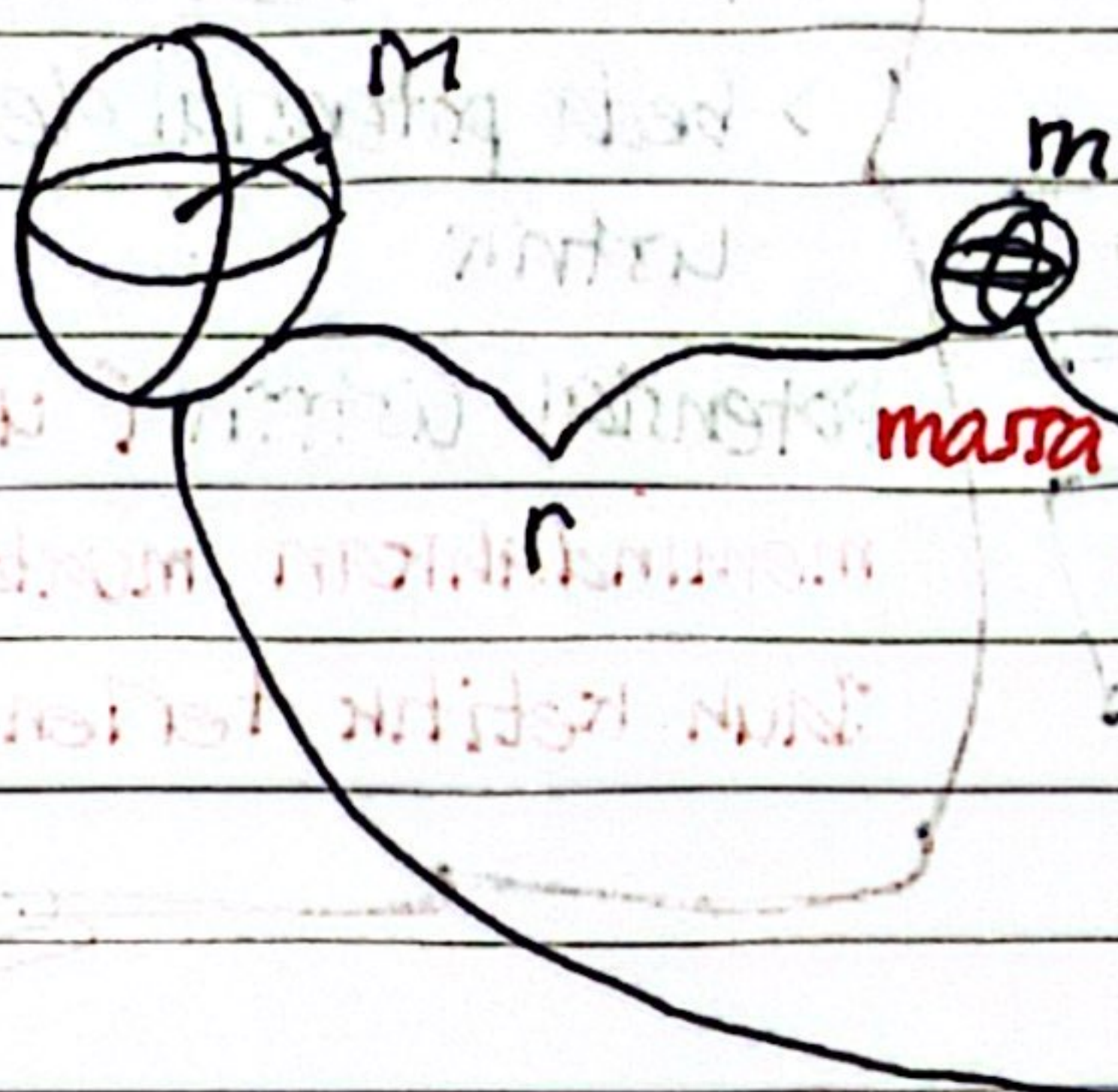


POTENSIAL LISTRIK / electric potential



$$W = G \frac{M \cdot m}{r}$$

$$V = G \frac{M}{r}$$

$$V = \frac{W}{m}$$

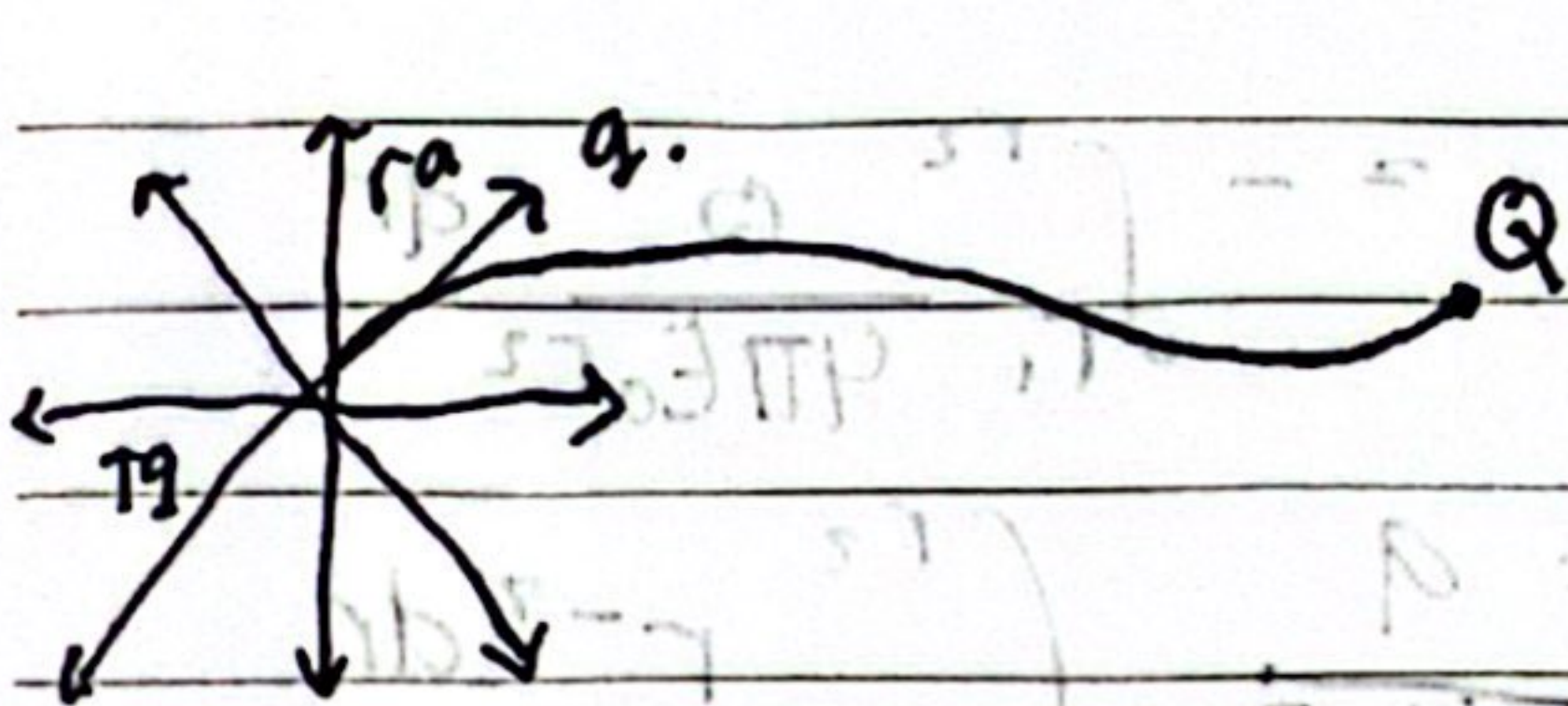
$$V = \frac{W}{M} = G \frac{m}{r}$$

