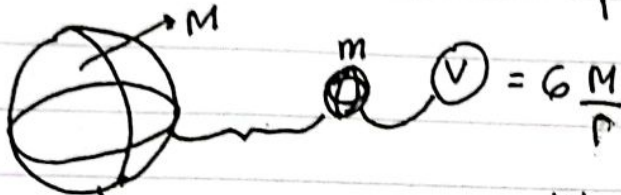


Potensial Listrik

(electric potensial)

$$W = G \frac{Mm}{r}$$



$$V = \frac{W}{m}$$

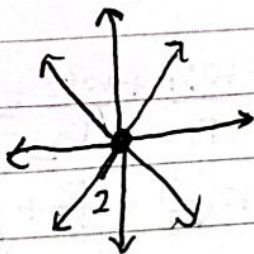
$$V = \frac{W}{m} = G \frac{M}{r}$$

$$V = \frac{W}{q} = \frac{F \cdot r}{q}$$

$$= \frac{k q_1 \cdot q_2}{r^2}$$

$$V = K \frac{q}{r}$$

$$\int_a^b dv = - \int \vec{E} \cdot d\vec{r}$$



$$V \Big|_a^b = - \int \frac{1}{4\pi\epsilon_0} \frac{q}{r^2} dr$$

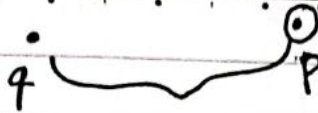
$$= - \frac{q}{4\pi\epsilon_0} \int_a^b \frac{1}{r^2} dr$$

$$= - \frac{q}{4\pi\epsilon_0} \left(- \frac{1}{r} \Big|_a^b \right)$$

$$= V_b - V_a = \frac{q}{4\pi\epsilon_0} \left(\frac{1}{r_b} - \frac{1}{r_a} \right)$$

$$V = k \frac{q}{r}$$

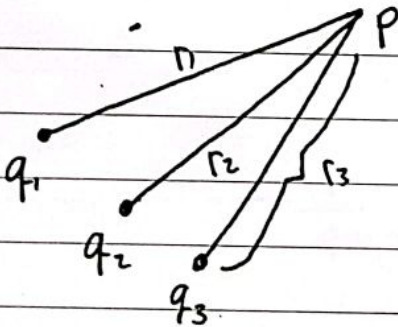
Kasus



$$k \frac{q \cdot d}{r}$$

$$V = \frac{W}{Q}$$

$$P = k \frac{q}{r}$$



$$V_P = k \left[\frac{q_1}{r_1} + \frac{q_2}{r_2} + \frac{q_3}{r_3} \right]$$

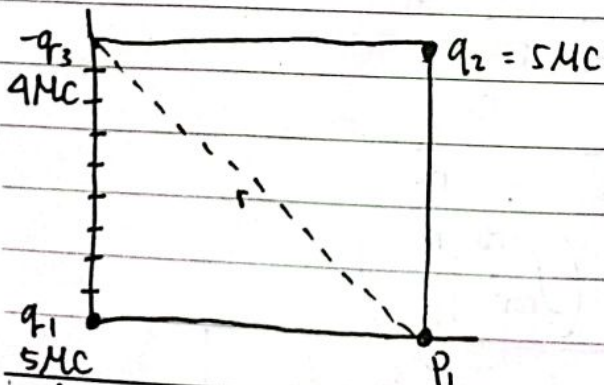
$$= k \sum_{i=1}^n \frac{q_i}{r_i}$$

$$V = \frac{W}{q} = \frac{P \cdot r}{q} = \left(k \frac{q}{r} \right)$$



$$V = k \frac{Q}{r}, r > R$$

Contoh :



$$\text{Jawab : } V = \frac{kq_1}{r_1} + \frac{kq_2}{r_2} + \frac{k(-q_3)}{r_3}$$

$$= k \left(\frac{5}{8} + \frac{5}{8} + \frac{(-4)}{\sqrt{8^2+8^2}} \right)$$

$$= k \left(\frac{5}{8} + \frac{5}{8} + \frac{(-4)}{\sqrt{128}} \right)$$

Persamaan Poisson dan Persamaan Laplace

$$\vec{E} = -\nabla V$$

$$\nabla \cdot \vec{E} = -\nabla^2 V$$

$$\nabla \cdot \vec{E} = \frac{\rho}{\epsilon_0}$$

$$\boxed{\nabla^2 V = -\frac{\rho}{\epsilon_0}} \rightarrow \text{Poisson}$$

$$\boxed{\nabla^2 V = 0} \rightarrow \text{Laplace}$$

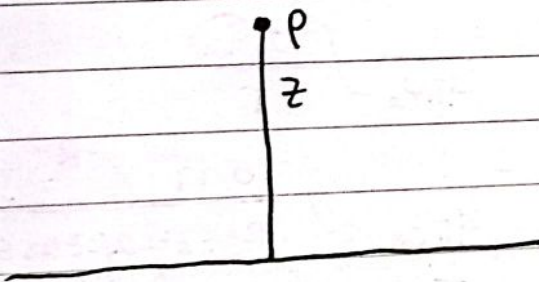
Potensial

Note :

