r = \sqrt{(R \sin \theta)^2 + (z - R \cos \theta)^2}$$

$$= \sqrt{R^2 \sin^2 \theta + z^2 \cos^2 \theta - 2Rz \cos \theta}$$

$$= \sqrt{R^2 (\sin^2 \theta + \cos^2 \theta) + z^2 - 2Rz \cos \theta}$$

$$= \sqrt{R^2 + z^2 - 2Rz \cos \theta}$$

$$V = \frac{1}{4\pi\epsilon_0} \int \frac{\sigma}{r} da \quad \rightarrow R^2 \sin \theta d\theta d\phi$$

$$= \frac{1}{4\pi\epsilon_0} \iint \frac{\sigma da}{(R^2 + z^2 - 2Rz \cos \theta)^{\frac{1}{2}}}$$

$$= \frac{\sigma}{4\pi\epsilon_0} \int_0^\pi \int_0^{2\pi} \frac{R^2 \sin \theta d\theta d\phi}{(R^2 + z^2 - 2Rz \cos \theta)^{\frac{1}{2}}}$$

$$= \frac{\sigma R^2 2\pi}{4\pi\epsilon_0} \int_0^\pi \frac{\sin \theta d\theta}{(R^2 + z^2 - 2Rz \cos \theta)^{\frac{1}{2}}}$$

$$V_p = \square \int_0^{\pi} \frac{d(\cos \theta)}{(R^2 + z^2 - 2Rz \cos \theta)^{\frac{1}{2}}}$$

$$= \square \int_0^{\pi} (R^2 + z^2 - 2Rz \cos \theta)^{\frac{1}{2}} d(\cos \theta)$$

$$= \square 2 (R^2 + z^2 - 2Rz \cos \theta)^{\frac{1}{2}} \Big|_0^{\pi}$$