$$V = \frac{W}{q} = \frac{F \cdot r}{q}$$

$$= k \frac{q_1 q_2}{r^2} r$$

$$V = k \frac{q}{r}$$

$$V = \frac{W}{q}$$



$$\int_a^b dv = - \int E dr$$

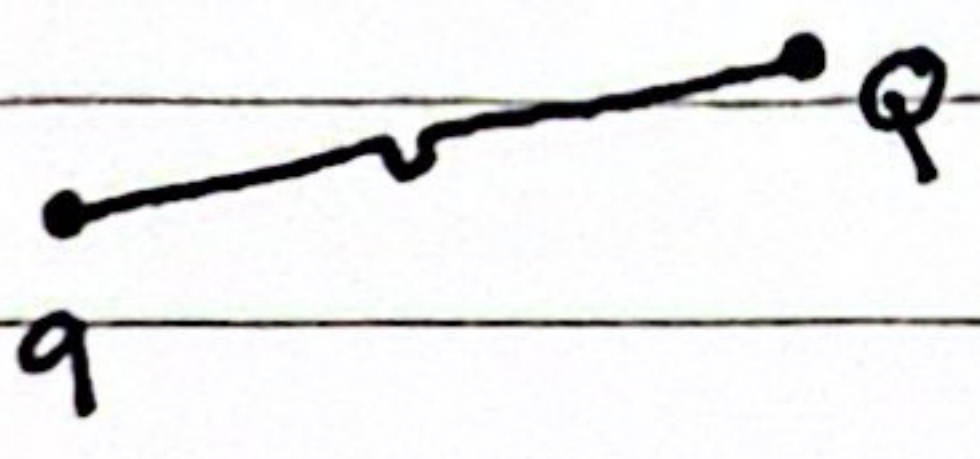
