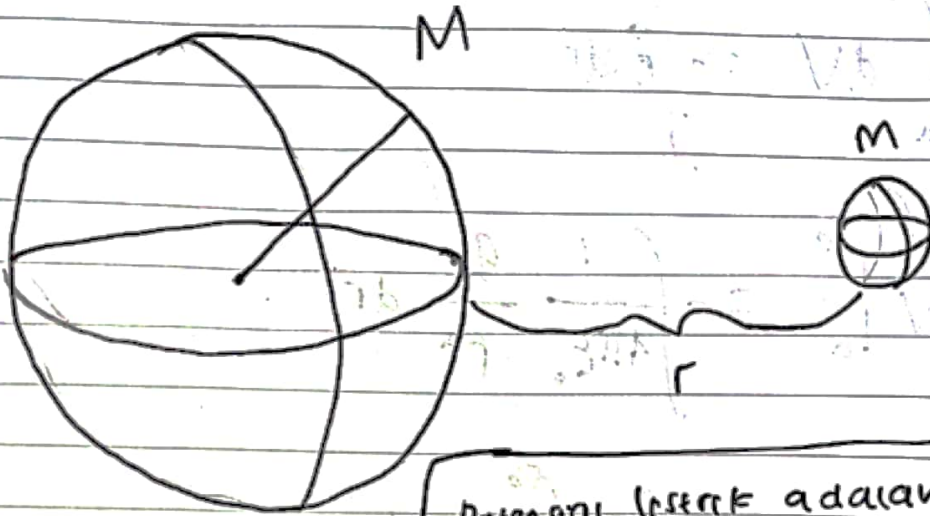


Potensial Listrik (Electric Potential)



$$W = G \frac{Mm}{r}$$

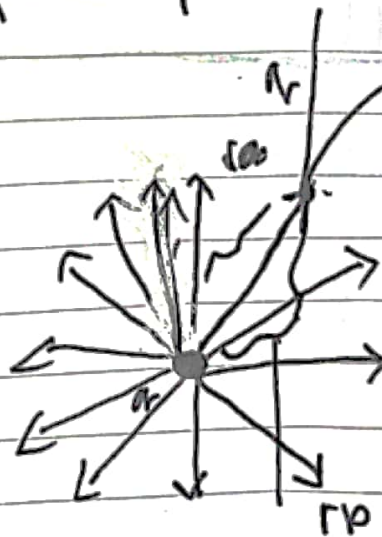
$$V = G \frac{M}{r}$$

$$V = \frac{W}{m}$$

$$V = \frac{W}{M} = G \frac{M}{r}$$

Potensial listrik adalah usaha untuk memindahkan satu satuan muatan listrik positif partikel tersebut.

$$V = \frac{W}{q}$$



$$\int_a^b dv = - \int_a^b \vec{E} dr$$

$$\int_a^b dV = - \int \vec{E} \cdot d\vec{r}$$

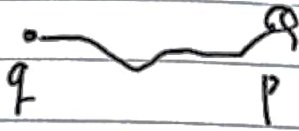
$$V \Big|_a^b = - \int \frac{1}{4\pi\epsilon_0} \frac{q}{r^2} dr$$

$$= - \frac{q}{4\pi\epsilon_0} \int_{r_a}^{r_b} \frac{1}{r^2} dr$$

$$= - \frac{q}{4\pi\epsilon_0} \left(- \frac{1}{r} \right) \Big|_{r_a}^{r_b}$$

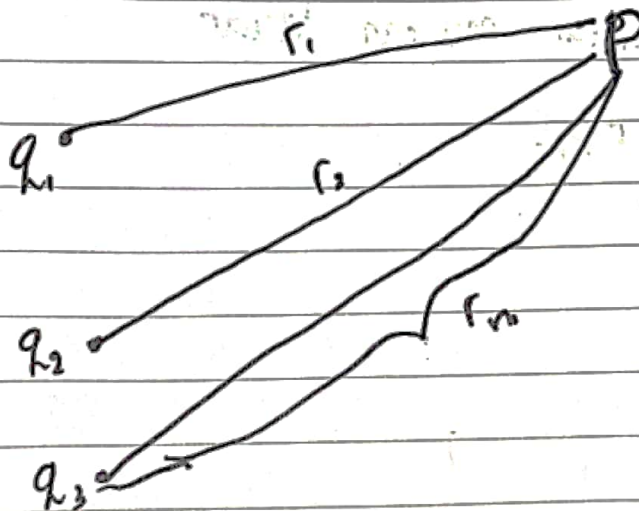
$$V_b - V_a = \frac{q}{4\pi\epsilon_0} \left(\frac{1}{r_b} - \frac{1}{r_a} \right)$$

