

$$\frac{q}{4\pi\epsilon_0} \int_{r_1}^{r_2} r^{-2} dr$$

$$= \square \int_{r_1}^{r_2} r^{-2} dr$$

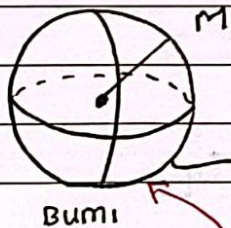
$$= \square \left(-\frac{1}{r} \right) \Big|_{r_1}^{r_2}$$

$$= \square \left(\frac{1}{r_2} - \frac{1}{r_1} \right)$$

$$V = \frac{1}{4\pi\epsilon_0} \frac{q}{r} = k \frac{q}{r}$$

1 April 2024

Potensial listrik (Elektrik potensial)



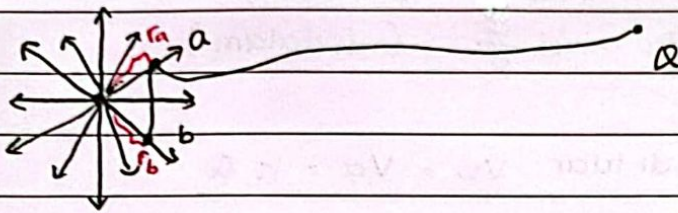
$$W = G \frac{Mm}{r}$$

$$V = G \frac{M}{r}$$

$$V = \frac{W}{m}$$

$$V = \frac{W}{M} = G \frac{M}{r}$$

$V = \frac{W}{Q} = \frac{F \cdot r}{Q}$ $= k \frac{q_1 \cdot Q}{r^2} \cdot \frac{r}{Q}$ $V = k \frac{q_1}{r}$



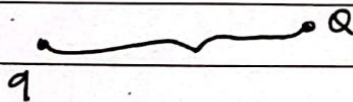
$$\int dv = - \int \vec{E} \cdot d\vec{r}$$

$$V \Big|_a^b = - \int_{r_a}^{r_b} \frac{1}{4\pi\epsilon_0} \frac{q}{r^2} dr$$

$$= - \frac{q}{4\pi\epsilon_0} \int_{r_a}^{r_b} \frac{1}{r^2} dr$$

$$= - \frac{q}{4\pi\epsilon_0} \left(- \frac{1}{r} \Big|_{r_a}^{r_b} \right)$$

$$= V_b - V_a = \frac{q}{4\pi\epsilon_0} \left(\frac{1}{r_b} - \frac{1}{r_a} \right)$$

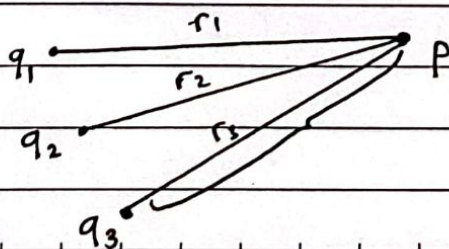


$$V = k \frac{q}{r}$$

$$V = \frac{W}{q}$$

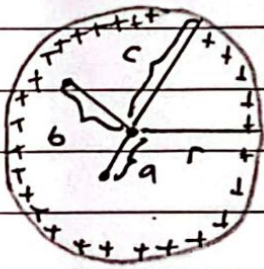
$$k \frac{qQ}{r}$$

$$\rightarrow V = k \frac{q}{r}$$



$$V_P = k \left[\frac{q_1}{r_1} + \frac{q_2}{r_2} + \frac{q_3}{r_3} \right]$$

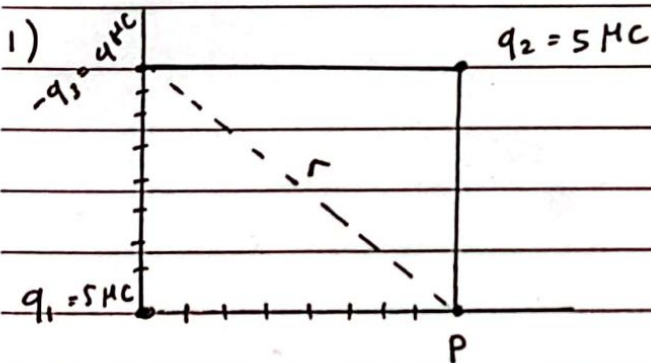
$$= k \sum_{i=1}^n \frac{q_i}{r_i}$$



$$V_b - V_a = \frac{q}{4\pi\epsilon_0} \left(\frac{1}{r_b} - \frac{1}{r_a} \right)$$