$$V \Big|_a^b = - \int \frac{1}{4\pi\epsilon_0} \frac{q}{r^2} dr$$

$$= - \frac{q}{4\pi\epsilon_0} \int_a^b \frac{1}{r^2} dr$$

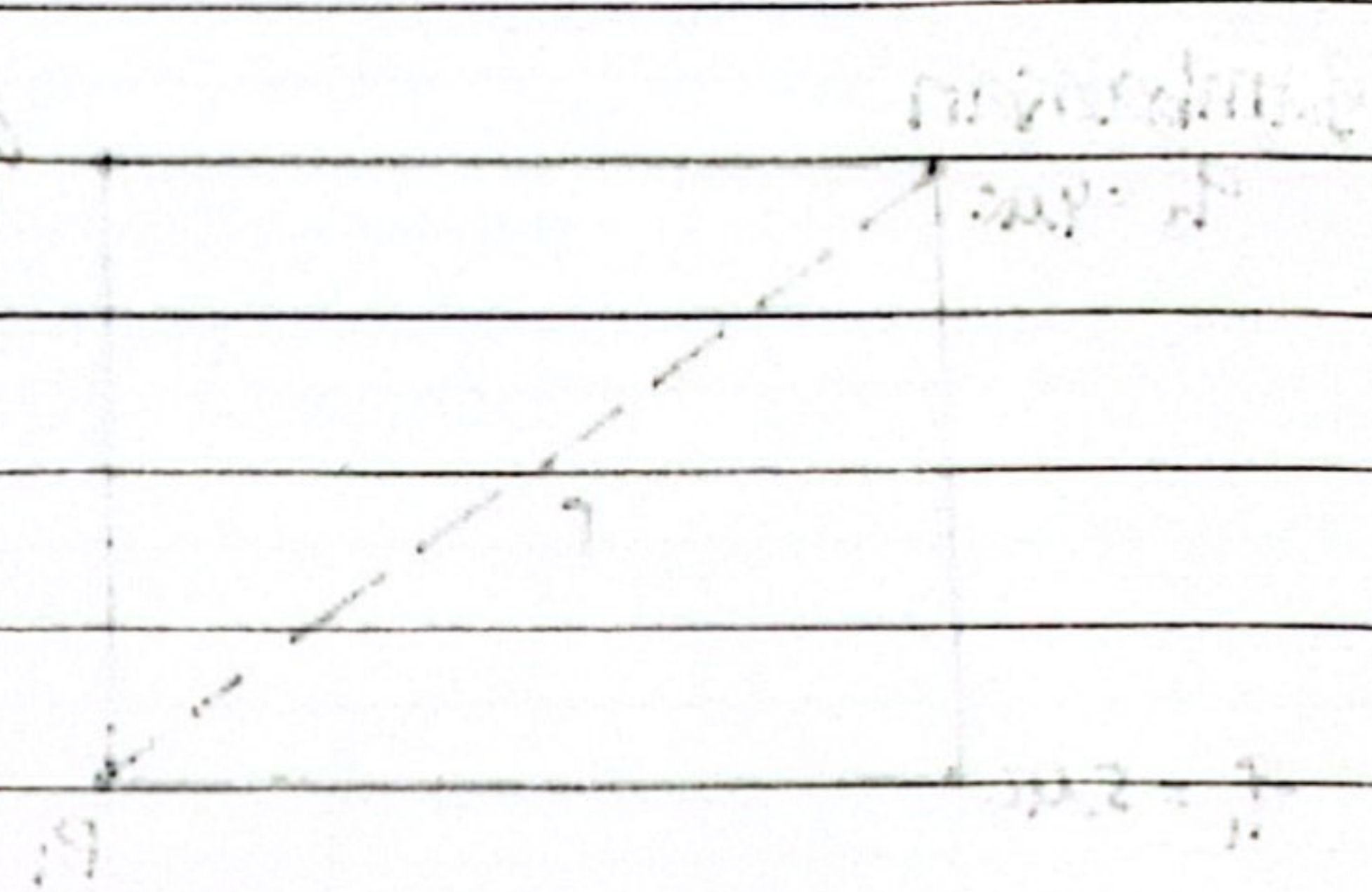
$$= - \frac{q}{4\pi\epsilon_0} \left(-\frac{1}{r} \Big|_a^b \right)$$