$$V = k \frac{q}{r}$$



$$V = \frac{W}{Q}$$

$$V = k \frac{q}{r}$$



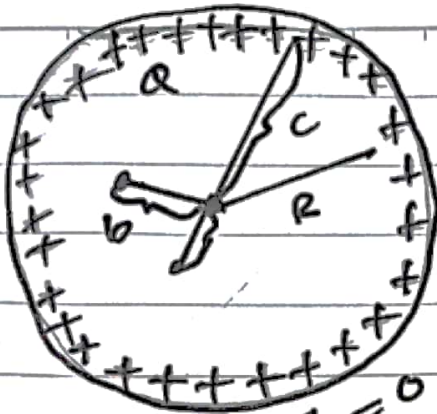
$$V = \frac{W}{q}$$

$$= \frac{\vec{F} \cdot \vec{s}}{q}$$

$$= k \frac{q}{r}$$

$$V_P = k \left[\frac{q_1}{r_1} + \frac{q_2}{r_2} + \frac{q_3}{r_3} \right]$$

$$= k \sum_{i=1}^n \frac{q_i}{r_i}$$



$$V_b - V_a = \frac{Q}{4\pi\epsilon_0} \left(\frac{1}{r_b} - \frac{1}{r_a} \right)$$

$$V_b - V_a = k \frac{Q}{R}$$

persamaan untuk muatan diluar

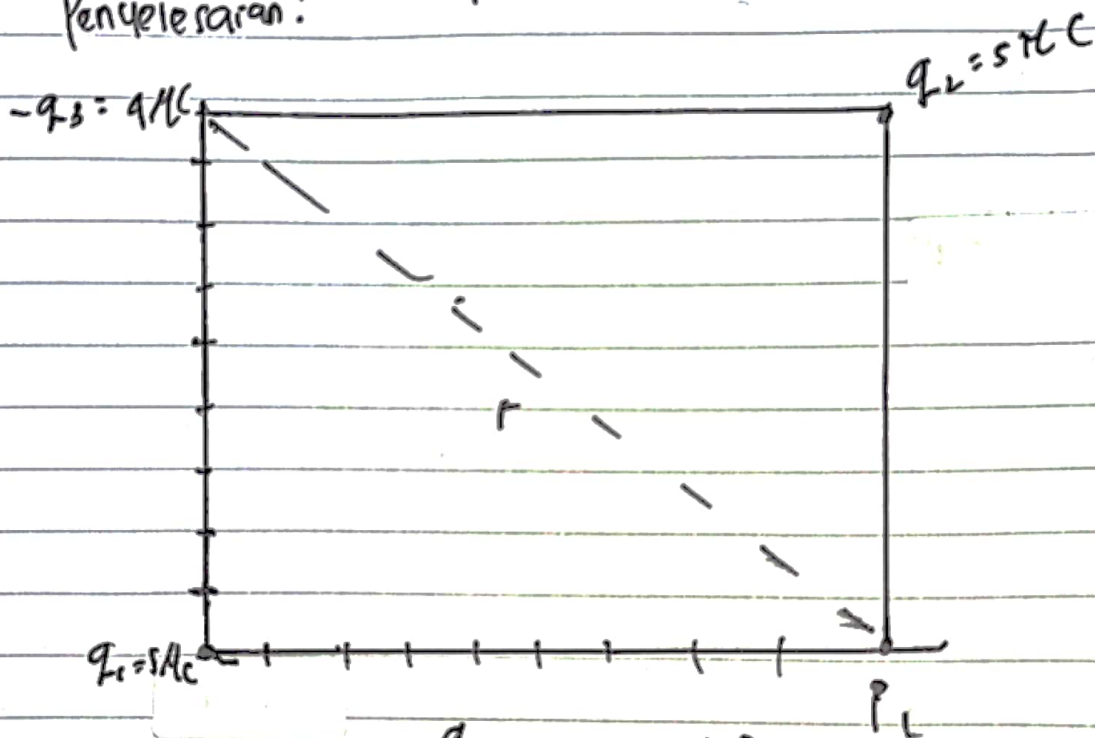
$$V = k \frac{Q}{r} \quad (r > R)$$

$$\left[\frac{1}{a} + \frac{1}{b} + \frac{1}{c} \right] + N$$

Example:

