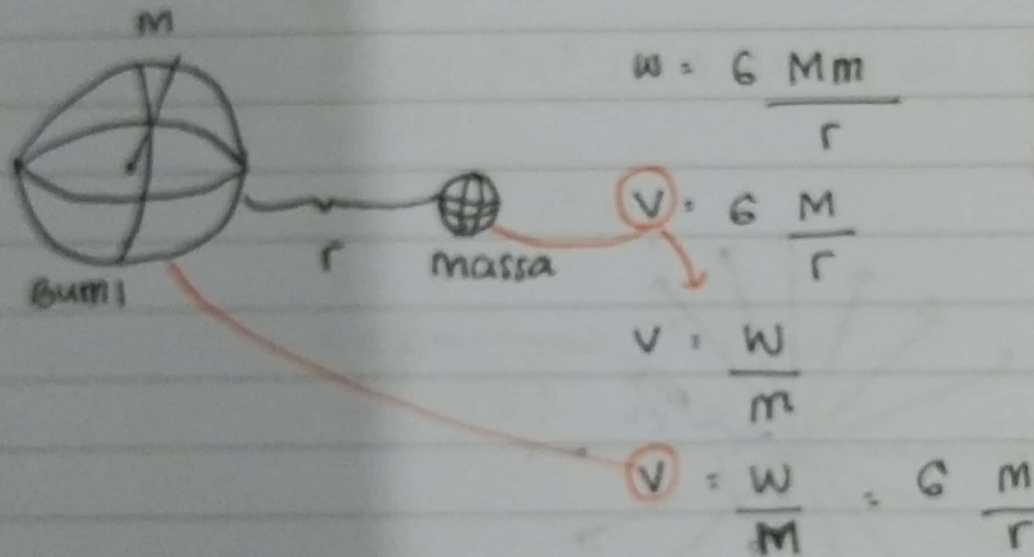


Potensial Listrik (electric Potential)

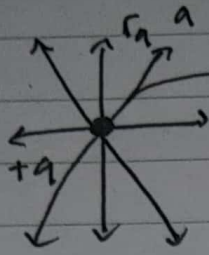


$$V = \frac{W}{Q} = \frac{F \cdot r}{Q}$$

$$= k \frac{q_1 q_2 \cdot r}{Q}$$

$$V = k \frac{q}{r}$$

Potensial listrik adalah usaha untuk melakukan perpindahan.



$$\int_a^b dv = - \int_a^b \vec{E} \cdot d\vec{r}$$

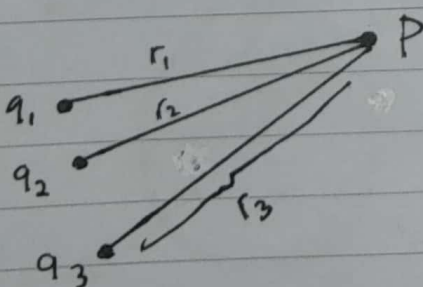
$$V \Big|_a^b = - \int_a^b \frac{1}{4\pi\epsilon_0} \frac{q}{r^2} dr$$

$$= - \frac{q}{4\pi\epsilon_0} \int_{r_a}^{r_b} \frac{1}{r^2} dr = - \frac{q}{4\pi\epsilon_0} \left(-\frac{1}{r} \Big|_{r_a}^{r_b} \right)$$

$$= V_b - V_a = \frac{q}{4\pi\epsilon_0} \left(\frac{1}{r_b} - \frac{1}{r_a} \right)$$

$$V = k \frac{q}{r}$$

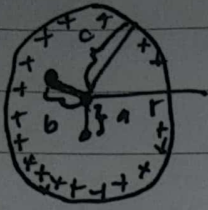
Diagram showing two point charges q and Q separated by a distance r . The work done W to move charge Q from infinity to distance r is $W = \frac{kqQ}{r}$. The potential V is defined as $V = \frac{W}{Q} \rightarrow V = k \frac{q}{r}$.



$$V_P = k \left[\frac{q_1}{r_1} + \frac{q_2}{r_2} + \frac{q_3}{r_3} \right]$$

$$= k \sum_{i=1}^n \frac{q_i}{r_i}$$

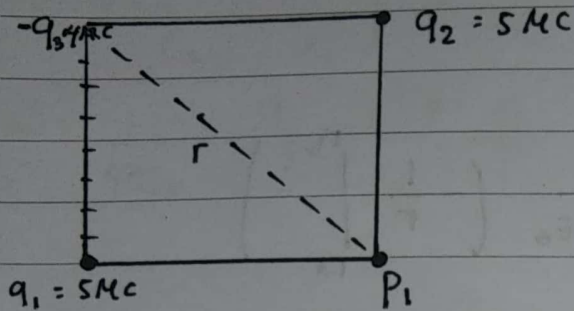
$$V = \frac{W}{q} = \frac{\vec{P} \cdot \vec{r}}{q} = k \frac{q}{r}$$



