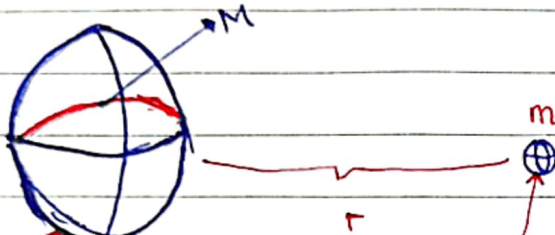


Diskrit } uru
Kontinu }

Potensial Listrik (Electro potential)



$$W = G \frac{Mm}{r}$$

$$V = G \frac{M}{r}$$

$$V = \frac{W}{m}$$

$$V = \frac{W}{M} = G \frac{M}{r}$$

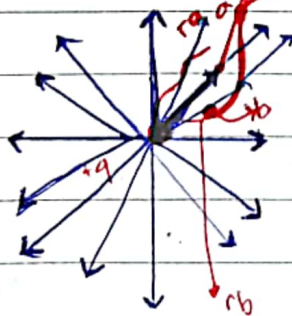
$$V = \frac{W}{q}$$

$$= \frac{f \cdot r}{q}$$

$$= K \frac{q_1 q_2}{r}$$

$$V = K \frac{q}{r}$$

$$V = \frac{W}{q}$$



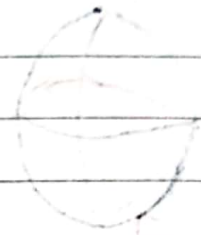
$$\int_a^b dV = - \int_a^b \vec{E} \cdot d\vec{r}$$

$$V \Big|_a^b = - \int_a^b \frac{1}{4\pi\epsilon_0} \frac{q}{r^2} dr$$

$$V_b - V_a = \frac{q}{4\pi\epsilon_0} \int_a^{rb} \frac{1}{r^2} dr$$

$$V_b - V_a = \frac{q}{4\pi\epsilon_0} \left(-\frac{1}{r} \right) \Big|_{ra}^{rb}$$

$$V_b - V_a = \frac{q}{4\pi\epsilon_0} \left(\frac{1}{rb} - \frac{1}{ra} \right)$$



Kasus.

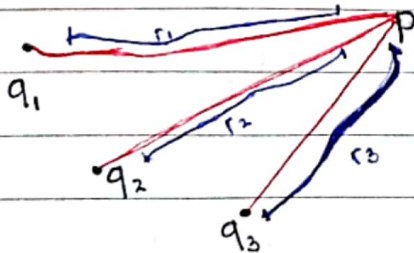
$$V = k \frac{q}{r}$$

$$V = k \frac{q}{r}$$

$$V = \frac{W}{Q}$$

$$V = k \frac{qQ}{r}$$

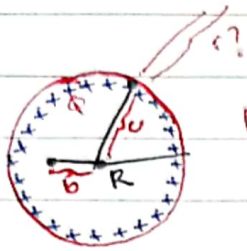
ex.



$$V = \frac{W}{q} = \frac{\vec{F}_1 \cdot \vec{s}}{q} = k \frac{q}{r}$$

$$V_P = k \left[\frac{q_1}{r_1} + \frac{q_2}{r_2} + \frac{q_3}{r_3} \right]$$

$$= k \sum_{i=1}^n \frac{q_i}{r_i}$$



potensial?

Potensial diluar??

potensialnya sama semua. $k \frac{Q}{R}$.

$$V_b - V_a = \frac{q}{4\pi\epsilon_0} \left(\frac{1}{r_b} - \frac{1}{r_a} \right)$$

$$V_b - V_a = k \frac{Q}{R}$$

potensial diluar

$$V = k \frac{Q}{r}, r > R.$$

$$V = \frac{kq_1}{r_1} + \frac{kq_2}{r_2} + \frac{kq_3}{r_3}$$

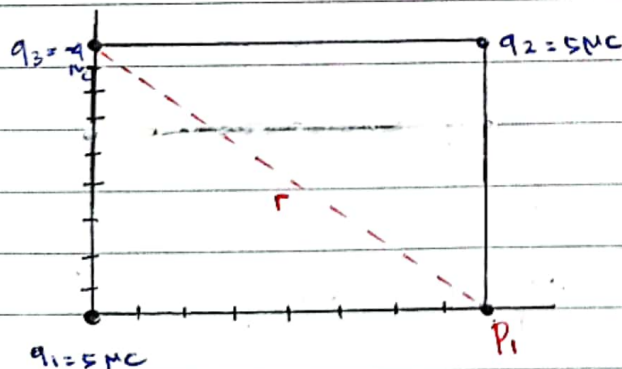
$$V = k \left(\frac{5}{8} + \frac{5}{8} + \frac{(-4)}{\sqrt{8^2+8^2}} \right)$$

$$V = k \left(\frac{5}{8} + \frac{5}{8} + \frac{(-4)}{\sqrt{128}} \right)$$

PERSAMAAN POISSON dan
PERSAMAAN LAPLACE

Soal!