$$= V_b - V_a = \frac{q}{4\pi\epsilon_0} \left(\frac{1}{r_b} - \frac{1}{r_a} \right)$$

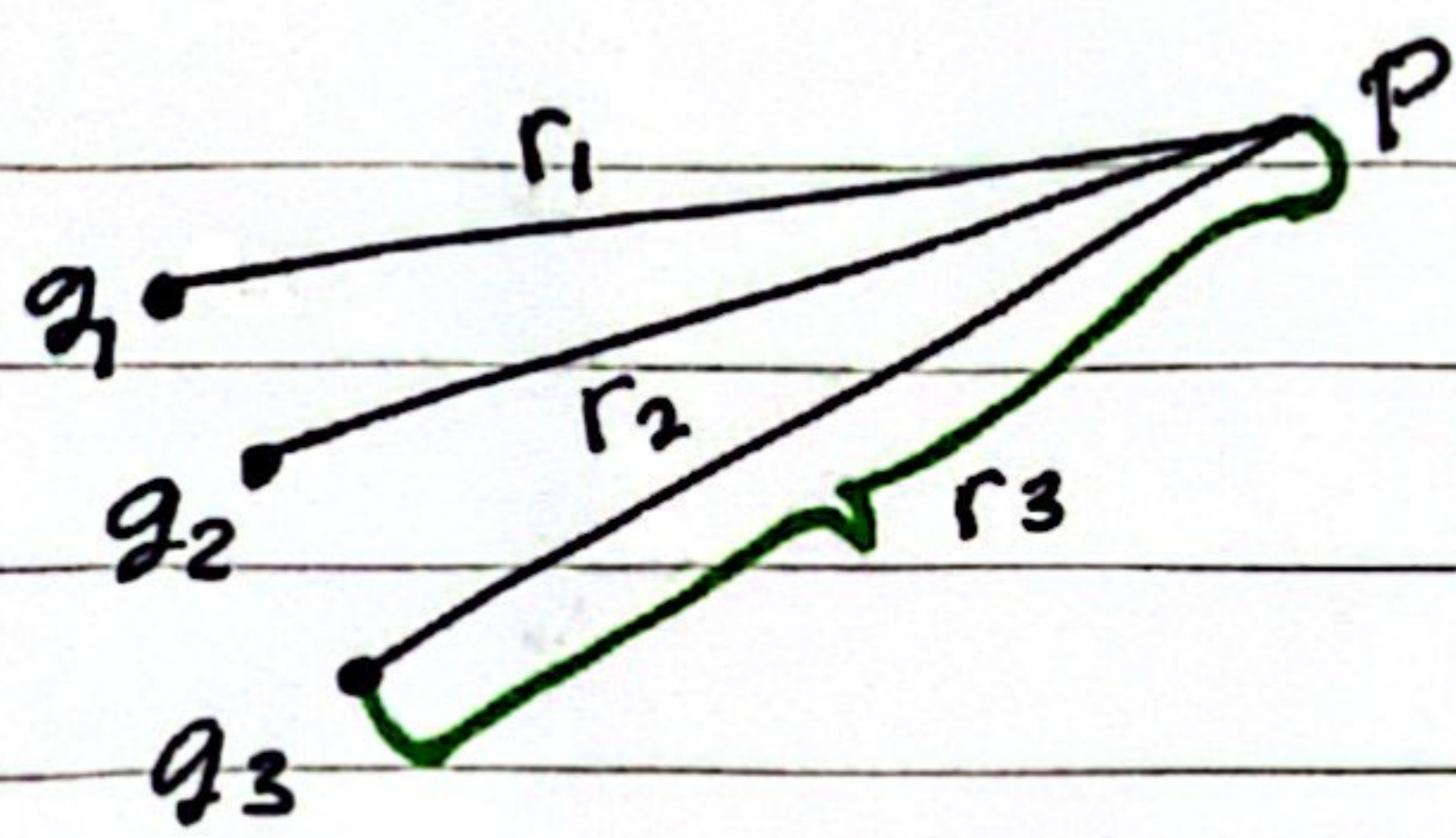
$$V = k \frac{q}{r}$$



$$V = \frac{W}{Q} \rightarrow V = k \frac{q}{r}$$

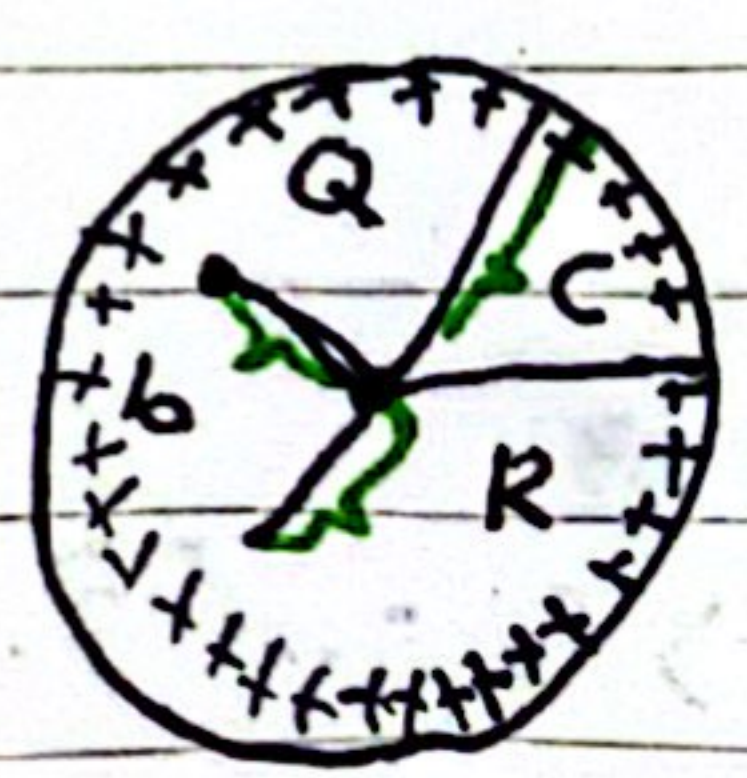