1. Gambarkan kasusnya!

Ada dua buah muatan positif besarnya 5 MC terletak pada sudut berlawanan yang panjang sisinya 8 cm . 1 muatan negatif diletakkan pada sudut yang kosong. Berapa potensial muatan pada sudut yang kosong?
Penyelesaian:



$$V = \frac{kq_1}{r_1} + \frac{kq_2}{r_2} + \frac{k(-q_3)}{r_3}$$

$$= k \left(\frac{5}{8} + \frac{5}{8} + \frac{(-4)}{\sqrt{8^2+8^2}} \right)$$

$$= k \left(\frac{5}{8} + \frac{5}{8} + \frac{(-4)}{\sqrt{128}} \right)$$

Persamaan poisson dan persamaan laplace

→ Persamaan poisson

$$E = -\nabla V$$

$$\nabla \cdot E = -\nabla^2 V$$

persamaan
gauss

$$\nabla \cdot \vec{E} = \frac{\rho}{\epsilon_0}$$

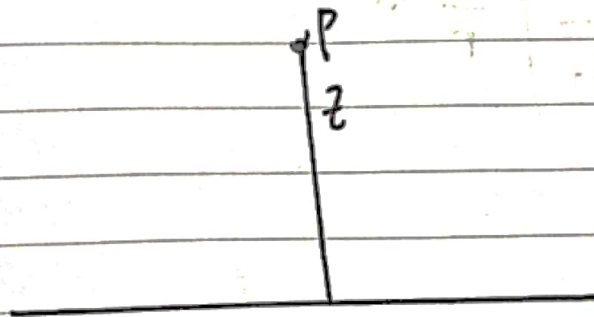
$$\nabla^2 V = \frac{\rho}{\epsilon_0} \rightarrow \text{poisson}$$

$$\nabla^2 V = 0 \text{ laplace}$$

→ Kajian persamaan gauss

$$\oint_S \vec{E} \cdot d\vec{a} = \int_V (\nabla \cdot \vec{E}) d\tau$$

→ Pada kawat lurus panjang



$$\vec{E} = \frac{\lambda}{2\pi\epsilon_0 r}$$

$$\oint \vec{E} \cdot d\vec{a} = \frac{\lambda \cdot l}{\epsilon_0}$$

$$\oint \vec{E} \cdot d\vec{a} = \frac{\lambda \cdot l}{\epsilon_0}$$

$$\vec{E} (2\pi r l) = \frac{\lambda \cdot l}{\epsilon_0}$$

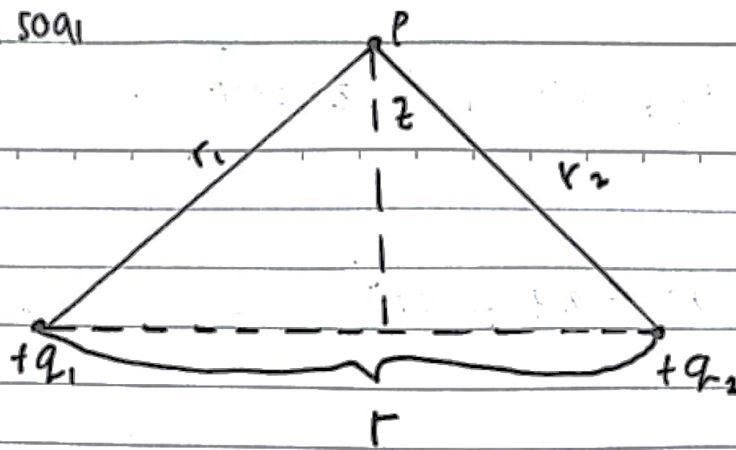
$$\vec{E} = \frac{\lambda}{2\pi \epsilon_0 r}$$