$$V_b - V_a = k \frac{Q}{R} \quad (\text{di dalam})$$

$$\text{kalau di luar } V_b = V_a = k \frac{Q}{r}$$



$$V = k \frac{q_1}{r_1} + k \frac{q_2}{r_2} + k \frac{(-q_3)}{r_3}$$

$$= k \left(\frac{5}{8} + \frac{5}{8} + \frac{(-4)}{\sqrt{8^2 + 8^2}} \right)$$

$$= k \left(\frac{5}{8} + \frac{5}{8} + \frac{(-4)}{\sqrt{128}} \right)$$

► Persamaan Poisson dan Persamaan Laplace

$$\vec{E} = -\nabla V$$

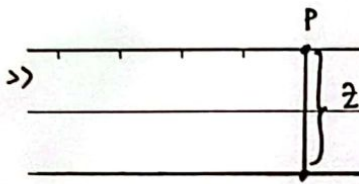
$$\nabla \cdot \vec{E} = -\nabla^2 V$$

$$\nabla \cdot \vec{E} = \frac{\rho}{\epsilon_0}$$

$$\nabla^2 V = -\frac{\rho}{\epsilon_0} \quad \text{poisson}$$

$$\nabla^2 V = 0 \quad \text{laplace}$$

Gradien : perubahan suhu



$$\vec{E} = \frac{\lambda}{2\pi\epsilon_0 r}$$

$$V = - \int \vec{E} \cdot d\vec{r}$$

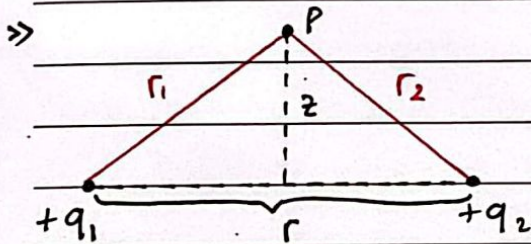
$$\oint \vec{E} \cdot d\vec{a} = \frac{\lambda \cdot l}{\epsilon_0}$$

$$= - \int \frac{\lambda}{2\pi\epsilon_0} \frac{1}{r} dr$$

$$\vec{E}(2\pi r l) = \frac{\lambda \cdot l}{\epsilon_0}$$

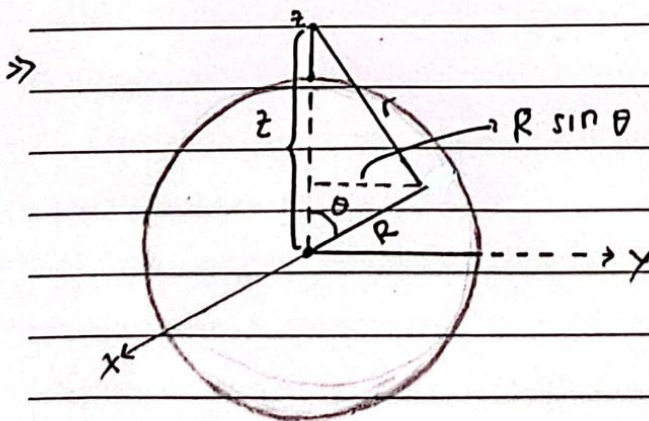
$$= - \frac{\lambda}{2\pi\epsilon_0} \int \frac{1}{r} dr$$

$$\vec{E} = \frac{\lambda}{2\pi\epsilon_0 r}$$



$V_P \dots ?$

$$V_P = k \left[\frac{q_1}{\sqrt{(\frac{1}{2}r)^2 + z^2}} + \frac{q_2}{\sqrt{(\frac{1}{2}r)^2 + z^2}} \right]$$



$$\begin{aligned}
 r &= \sqrt{(R \sin \theta)^2 + (z - R \cos \theta)^2} \\
 &= \sqrt{R^2 \sin^2 \theta + z^2 + R^2 \cos^2 \theta - 2zR \cos \theta} \\
 &= \sqrt{R^2 (\sin^2 \theta + \cos^2 \theta) + z^2 - 2zR \cos \theta} \\
 &= \sqrt{R^2 + z^2 - 2zR \cos \theta}
 \end{aligned}$$

$$\begin{aligned}
 V &= \frac{1}{4\pi\epsilon_0} \int \frac{\sigma da}{r} \\
 &= \frac{1}{4\pi\epsilon_0} \iint \frac{\sigma (da)}{(R^2 + z^2 - 2zR \cos \theta)^{1/2}} \quad R^2 \sin \theta d\theta d\phi \\
 &= \frac{\sigma}{4\pi\epsilon_0} \int_0^\pi \int_0^{2\pi} \frac{(r^2) \sin \theta d\theta d\phi}{(R^2 + z^2 - 2zR \cos \theta)^{1/2}} \quad \begin{array}{l} r \text{ disini adalah } R \text{ besar di gambar} \\ R \text{ disini adalah } r \text{ kecil pd gambar} \end{array}
 \end{aligned}$$

$$\begin{aligned}
 &= \frac{\sigma R 2\pi}{4\pi\epsilon_0} \int_0^\pi \frac{\sin \theta d\theta}{(R^2 + z^2 - 2zR \cos \theta)^{1/2}} \\
 &= \frac{\sigma R 2\pi}{4\pi\epsilon_0} \int_0^\pi \frac{d(\cos \theta)}{(R^2 + z^2 - 2zR \cos \theta)^{1/2}} \\
 &= \frac{\sigma R 2\pi}{4\pi\epsilon_0} \int_0^\pi (R^2 + z^2 - 2zR \cos \theta)^{-1/2} d(\cos \theta) \\
 &= \frac{\sigma R 2\pi}{4\pi\epsilon_0} 2 \left(R^2 + z^2 - 2zR \cos \theta \right)^{1/2} \Big|_0^\pi
 \end{aligned}$$