$$V_1 + V_2 + V_3 = V$$



$$V_P = k \left[\frac{q_1}{r_1} + \frac{q_2}{r_2} + \frac{q_3}{r_3} \right]$$

$$= k \sum_{i=1}^n \frac{q_i}{r_i}$$



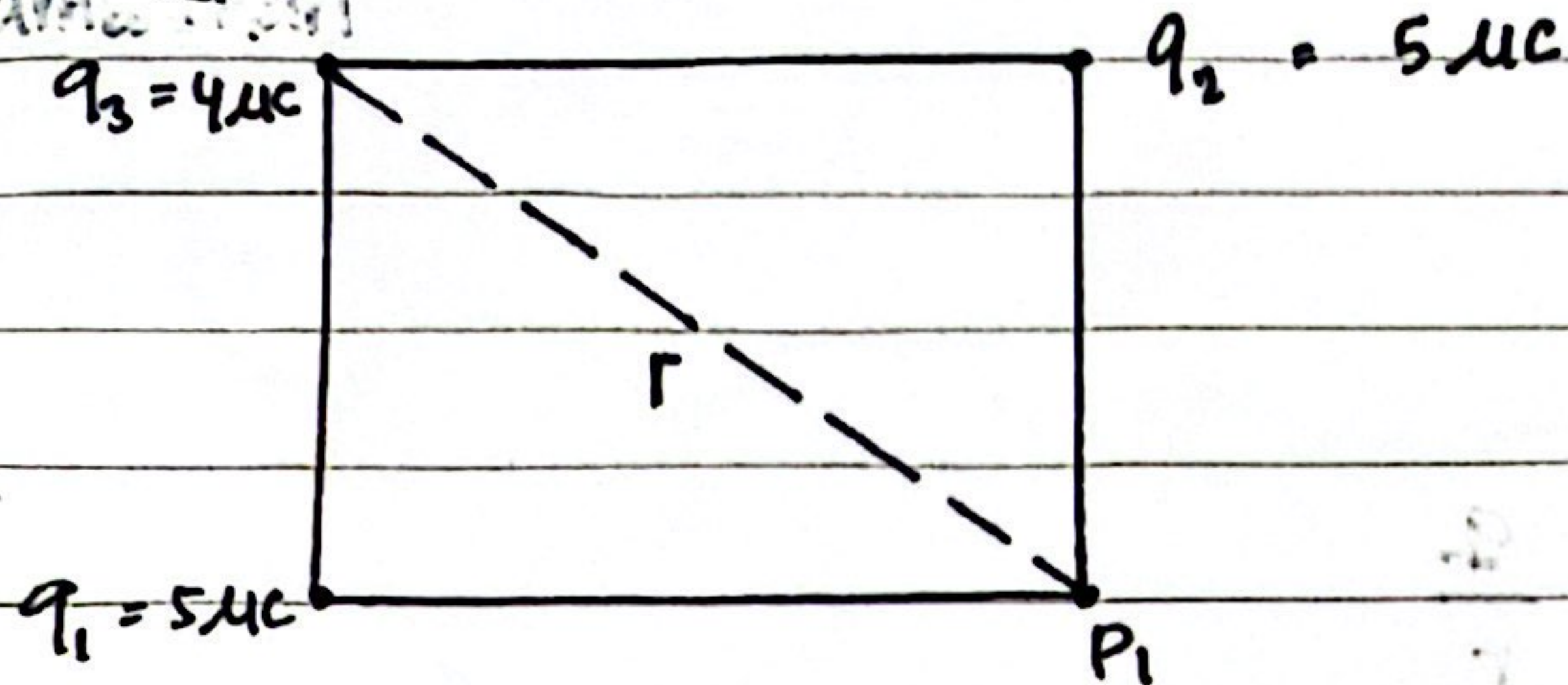
$$V_b - V_a = \frac{Q}{4\pi\epsilon_0} \left(\frac{1}{r_b} - \frac{1}{r_a} \right)$$