(Gaus)

$$\oint_S \vec{E} \cdot d\vec{a} = \oint_V (\nabla \cdot \vec{E}) dV$$

Gradien = perubahan (dlm fisika)



$$\rightarrow \vec{E} = \frac{\lambda}{2\pi\epsilon_0 r}$$

$$\oint \vec{E} \cdot d\vec{a} = \frac{\lambda \cdot l}{\epsilon_0}$$

$$\vec{E} (2\pi r l) = \frac{\lambda \cdot l}{\epsilon_0}$$

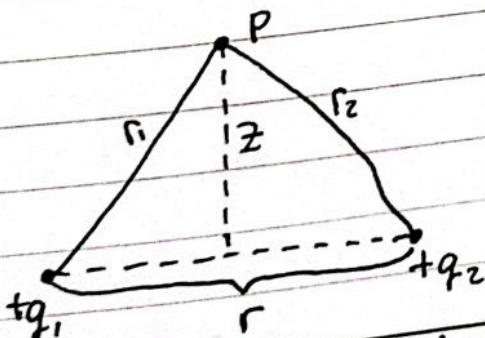
$$V = -\int \vec{E} \cdot d\vec{r}$$

$$= -\int \frac{\lambda}{2\pi\epsilon_0} \frac{1}{r} dr$$

$$= -\frac{\lambda}{2\pi\epsilon_0} \int \frac{1}{r} dr$$

$$\boxed{\vec{E} = \frac{\lambda}{2\pi\epsilon_0 r}}$$

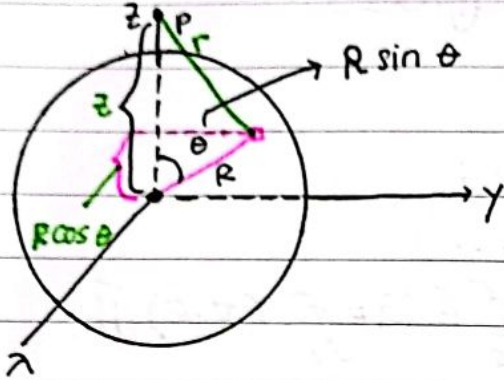
Contoh :



$$V_P = ?$$

$$V_P = K \left[\frac{q_1}{\sqrt{(\frac{1}{2}r)^2 + z^2}} + \frac{q_2}{\sqrt{(\frac{1}{2}r)^2 + z^2}} \right]$$

Contoh :



$$\begin{aligned}
 r &= \sqrt{(R \sin \theta)^2 + (z - R \cos \theta)^2} \\
 &= \sqrt{R^2 \sin^2 \theta + z^2 + R^2 \cos^2 \theta - 2zR \cos \theta} \\
 &= \sqrt{R^2 (\sin^2 \theta + \cos^2 \theta) + z^2 - 2zR \cos \theta} \\
 &= \sqrt{R^2 + z^2 - 2zR \cos \theta}
 \end{aligned}$$

$$V(p) = \frac{1}{4\pi\epsilon_0} \int \frac{\sigma da}{r}$$

$$r^2 = R^2 + z^2 - 2zR \cos \theta$$

$$dg = \sigma da$$

contoh :

$$V_p = \frac{\sigma R 2\pi}{4\pi\epsilon_0} \int_0^\pi \frac{d(\cos \theta)}{(R^2 + z^2 - 2zR \cos \theta)^{1/2}}$$

$$= \frac{\sigma R 2\pi}{4\pi\epsilon_0} \int_0^\pi (R^2 + z^2 - 2zR \cos \theta)^{-1/2}$$

$$(\cos \theta)$$

$$= \frac{\sigma R 2\pi}{4\pi\epsilon_0} \left[2 (R^2 + z^2 - 2zR \cos \theta)^{1/2} \right]_0^\pi$$

$1 : \frac{1}{2}$

$$V = \frac{1}{4\pi\epsilon_0} \int \frac{\sigma da}{r}$$

$$= \frac{1}{4\pi\epsilon_0} \iint \frac{\sigma da}{(R^2 + z^2 - 2zR \cos \theta)^{1/2}}$$

$$= \frac{\sigma}{4\pi\epsilon_0} \int_0^\pi \int_0^{2\pi} \frac{R^2 \sin \theta d\theta d\phi}{(R^2 + z^2 - 2zR \cos \theta)^{1/2}}$$

$$= \frac{\sigma R 2\pi}{4\pi\epsilon_0} \int_0^\pi \frac{\sin \theta d\theta}{(R^2 + z^2 - 2zR \cos \theta)^{1/2}}$$