$$V_b - V_a = K q \left(\frac{1}{r_b} - \frac{1}{r_a} \right)$$

$$V_b - V_a = K \frac{Q}{R} \quad \text{didalam}$$

$$V = K \frac{Q}{r}, \quad r > R \quad \text{diluar}$$



$$V = \frac{Kq_1}{r_1} + \frac{Kq_2}{r_2} + \frac{K(-q_3)}{r_3}$$

$$= K \left(\frac{5}{8} + \frac{5}{8} + \frac{(-4)}{\sqrt{8^2 + 8^2}} \right)$$

$$= K \left(\frac{5}{8} + \frac{5}{8} + \frac{(-4)}{\sqrt{128}} \right)$$

▷ Persamaan Poisson dan Persamaan Laplace

$$\vec{E} = -\nabla V$$

$$\nabla \cdot \vec{E} = -\nabla^2 V$$

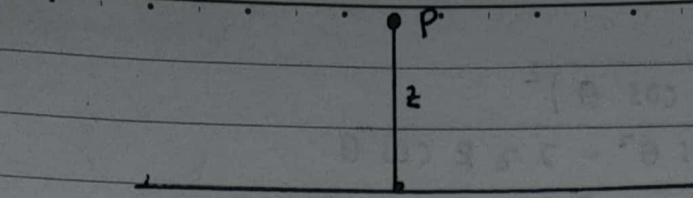
$$\nabla \cdot \vec{E} = \frac{\rho}{\epsilon_0}$$

$$\nabla^2 V = \frac{\rho}{\epsilon_0} \quad \text{Poisson}$$

$$\nabla^2 V = 0 \quad \text{Laplace}$$

1)

V



$$\vec{E} = \frac{\lambda}{2\pi\epsilon_0 r}$$

$$V = \int \vec{E} \cdot d\vec{r}$$

$$\oint \vec{E} \cdot d\vec{a} = \frac{\lambda \cdot l}{\epsilon_0}$$

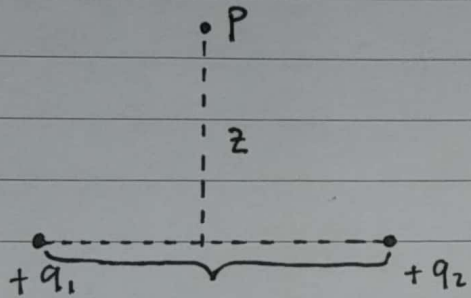
$$= - \int \frac{\lambda}{2\pi\epsilon_0} \frac{1}{r} dr$$

$$\vec{E} (2\pi r l) = \frac{\lambda \cdot l}{\epsilon_0}$$

$$= - \frac{\lambda}{2\pi\epsilon_0} \int \frac{1}{r} dr$$

$$\vec{E} = \frac{\lambda}{2\pi\epsilon_0 r}$$

4



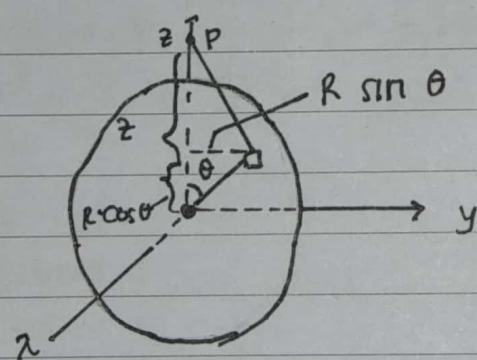
$$V_P = k \left[\frac{q_1}{\sqrt{(1/2 r)^2 + z^2}} + \frac{q_2}{\sqrt{(1/2 r)^2 + z^2}} \right]$$

D B

lit

jal

t



$$V_{cp} = \frac{1}{4\pi\epsilon_0} \int \frac{\sigma}{r} da$$

$$r^2 = R^2 + z^2 - 2Rz \cos \theta$$

$$r = \sqrt{(R \sin \theta)^2 + (z - R \cos \theta)^2}$$

$$= \sqrt{R^2 \sin^2 \theta + z^2 + R^2 \cos^2 \theta - 2zR \cos \theta}$$

$$= \sqrt{R^2 (\sin^2 \theta + \cos^2 \theta) + z^2 - 2zR \cos \theta}$$

$$= \sqrt{R^2 + z^2 - 2zR \cos \theta}$$

$$V = \frac{1}{4\pi\epsilon_0} \int \frac{\sigma da}{r}$$

$$= \frac{1}{4\pi\epsilon_0} \iint \frac{\sigma da}{(R^2 + z^2 - 2Rz \cos \theta)^{\frac{1}{2}}}$$

$$= \frac{\sigma}{4\pi\epsilon_0} \int_0^\pi \int_0^{2\pi} \frac{r^2 \sin \theta d\theta d\phi}{(R^2 + z^2 - 2Rz \cos \theta)^{\frac{1}{2}}}$$

$$= \frac{\sigma R^2 2\pi}{4\pi\epsilon_0} \int_0^\pi \frac{\sin \theta d\theta}{(R^2 + z^2 - 2Rz \cos \theta)^{\frac{1}{2}}}$$

$$V_p = \square \int_0^\pi \frac{d(\cos \theta)}{(R^2 + z^2 - 2Rz \cos \theta)^{\frac{1}{2}}}$$

$$= \square \int_0^\pi (R^2 + z^2 - 2Rz \cos \theta)^{-\frac{1}{2}} d(\cos \theta)$$

$$= \square 2 (R^2 + z^2 - 2Rz \cos \theta)^{\frac{1}{2}} \Big|_0^\pi$$