$$V_b - V_a = k \frac{Q}{R} \quad \text{di dalam}$$

$$V = k \frac{Q}{r}, \quad r > R \quad \text{di luar}$$

Soal 1

Diagram:



$$V = \frac{kq_1}{r_1} + \frac{kq_2}{r_2} + \frac{kq_3}{r_3}$$

$$= \left(\frac{5}{8} + \frac{5}{8} + \frac{(-4)}{\sqrt{8^2 + 8^2}} \right)$$

$$= k \left(\frac{5}{8} + \frac{5}{8} + \frac{(-4)}{\sqrt{128}} \right)$$

$$E = -\nabla V$$

$$\nabla \cdot E = -\nabla^2 V$$

$$\nabla \cdot \vec{E} = \frac{\rho}{\epsilon_0}$$

$$\nabla^2 V = \frac{\rho}{\epsilon_0}$$

Poisson

$$\nabla^2 V = 0$$

Laplace

P

z

$$\vec{E} = \frac{\lambda}{2\pi\epsilon_0 r}$$

$$\oint \vec{E} \cdot d\vec{a} = \frac{\lambda \cdot L}{\epsilon_0}$$

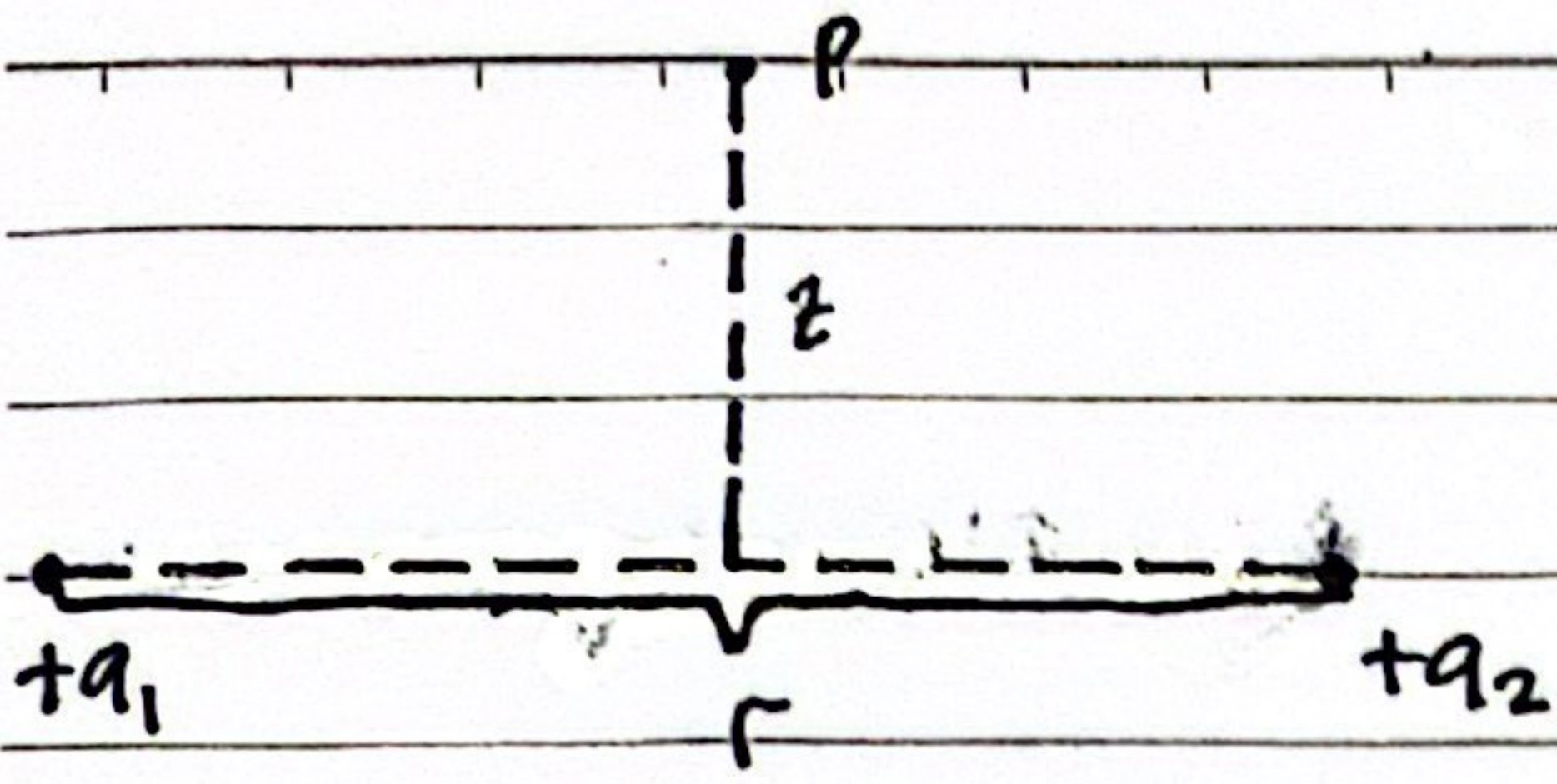
$$\vec{E} (2\pi r L) = \frac{\lambda \cdot L}{\epsilon_0}$$