1. Dua muatan titik positif sama besarnya $+5 \text{ nC}$ pada sumbu x. satu dipusat (0,0) dan yg lain pada (8,0) cm. Tentukan potensial di (a) titik P. pada posisi (8,6) cm.



1. POISSON.

$$\vec{E} = -\nabla V$$

$$\nabla \cdot \vec{E} = -\nabla^2 V$$

$$\nabla \cdot \vec{E} = \frac{\rho}{\epsilon_0}$$

$$\nabla^2 V = \frac{\rho}{\epsilon_0}$$

$$\nabla^2 V = 0 \text{ tdk ada sumber}$$

note: $\oint \vec{E} \cdot d\vec{a} = \oint (\nabla \cdot \vec{E}) d\vec{a} \quad (Gauss)$

potensial
 $\nabla^2 V = 0$ Laplace.

Gradien = perubahan (dlm fisika)

z

$$\vec{E} = \frac{\lambda}{2\pi\epsilon_0 r}$$

$$\oint \vec{E} da = \frac{\lambda \cdot l}{\epsilon_0}$$

$$\vec{E} (2\pi r l) = \frac{\lambda \cdot l}{\epsilon_0}$$

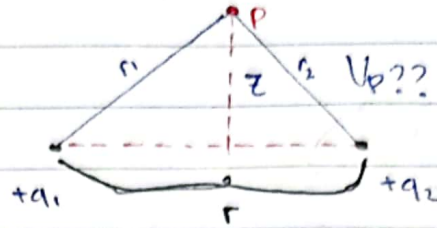
$$\vec{E} = \frac{\lambda}{2\pi\epsilon_0 r}$$

$$V = - \int \vec{E} dr$$

$$= - \int \frac{\lambda}{2\pi\epsilon_0} \frac{1}{r} dr$$

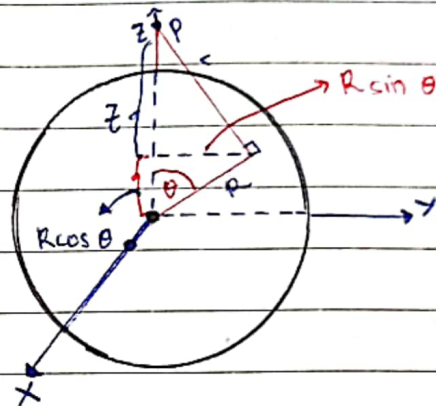
$$= - \frac{\lambda}{2\pi\epsilon_0} \int \frac{1}{r} dr$$

1.



$$V_p = k \left[\frac{q_1}{\sqrt{(\frac{1}{2}r)^2 + z^2}} + \frac{q_2}{\sqrt{(\frac{1}{2}r)^2 + z^2}} \right]$$

2.



$$V_p = \frac{1}{4\pi\epsilon_0} \int \frac{\sigma}{r} da$$

$$r = \sqrt{(R \sin \theta)^2 + (z - R \cos \theta)^2}$$

$$= \sqrt{R^2 \sin^2 \theta + z^2 + R^2 \cos^2 \theta - 2zR \cos \theta}$$

$$= \sqrt{R^2 (\sin^2 \theta + \cos^2 \theta) + z^2 - 2zR \cos \theta}$$

$$= \sqrt{R^2 + z^2 - 2zR \cos \theta}$$

Kalimat

lanjutan

$[dg \cdot d\Omega]$

$$V_p = \frac{1}{4\pi\epsilon_0} \int \frac{\sigma}{r} da$$

$$= \frac{1}{4\pi\epsilon_0} \iint \frac{\sigma da}{(R^2 + z^2 - 2Rz \cos\theta)^{1/2}}$$

$R^2 \sin\theta d\theta d\phi$

$$= \frac{\sigma}{4\pi\epsilon_0} \int_0^\pi \int_0^{2\pi} \frac{R^2 \sin\theta d\theta d\phi}{(R^2 + z^2 - 2Rz \cos\theta)^{1/2}}$$

$$= \frac{\sigma R^2 \pi}{4\pi\epsilon_0} \int_0^\pi \frac{\sin\theta d\theta}{(R^2 + z^2 - 2Rz \cos\theta)^{1/2}}$$

$$V_p = \frac{\sigma R^2 \pi}{4\pi\epsilon_0} \int_0^\pi \frac{d(\cos\theta)}{(R^2 + z^2 - 2Rz \cos\theta)^{1/2}}$$

$$= \frac{\sigma R^2 \pi}{4\pi\epsilon_0} \int_0^\pi (R^2 + z^2 - 2Rz \cos\theta)^{-1/2} d(\cos\theta)$$

$$= \frac{\sigma R^2 \pi}{4\pi\epsilon_0} \left[\frac{1}{-1/2 - 2} (R^2 + z^2 - 2Rz \cos\theta)^{-1/2} \right]_0^\pi$$

$(\frac{1}{-1/2 - 2}) = 2$