$$V = - \int \vec{E} \cdot d\vec{r}$$

$$= - \int \frac{\lambda}{2\pi \epsilon_0} \frac{1}{r} dr$$

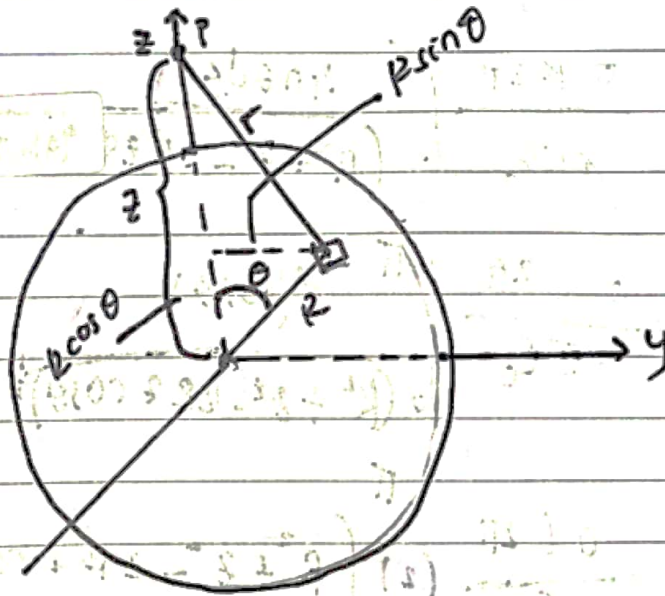
$$= - \frac{\lambda}{2\pi \epsilon_0} \int \frac{1}{r} dr$$

Contoh soal

 $V_P = ?$

$$V_P = K \left[\frac{q_1}{\sqrt{\left(\frac{1}{2}r\right)^2 + z^2}} + \frac{q_2}{\sqrt{\left(\frac{1}{2}r\right)^2 + z^2}} \right]$$

2.



$$r = \sqrt{(R \sin \theta)^2 + (z - R \cos \theta)^2}$$

$$= \sqrt{R^2 \sin^2 \theta + z^2 + R^2 \cos^2 \theta - 2zR \cos \theta}$$

$$r = \sqrt{R^2 (\sin^2 \theta + \cos^2 \theta) + z^2 - 2zR \cos \theta}$$

$$r = \sqrt{R^2 + z^2 - 2zR \cos \theta}$$

$$V = \frac{1}{4\pi\epsilon_0} \int \frac{\sigma da}{r}$$

$$= \frac{1}{4\pi\epsilon_0} \int \frac{\sigma da}{(R^2 + z^2 - 2zR \cos \theta)^{\frac{1}{2}}}$$

$$= \frac{\sigma}{4\pi\epsilon_0} \int_0^\pi \int_0^{2\pi} \frac{r^2 \sin \theta d\theta d\phi}{(R^2 + z^2 - 2zR \cos \theta)^{\frac{1}{2}}}$$

$$= \frac{\sigma R 2\pi}{4\pi\epsilon_0} \int_0^\pi \frac{\sin \theta d\theta}{(R^2 + z^2 - 2zR \cos \theta)^{\frac{1}{2}}}$$

$$V_P = \frac{\sigma R 2\pi}{4\pi\epsilon_0} \int_0^\pi \frac{d(\cos \theta)}{(R^2 + z^2 - 2zR \cos \theta)^{\frac{1}{2}}}$$

$$= \frac{\sigma R 2\pi}{2\pi} \int_0^\pi \left(R^2 + z^2 - 2zR \cos \theta \right)^{-\frac{1}{2}} d(\cos \theta)$$

$$= \frac{\sigma R 2\pi}{2\pi} (2) \left(R^2 + z^2 - 2zR \cos \theta \right)^{\frac{1}{2}} \Big|_0^\pi$$

$$= \frac{\sigma R^2 \pi}{2\pi} (2) \left[(R^2 + z^2 - 2Rz \cos \pi)^{\frac{1}{2}} - R^2 + z^2 - 2Rz \cos 0 \right]^{\frac{1}{2}}$$