$$E = \frac{\lambda}{2\pi\epsilon_0 r}$$

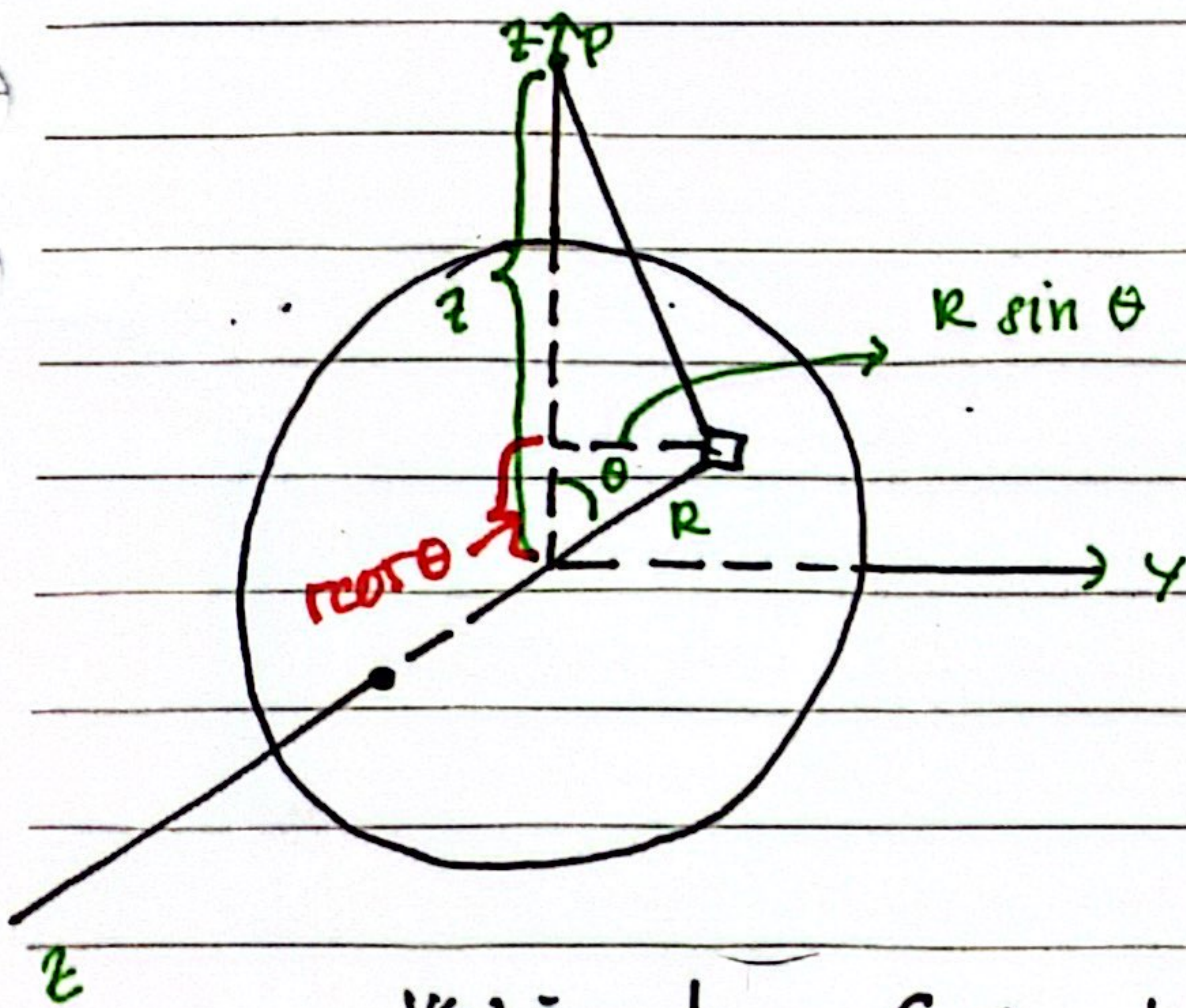
$$V = -\int \vec{E} \cdot d\vec{r}$$

$$= -\int \frac{\lambda}{2\pi\epsilon_0} \frac{1}{r} dr$$

$$= -\frac{\lambda}{2\pi\epsilon_0} \int \frac{1}{r} dr$$



$$V_p = ? k \left[\frac{q_1}{\sqrt{(\frac{1}{2}r)^2 + z^2}} + \frac{q_2}{\sqrt{(\frac{1}{2}r)^2 + z^2}} \right]$$



$$V_p = \frac{1}{4\pi\epsilon_0} \int \frac{q}{r} da$$

$$r^2 = R^2 + z^2 - 2Rz \cos \theta$$

$$\begin{aligned} r &= \sqrt{(R \sin \theta)^2 + (z - R \cos \theta)^2} \\ &= \sqrt{R^2 \sin^2 \theta + z^2 + R^2 \cos^2 \theta - 2zR \cos \theta} \\ &= \sqrt{R^2 (\sin^2 \theta + \cos^2 \theta) + z^2 - 2zR \cos \theta} \\ &= \sqrt{R^2 + z^2 - 2zR \cos \theta} \end{aligned}$$

$$V = \frac{1}{4\pi\epsilon_0} \int \frac{\sigma da}{r}$$

$$= \frac{1}{4\pi\epsilon_0} \iint \frac{\sigma da}{(R^2 + z^2 - 2Rz \cos \theta)^{1/2}}$$

$$= \frac{\sigma}{4\pi\epsilon_0} \int_0^\pi \int_0^{2\pi} \frac{r^2 \sin \theta d\theta d\phi}{(R^2 + z^2 - 2Rz \cos \theta)^{1/2}}$$

$$= \frac{\sigma R 2\pi}{4\pi\epsilon_0} \int_0^\pi \frac{\sin \theta d\theta}{(R^2 + z^2 - 2Rz \cos \theta)^{1/2}}$$

$$V_P = \boxed{\frac{1}{2}} \int_0^\pi \frac{d(\cos \theta)}{(R^2 + z^2 - 2Rz \cos \theta)^{1/2}}$$

$$= \boxed{\frac{1}{2}} \int_0^\pi (R^2 + z^2 - 2Rz \cos \theta)^{-1/2} d(\cos \theta)$$

$$= \boxed{\frac{1}{2}} 2 \left(R^2 + z^2 - 2Rz \cos \theta \right)^{1/2} \bigg|_0^\pi$$